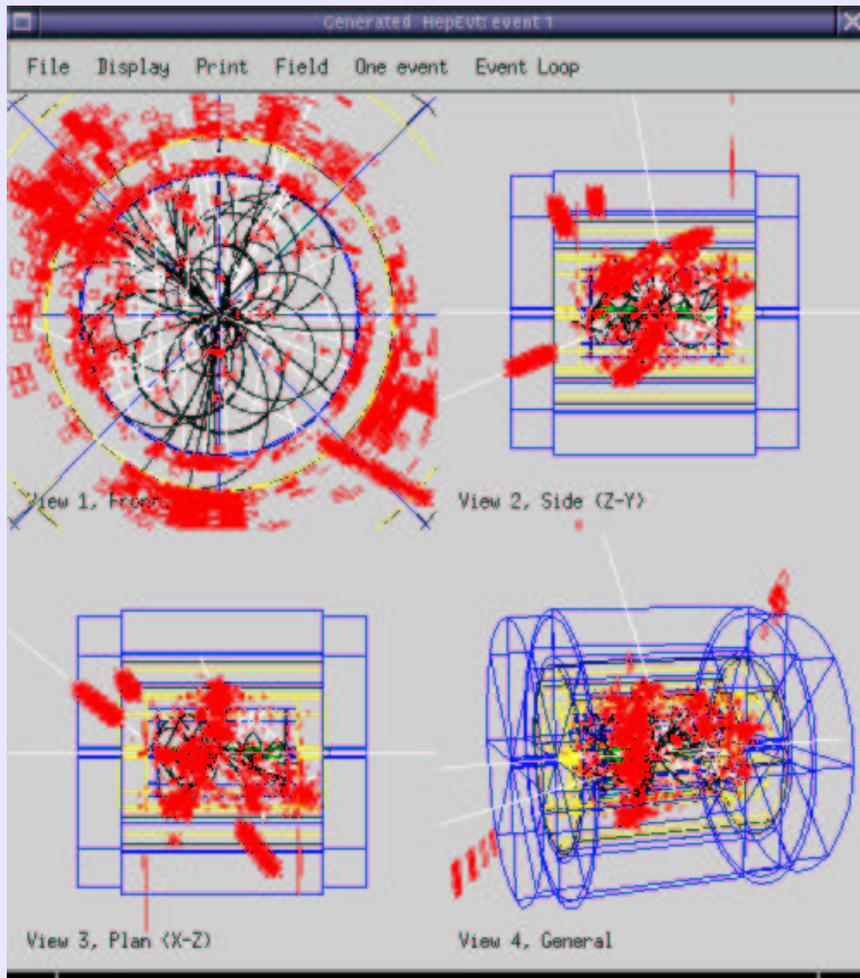


Top/QCD at the Linear Collider: Experimental Aspects



David Gerdes
University of Michigan

Loopfest
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Outline

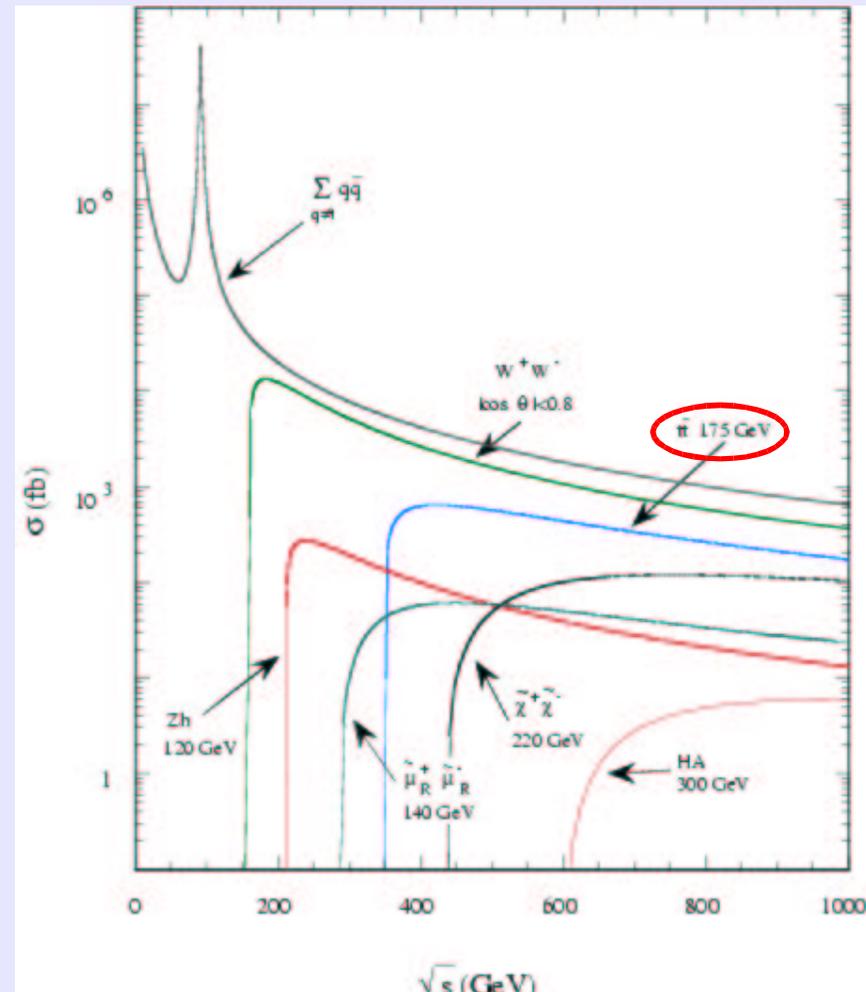
- Top Quark Physics
 - Measurements at threshold
 - Measurements above threshold
- QCD
 - Precision measurement of α_s
 - Q^2 evolution

Machine Parameters

	TESLA(500)	TESLA(800)	NLC(500)	NLC(1000)	Tevatron
E (GeV)	500	800	500	1000	2000
Lum. x 1E33	31	5	20	34	0.1
Rep rate (Hz)	5	3	120	120	--
Bunches/pulse	2820	4500	190	190	--
Bunch sep (ns)	337	189	1.4	1.4	396
$\sigma(x)$ at i.p.	553 nm	391 nm	245 nm	190 nm	30 μ m
$\sigma(y)$ at i.p.	5 nm	2 nm	2.7 nm	2.1	30 μ m
$\sigma(z)$ at i.p.	0.4 mm	0.3 mm	110 nm	110 nm	30 cm
δB(%)	3.3	4.7	4.7	10.2	0
P(e⁻) (%)	80–90	80–90	80–90	80–90	--
P(e⁺)(%)	60	60	--	--	--

