

The plan:

Neutrinos Now... *Today*

Neutrinos Next:

Neutrinos and the New Paradigm

Neutrinos and the Unexpected

Neutrinos and the Cosmos

Neutrino Opportunities

Tomorrow

Today
Tomorrow
Tomorrow

“Neutrinos Next” will follow

The APS-sponsored
Multidivisional study on...
The Future of Neutrino Physics

Working Groups:

Solar & Atmospheric Neutrinos

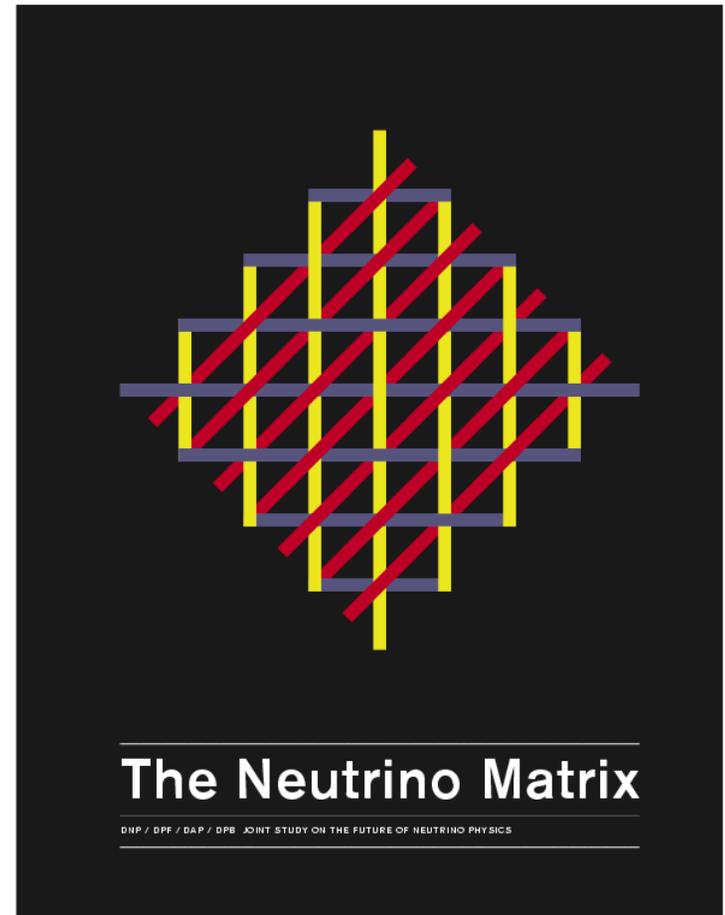
Reactor Neutrinos

Super Beams

Neutrino Factory & Beta Beams

Neutrinoless Double Beta Decay

Astrophysics & Cosmology



Disclaimers:

These lectures are on understanding neutrinos,
as opposed to using neutrinos to understand other physics.

I define a “neutrino experiment” as an experiment that
is relevant to understanding neutrinos

There are many experiments...

There are many experimental questions...

These are “Janet’s Picks”