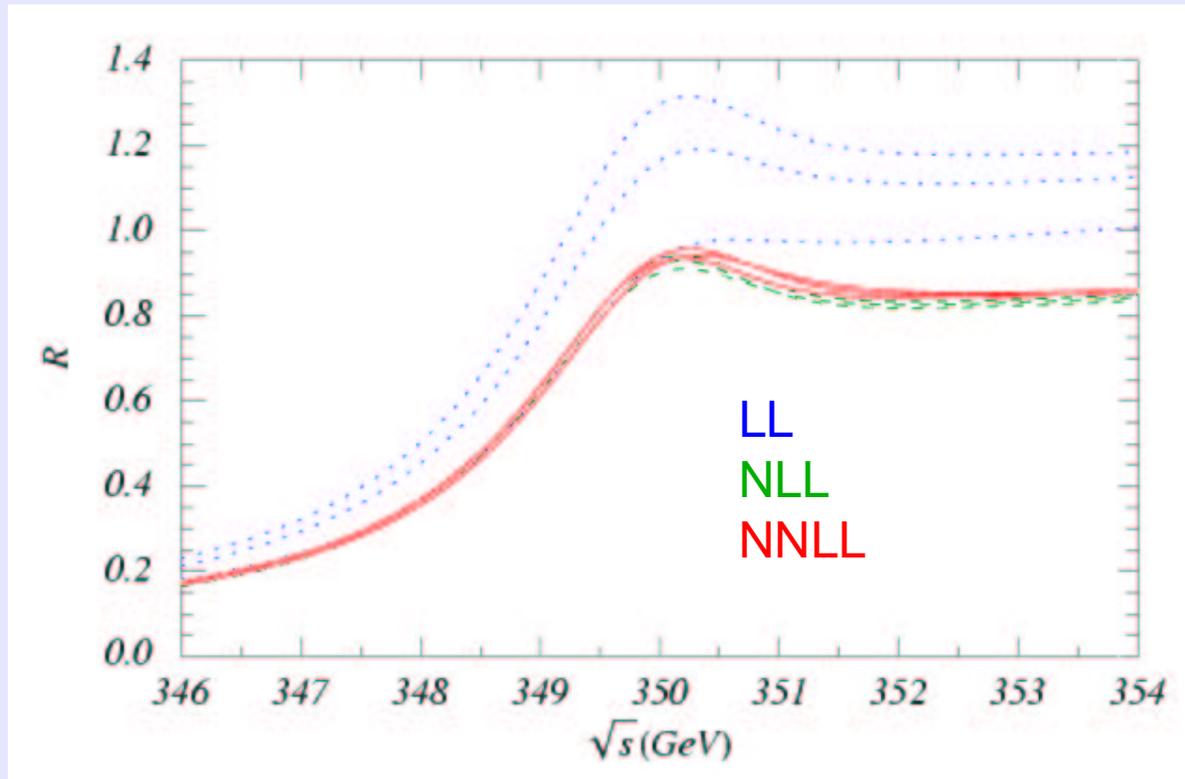
Top Production at the LC

- $\sigma_{t\bar{t}} \approx 0.6 \text{ pb}$ at $\sqrt{s} = 500 \text{ GeV}$
- $\Rightarrow 200,000 \text{ } t\bar{t} \text{ pairs / year}$ at TESLA design luminosity.
- **Why "do top"?**
 - $\Gamma_t \sim 1.3 \text{ GeV} \gg \Lambda_{\text{QCD}}$, so top decays before hadronization: Unique opportunity to observe the weak interactions of a bare quark.
 - m_t, Γ_t, g_{tth} etc. are precision EWK parameters.
 - Possible role in EWSB dynamics



Top Quark Threshold

Large top width provides IR cutoff, so can use pQCD to compute threshold cross section. Convergence is sensitive to mass definition used: pole and kinematic masses not IR-safe.

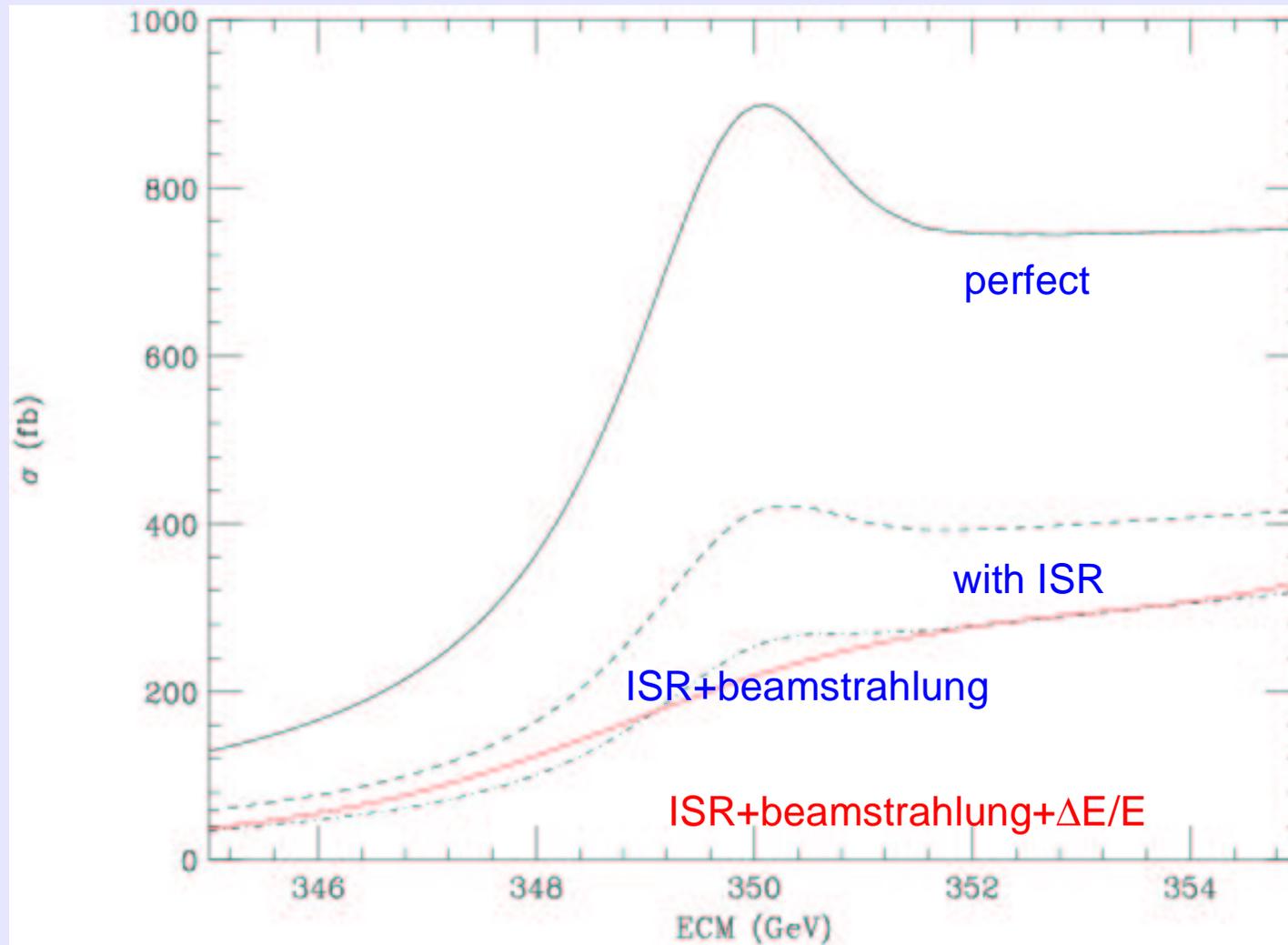


Hoang, Manohar, Stewart, Teubner, hep-ph/0107144

Best results come from using the **1S mass** definition ($\frac{1}{2}$ the mass of the lowest $t\bar{t}$ bound state, evaluated in the limit $\Gamma_t \rightarrow 0$) combined with a **velocity resummation**.

Also, reduces previous large correlation between m_t and α_s .

Machine Effects on Top Threshold Lineshape

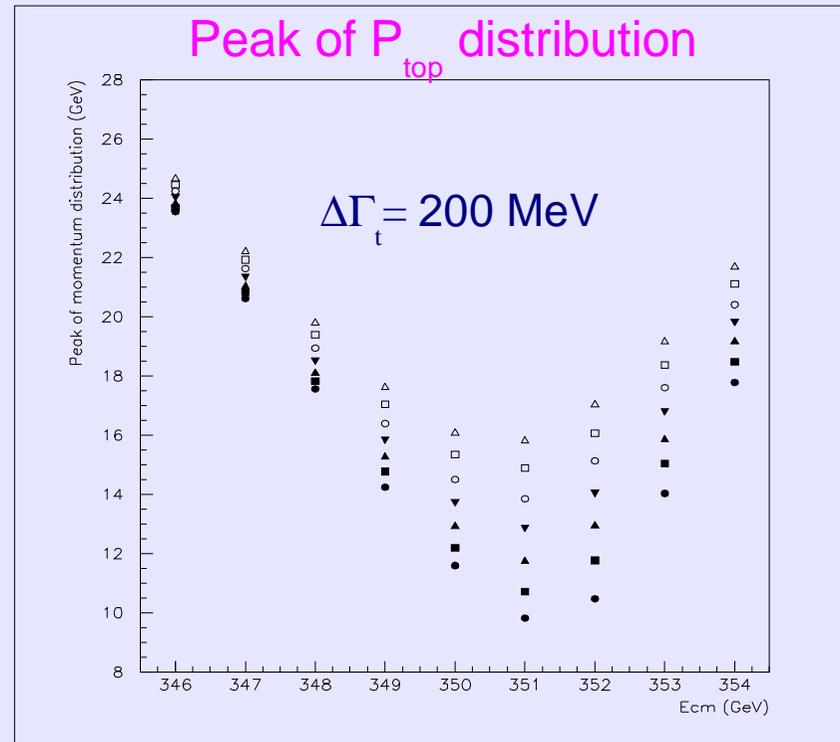
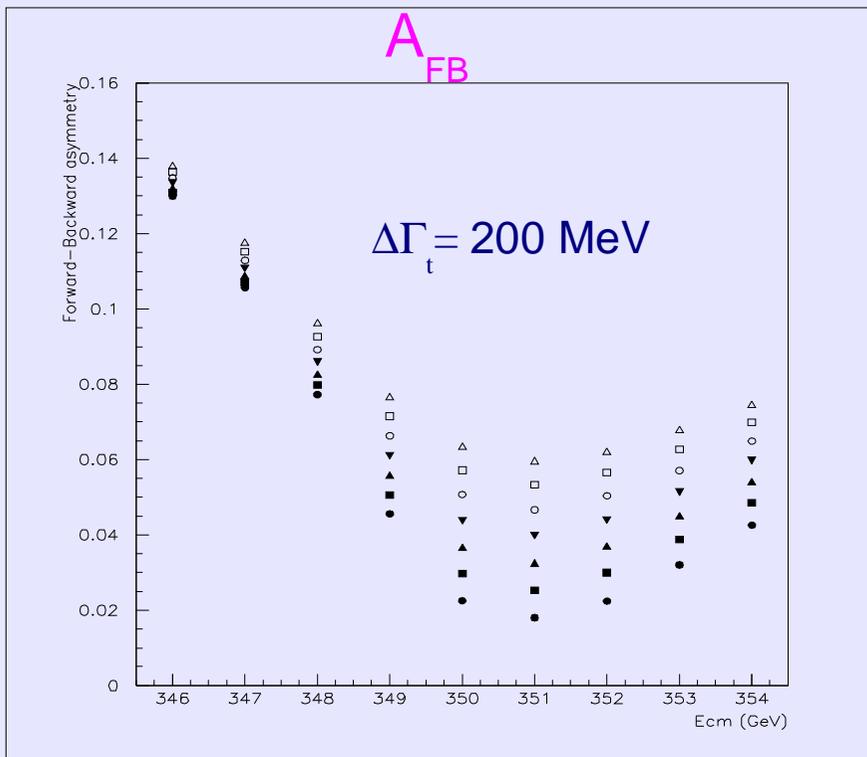


Note: can reduce beamstrahlung at cost of luminosity: optimization issue for experimentalists.

Threshold Measurements

Recent analysis by R. Miquel, M. Martinez (Chicago LCWS '02):

- Assume 300 fb^{-1} and 9 scan points plus one well below threshold for background determination.
- Use the cross section and, in addition, the observables A_{FB} and P_{peak}