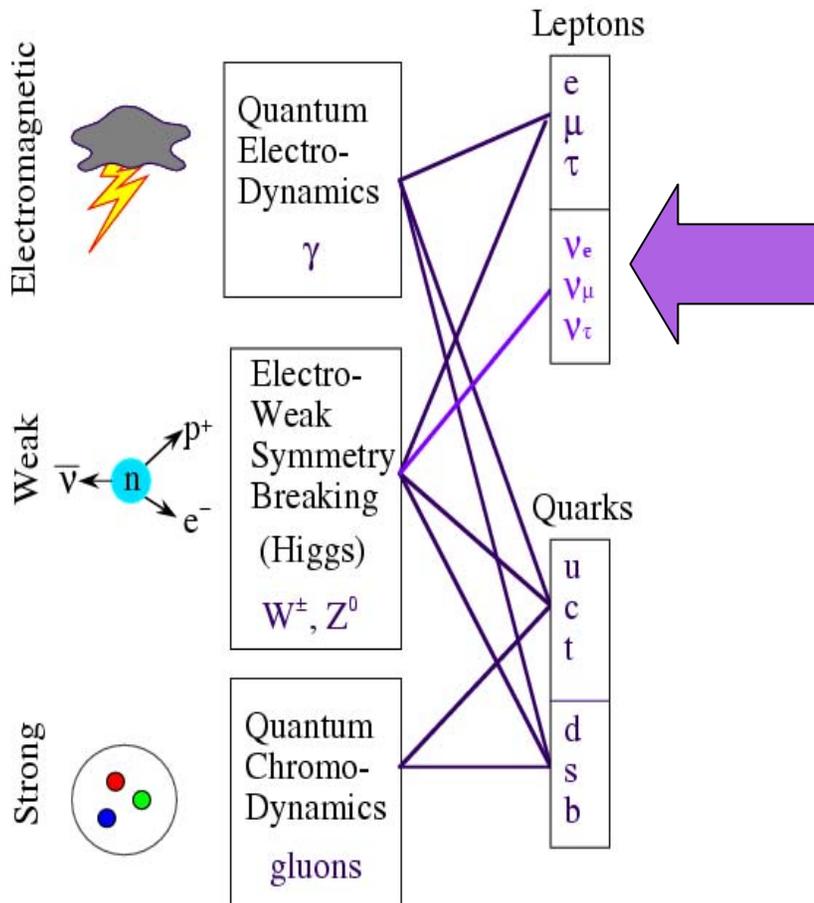
I identify statements that are “Janet’s Opinions”

I am focussing mainly on now and the future...

Neutrinos Now:

Setting up the Experimental Questions

SM Neutrinos in a nutshell..



- Only interact via the “weak force”
- Interact thru W and Z bosons exchange is (V-A)
 - Neutrinos are left-handed (Antineutrinos are right-handed)
- Neutrinos are massless
- Neutrinos have three flavors
 - Electron $\nu_e \rightarrow e$
 - Muon $\nu_\mu \rightarrow \mu$
 - Tau $\nu_\tau \rightarrow \tau$

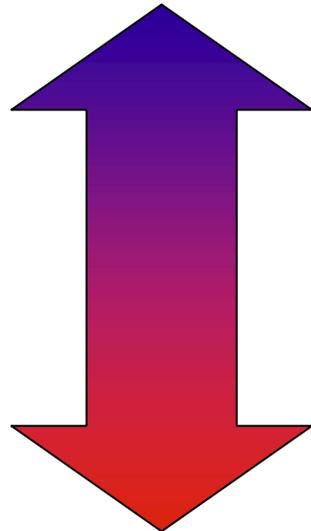
The interaction depends upon the ν energy...

The main sources

Reactors,
The Sun

Cosmic rays,
accelerators

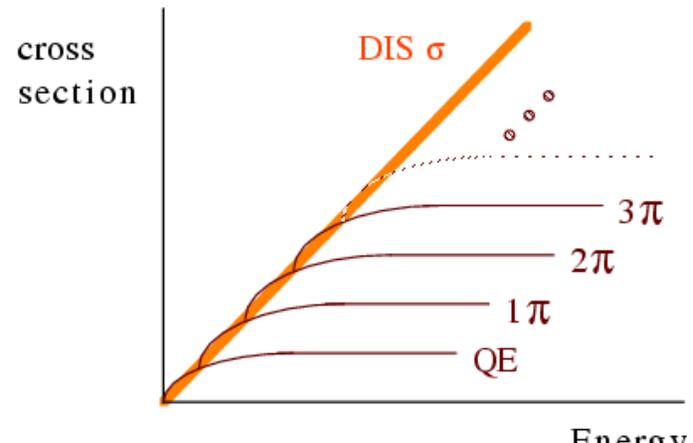
Few MeV



Multi-GeV+

Useful interactions

Elastic (esp. $\nu e \rightarrow \nu e$)
Quasielastic ($\nu N \rightarrow \ell N'$)
Single Pion Production
(resonant & coherent)
Deep Inelastic Scattering