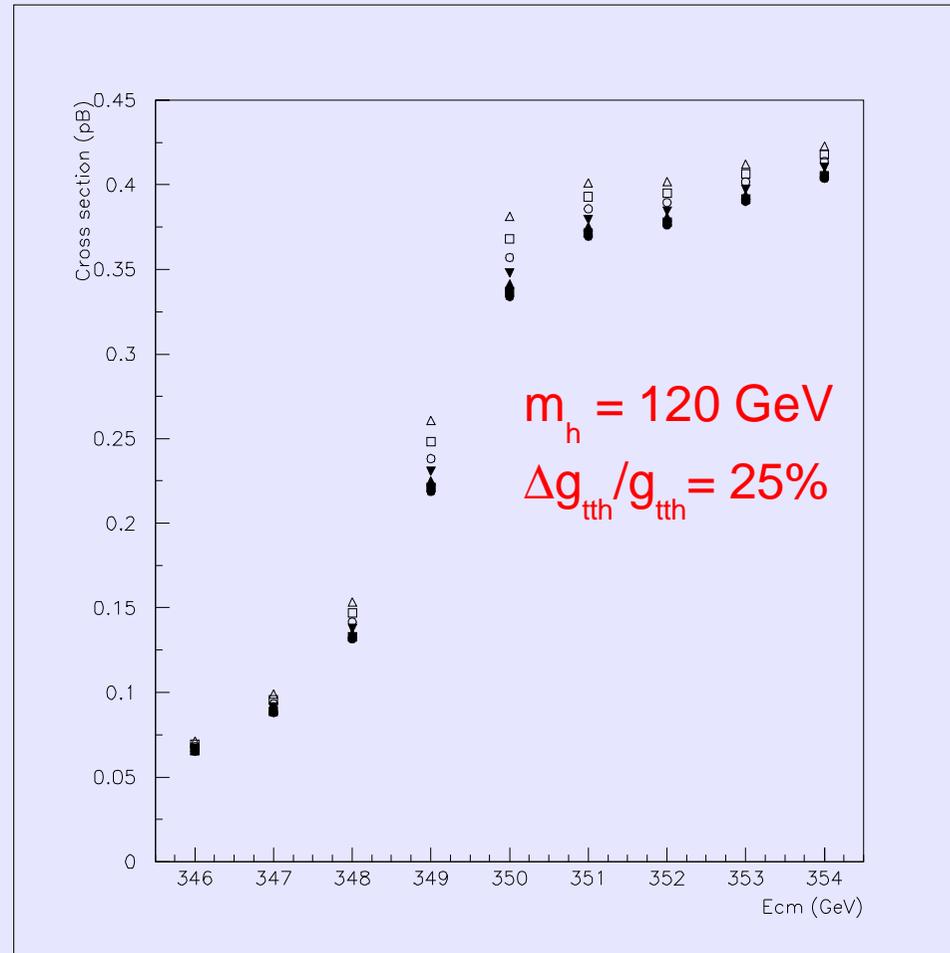


Threshold Results

- **Mass:** $\Delta m_t = 16 \text{ MeV}$, $\Delta \alpha_S = 0.0011$
 - Using cross section only: $\Delta m_t = 24 \text{ MeV}$, $\Delta \alpha_S = 0.0017$.
 - Γ_t , g_{tth} fixed at SM values; assume $m_h = 120 \text{ GeV}$, $\alpha_s(M_Z) = 0.120$.
 - Theory error: $\sim 100 \text{ MeV}$.
- **Width:** allow to vary in a 3-parameter fit.
 - $\Delta \Gamma_t = 32 \text{ MeV}$, $\Delta m_t = 18 \text{ MeV}$, $\Delta \alpha_S = 0.0015$
 - 2% exp. uncertainty on width

Top–Higgs Yukawa Coupling at Threshold

- Small effect in all observables, diminishes rapidly for $m_h > 120$ GeV
- If all other parameters fixed (best–case scenario), find $\Delta g_{tth}/g_{tth} = +17\% - 24\%$
- Fit m_t, Γ_t, g_{tth} simultaneously with 0.001 constraint on α_s :
 $\Delta g_{tth}/g_{tth} = +33\% - 57\%$
 (with correlations up to 85%)
 Also $\Delta m_t = 30$ MeV, $\Delta \Gamma_t = 33$ MeV.
- \Rightarrow This measurement looks hard.

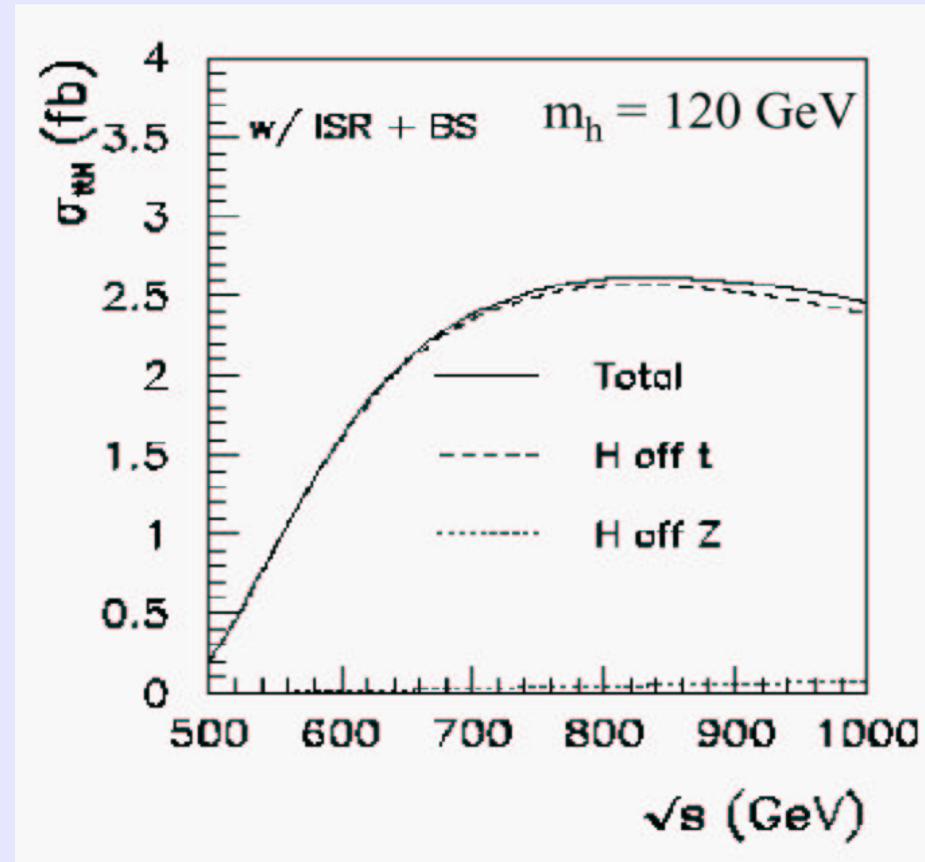


Loopfest Wish List for Top Threshold

- Measurements may be dominated by theory systematics.
- Much progress in recent years on threshold cross section. How much more can calculation be improved? Better quantification of systematics?
- Improved calculations of other threshold observables (NLL calculations currently used for A_{FB} , P_{peak} , e.g.)

$t\bar{t}H$ production and the Top Yukawa Coupling

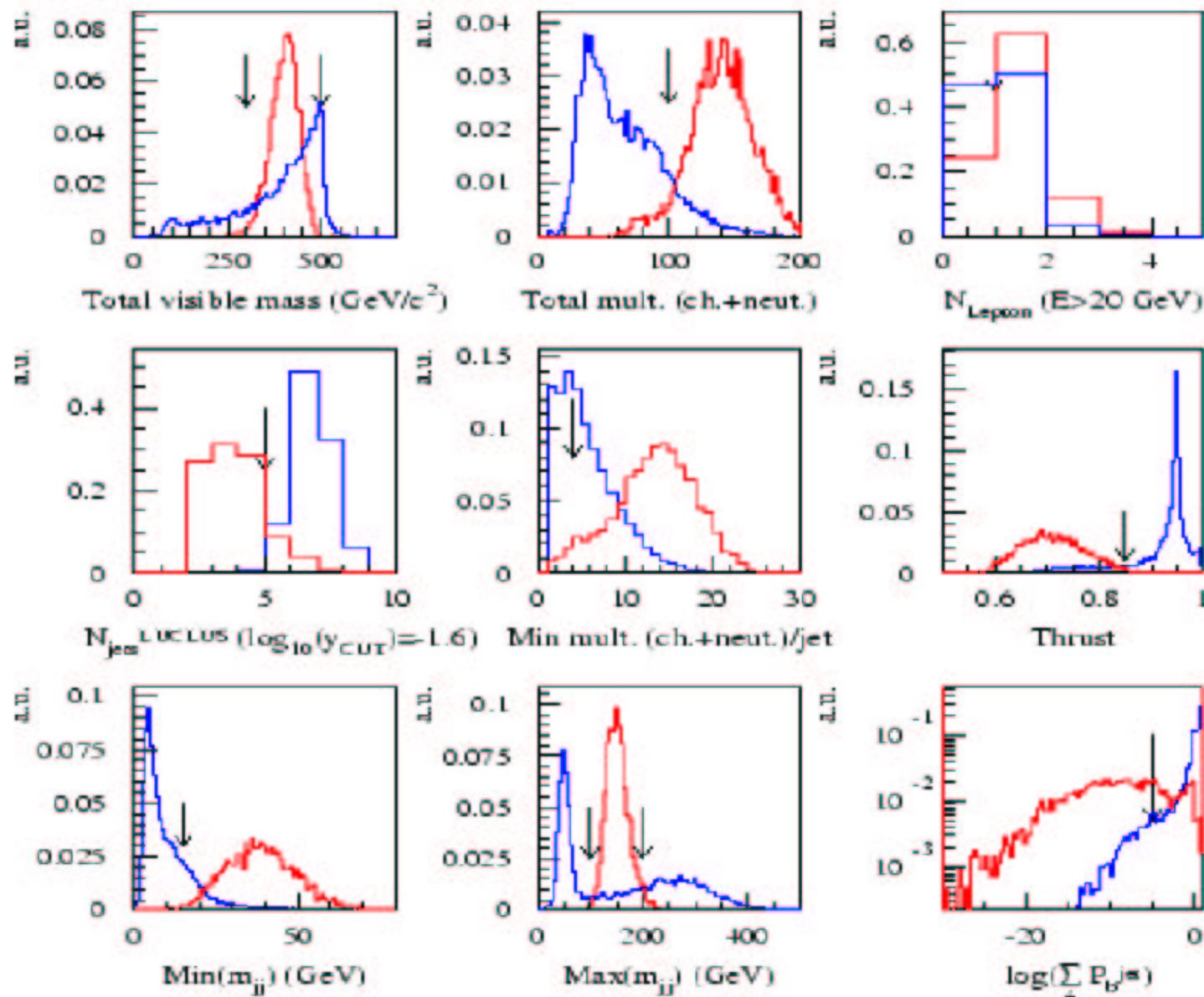
- $e^+e^- \rightarrow t\bar{t}H \rightarrow WbWb\ bb$
- Very complicated final state:
 - Up to 8 jets
 - 4 b's
 - Many kinematic constraints
- Tiny cross section (~ 2 fb), with backgrounds ~ 3 orders of magnitude higher.
- Interfering backgrounds from EWK ($t\bar{t}Z$), QCD ($g \rightarrow b\bar{b}$)
- Non-interfering backgrounds
 - Dominantly $e^+e^- \rightarrow t\bar{t}$
 - Formally smaller number of partons, but can enter the selection due to hard gluon radiation, detector effects, and their very large cross sections



$t\bar{t}H$ Analysis Strategy (Juste, Merino)

- **Lots of luminosity:** 1 ab^{-1} at 500 GeV
- Loose preselection on semileptonic final states (9 event variables)
 - Retains ~45% of signal while reducing bkgd by 2–3 orders of magnitude.
 - Still have only ~36 signal events, ~3800 bkgd events, about half of which are $t\bar{t}$.
- Then apply multivariate analysis to remaining events. Neural net that uses the 9 preselection variables plus 14 more.

ttH Preselection



— Signal
— Bkgds

ttH Sensitivity

- For the semileptonic channel, $L=1 \text{ ab}^{-1}$, $m_H=120$, find

$$\left(\frac{\Delta g_{ttH}}{g_{ttH}} \right)_{stat} \approx 0.33$$

- Only $N \sim 11$ signal events, ~ 54 background events survive.
- Assuming $\sqrt{2}$ improvement from fully hadronic channel,

$$\left(\frac{\Delta g_{ttH}}{g_{ttH}} \right)_{stat} \approx 0.23$$

- **NB:** K-factors not used for signal or bkgd processes. Know $K \sim 1.5$ for ttH @ 500 GeV (Dawson and Reina; Dittmaier et al.); would improve sensitivity by 22%.
K-factors for backgrounds?
- Factor of **3–4** improvement at $\sqrt{s} = 800 \text{ GeV}$.

Top Production/Decay Form Factors

General neutral-current couplings:

$$\Gamma_{t\bar{t}\gamma,Z}^\mu = ie \left\{ \gamma^\mu \left[F_{1V}^{\gamma,Z} + F_{1A}^{\gamma,Z} \gamma^5 \right] + \frac{i \sigma^{\mu\nu} q_\nu}{2m_t} \left[F_{2V}^{\gamma,Z} + F_{2A}^{\gamma,Z} \gamma^5 \right] \right\}$$

SM: only F_{1V}^γ , F_{1V}^Z , F_{1A}^Z are nonzero.