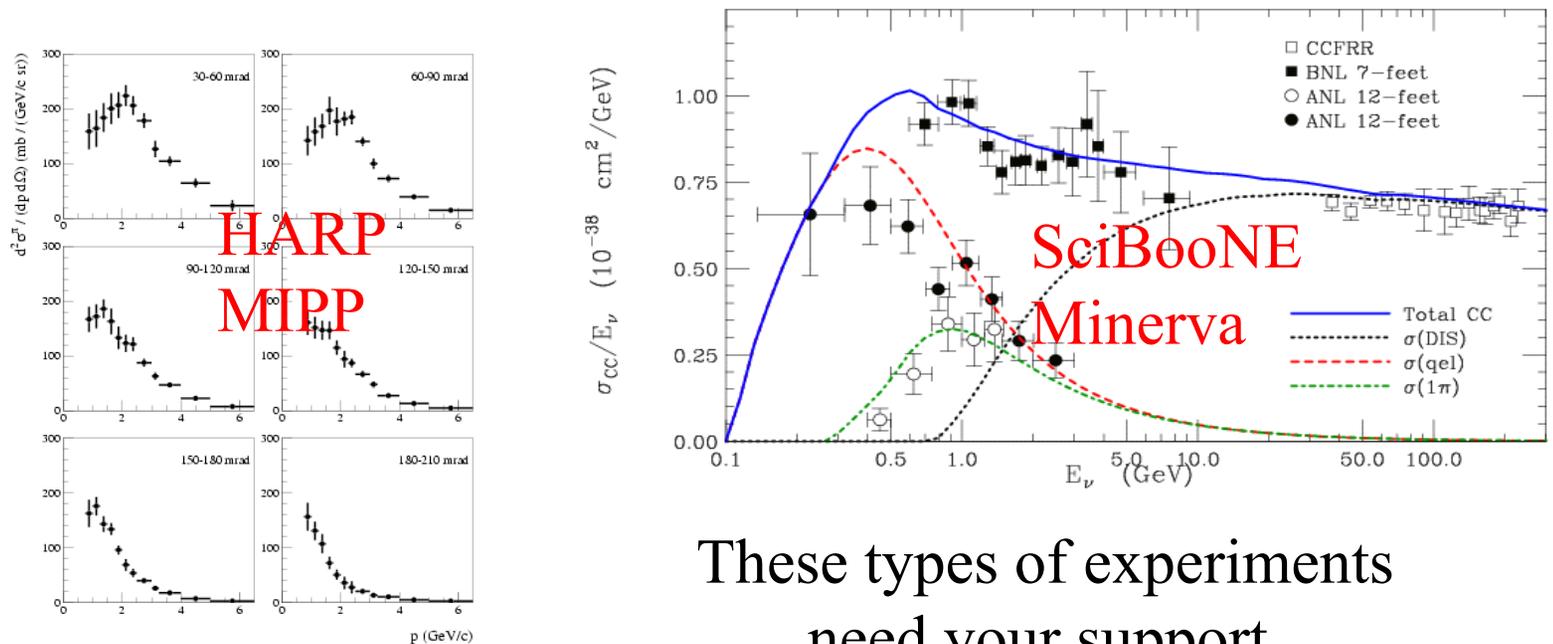


Janet's opinion:

Nearly all “new physics” searches experiments require accurate knowledge of the beam and cross section.

Otherwise you end up with effects like the Hera “high Q^2 events”

In neutrino physics, these are experiments like:



These types of experiments need your support

Why study neutrinos?

Theory-based Reasons

Even within the Standard Model,
Neutrinos are not “standard”!

Because of their unique properties,
BSM effects may show up in neutrino interactions

Experimentally-based Reasons

The Standard Model characteristics show 5σ disagreement with data.

The “non-standardness” of the SM neutrino...