F_{2V} \Rightarrow weak magnetic dipole moment ($\neq 0$ in some strong EWSB models)

F_{2A} \Rightarrow weak electric dipole moment, violates CP. ($\neq 0$ in some SUSY models)

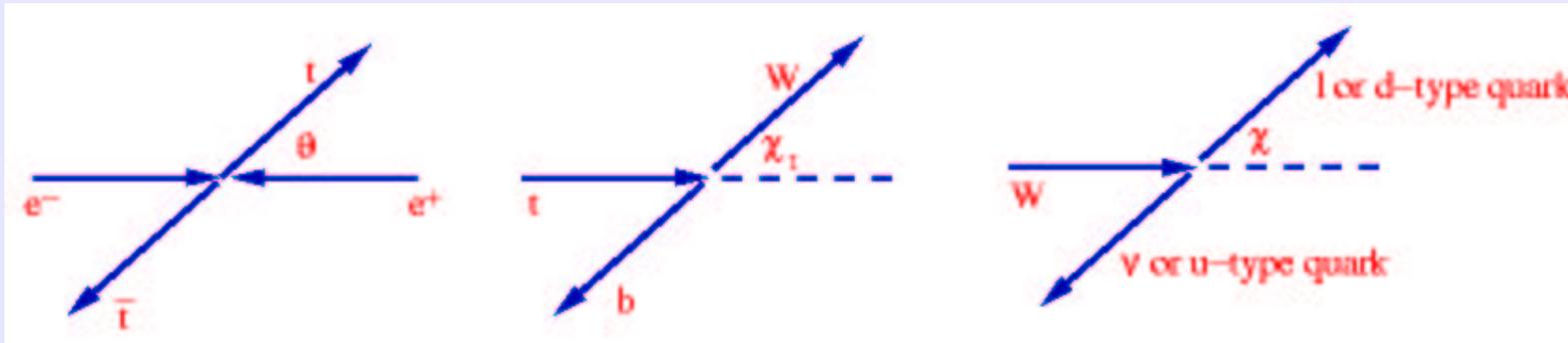
General charged-current couplings:

$$\Gamma_{tbW}^\mu = \frac{-g}{\sqrt{2}} V_{tb} \left\{ \gamma^\mu \left[F_{1L} P_L + F_{1R} P_R \right] + \frac{i \sigma^{\mu\nu} q_\nu}{2m_t} \left[F_{2L} P_L + F_{2R} P_R \right] \right\}$$

SM: only F_{1L} is nonzero.

Couplings Measurement

Information about the form factors is encoded in the **helicity angles**:



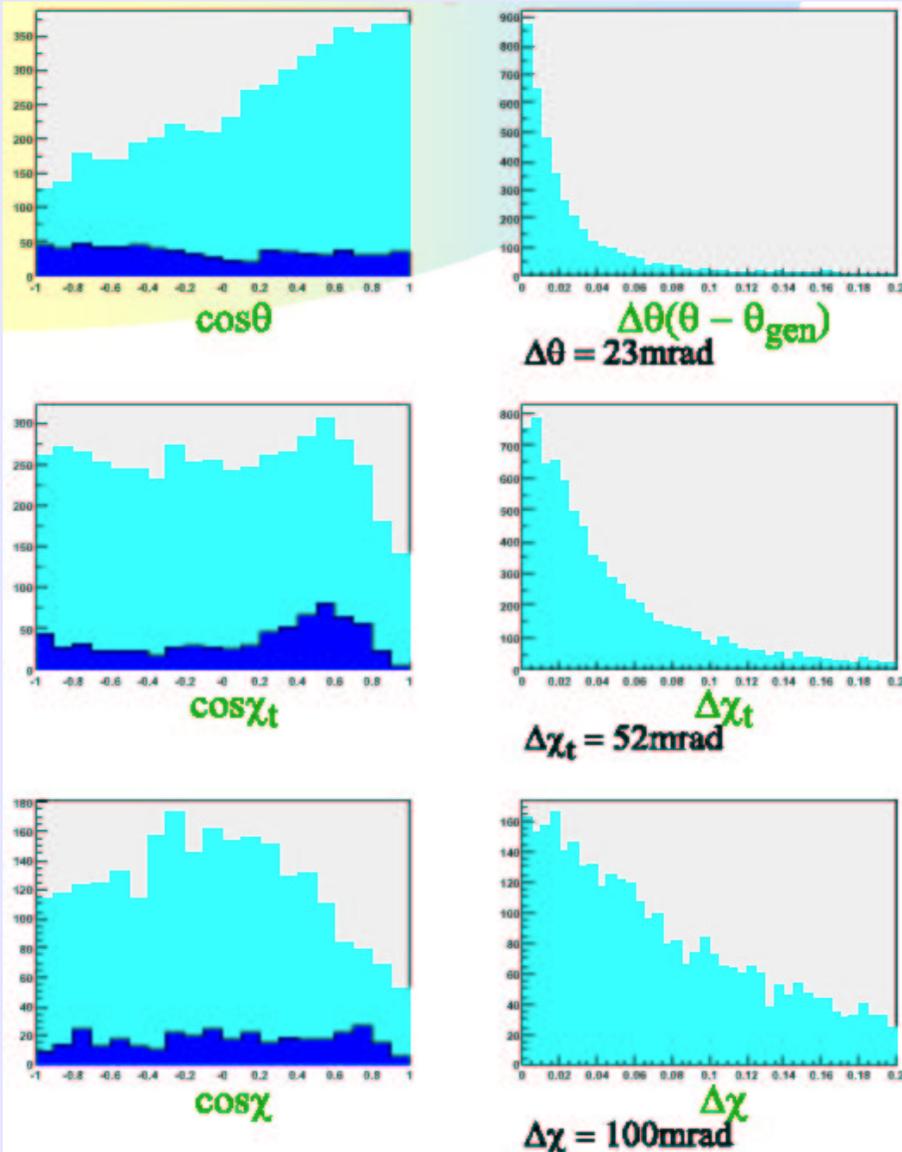
Focus on the semileptonic (4-jet) final state:

- Charge of lepton tags t or \bar{t}
- Can also use charge of b -tagged jet ($\epsilon=57\%$, purity = 83%)
- Four-momentum of the leptonic t -quark from the opposite hadronically-decaying top.

Analysis strategy (M. Iwasaki, 2002): assume 100 fb^{-1} at $\sqrt{s} = 500 \text{ GeV}$

- Force 4-jet final state using JADE clustering algorithm ($\epsilon = 60\%$)
- Cut on 2-jet invariant mass (W identification) and 3-jet mass (top ID) (50%)
- b -tag using SLD-esque algorithm ZVTOP. (67%)

Reconstructed Helicity Angles and Results



Axial form factors from maximum likelihood analysis:

68% C.L. sensitivities

	F_{1A}^γ	F_{1A}^Z	F_{2A}^γ	F_{2A}^Z
$P_{e^-} = -0.8$	0.011	0.013	0.016	0.049
$P_{e^-} = -0.8, P_{e^+} = 0.5$	0.009	0.011	0.021	0.033
No polarization	0.011	0.014	0.013	0.059
$P_{e^-} = +0.8$	0.011	0.015	0.014	0.052

Vector form factors from L-R asymmetry (200 fb^{-1})

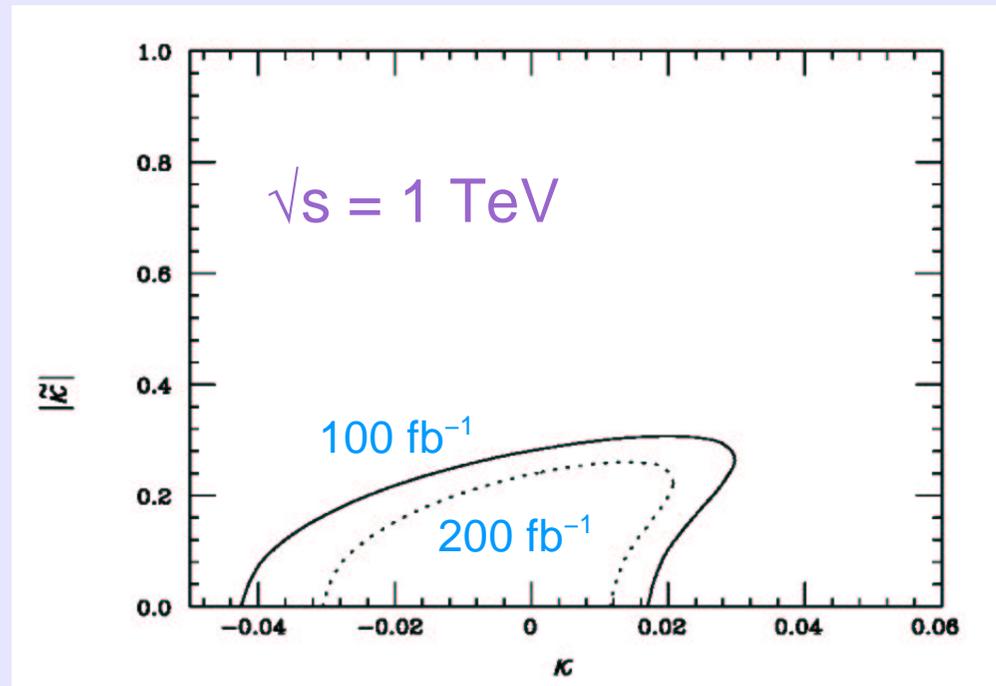
- $F_{1V}^\gamma \sim 0.05$
- $F_{1V}^Z \sim 0.01$
- $F_{2V}^\gamma \sim 0.04$
- $F_{2V}^Z \sim 0.01$

Top Quark Strong Moments

- Top may play a role in new strong interactions, which can modify top couplings through higher-dimension operators.
- Simplest, CP-conserving form:
- $\kappa, \tilde{\kappa}$ both zero in SM.

$$L = g_s t T_a \left(\gamma_\mu + \frac{i}{2m_t} \sigma_{\mu\nu} (\kappa - i\tilde{\kappa}\gamma_5) q^\nu \right) t G_a^\mu$$

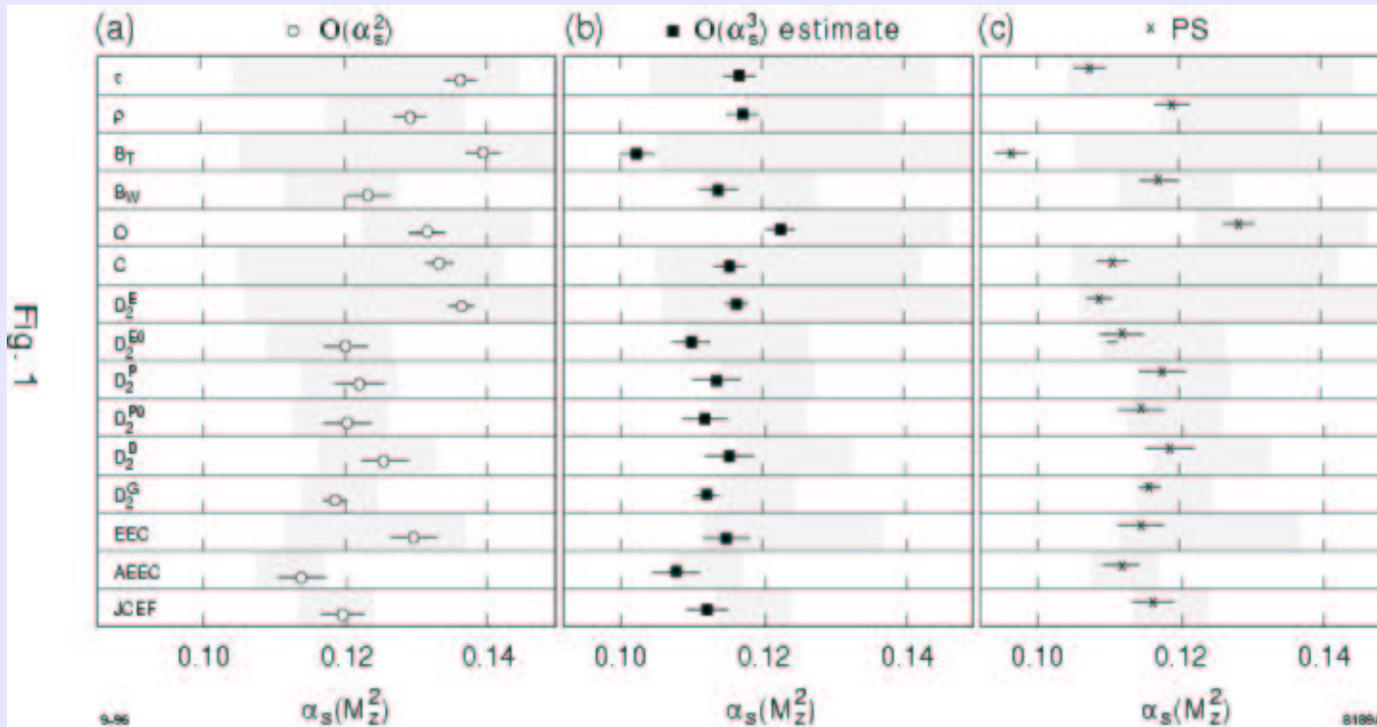
Affects energy spectrum and angular distribution of hard gluon radiation above threshold.



Precision Measurement of α_s

- Why?
 - RG extrapolation of the gauge couplings constrains / tests physics at the GUT scale. Currently limited by ~few percent uncertainty on α_s .
 - Measure Q^2 -dependence over wide range to test QCD or reveal new physics.
- Main technique: event shape observables
 - E.g. thrust, sphericity, jet masses, jet rates...
 - Fit each observable to a pQCD prediction, allowing α_s to vary.
 - Statistical uncertainties currently ~ 0.001 , experimental systematics at level of ~ 0.001 – 0.004 .

Theory Uncertainty Dominates



Points: measured values with exp. errors

Gray bands: theory uncertainty

P. N. Burrows, hep-ex/9612008

Ratio Method (GigaZ)

- Measure inclusive ratios $\Gamma_Z^{\text{had}}/\Gamma_Z^{\text{lept}}$, $\Gamma_\tau^{\text{had}}/\Gamma_\tau^{\text{lept}}$, which depend on α_s through radiative corrections.
- LEP data (16M Z's): $\Delta\alpha_s = \pm 2.5\%$ (stat.) $\pm 1\%$ (exp. syst.)
- GigaZ: $\Delta\alpha_s = \pm 0.4\%$ (stat.)
- Theory uncertainties controversial: 1–2%, maybe as high as 5%.
- If theory uncertainties clarified/improved, this could be a competitive ~1%–level measurement.

α_s Wish List

- What we have:
 - 5 partons at tree level
 - 4 partons at one loop
 - parts of 3 parton amplitudes at 2 loops
 - Ratio method calculated to NNLO
- What we need for a 1% measurement:
 - Full NNLO calculation of jet rates!
 - For ratio method, need NNNLO calculation, as well as NLO(?) EWK corrections.
 - This is left as an exercise...

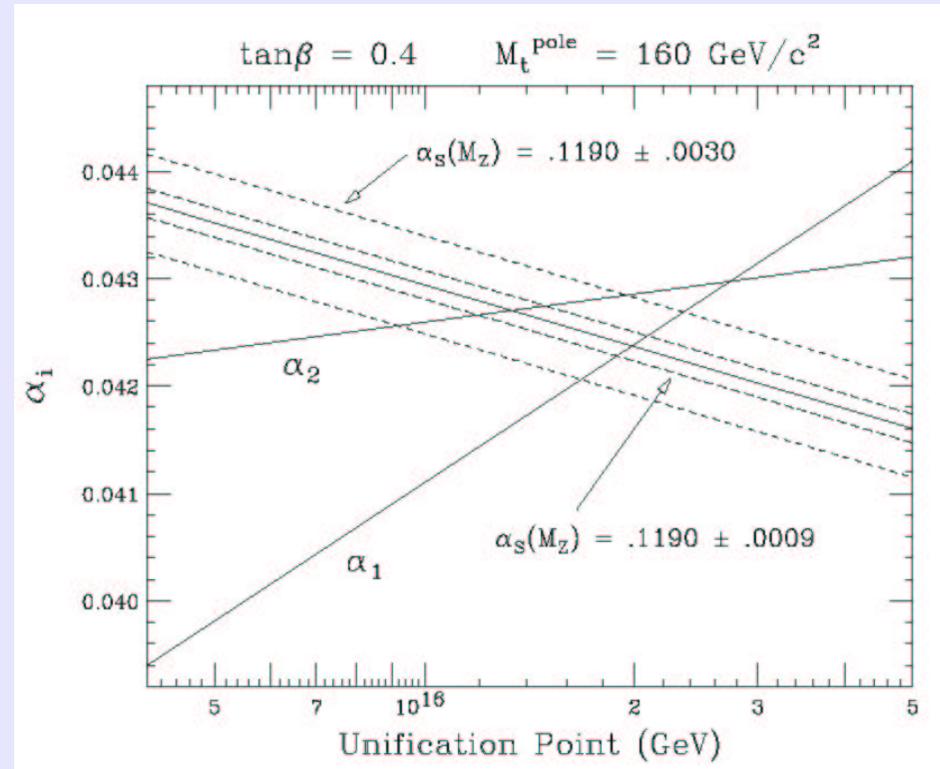
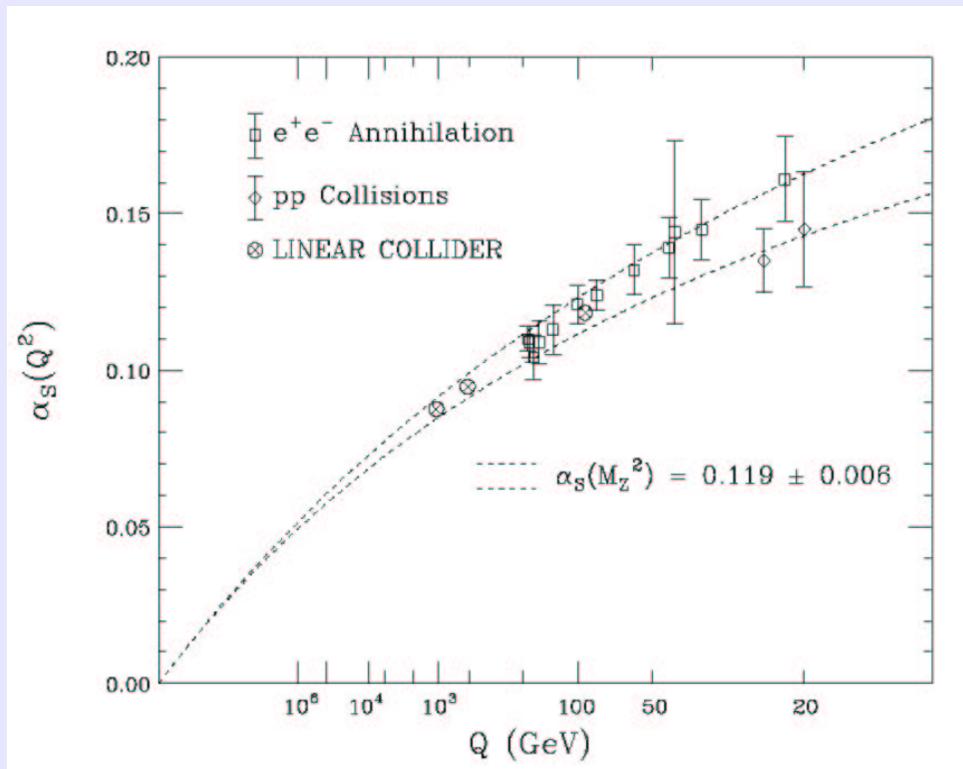
Q^2 Evolution of α_s

- For the preceding measurements, we normalize to $\alpha_s(M_Z^2)$, using the QCD β -function to connect measurements at different scales.
- But want to test this running explicitly, since the β -function itself is an important prediction of QCD.
- **Linear collider is well-suited to high-precision measurements under similar experimental conditions over a large lever arm in Q^2 .**

Measurement of Q^2 Evolution

- LC at $\sqrt{s}=91, 500, 1000$ GeV
- Use jet rates/shapes at all energies, and ratio technique at Z pole.
- Assume 1% theory uncertainty.

Resulting improvement in extrapolation to GUT scale with 1% measurement:



Conclusions

- Top and QCD illustrate many of the challenges and rewards of the LC physics program.
- At the same time, they only scratch the surface of the physics we hope to do there!
- We need calculations and theories worthy of the machine and detectors we are going to build.
- For the LC physics program to reach its potential, your help is essential!