- The only fermion that does not carry electric charge
- The only fermion that is only left handed
- The only fermion which is massless

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- The only fermion that does not carry electric charge

- The only fermion that is only left handed

- The only fermion which is massless

These two are related...

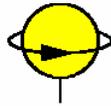
A quick reminder about parity violation...

All spin 1/2 particles have “helicity”

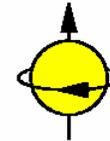
The projection of spin along the particle's direction

The operator: $\sigma \cdot \mathbf{p}$

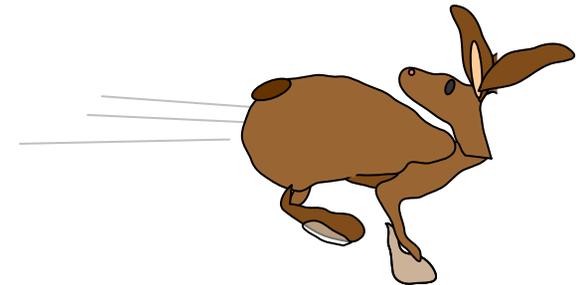
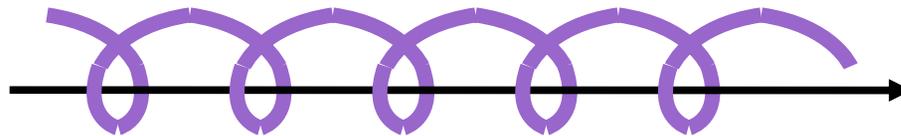
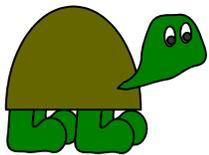
right-helicity



left-helicity



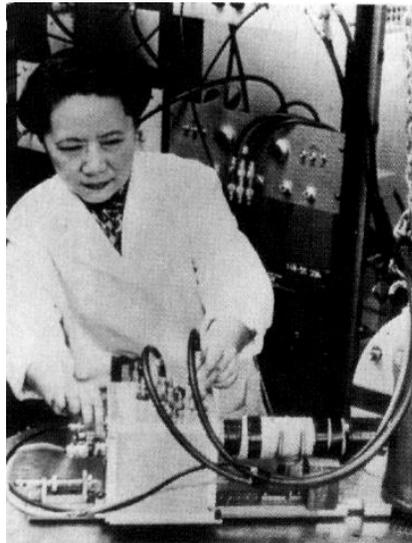
Frame dependent (if particle is massive)



Handedness (or chirality) is the Lorentz-invariant counterpart
Identical to helicity for massless particles (standard model ν 's)

All particles except neutrinos come in LH & RH
Neutrinos are only observed as LH (and antineutrinos RH)

Neutrinos have a specific “handedness”



50th anniversary of
CS Wu's experiment
is next December!



How do you enforce the law of left-handedness?

Well... what couples left-handed particles to right?

A Dirac mass term
in the SM Lagrangian:

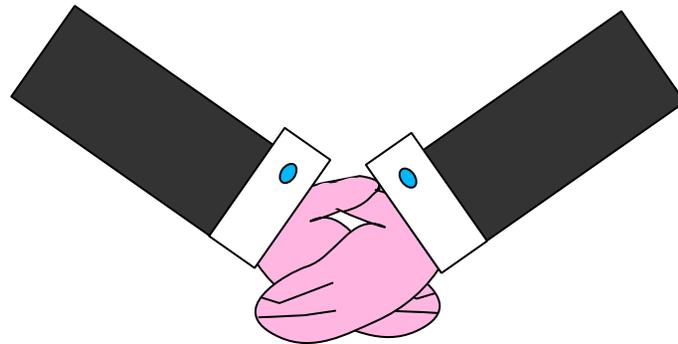
$$m(\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L)$$

If you want to build parity violation into “the law”
you have to keep this term out of the Lagrangian...
a simple solution is: $m=0$

The SM neutrino may be sensitive to BSM effects...

- Not “obscured” by the “strongest” interactions... strong and electromagnetic.
- singlet partners can be motivated if handedness is intrinsic to the EW Bosons.

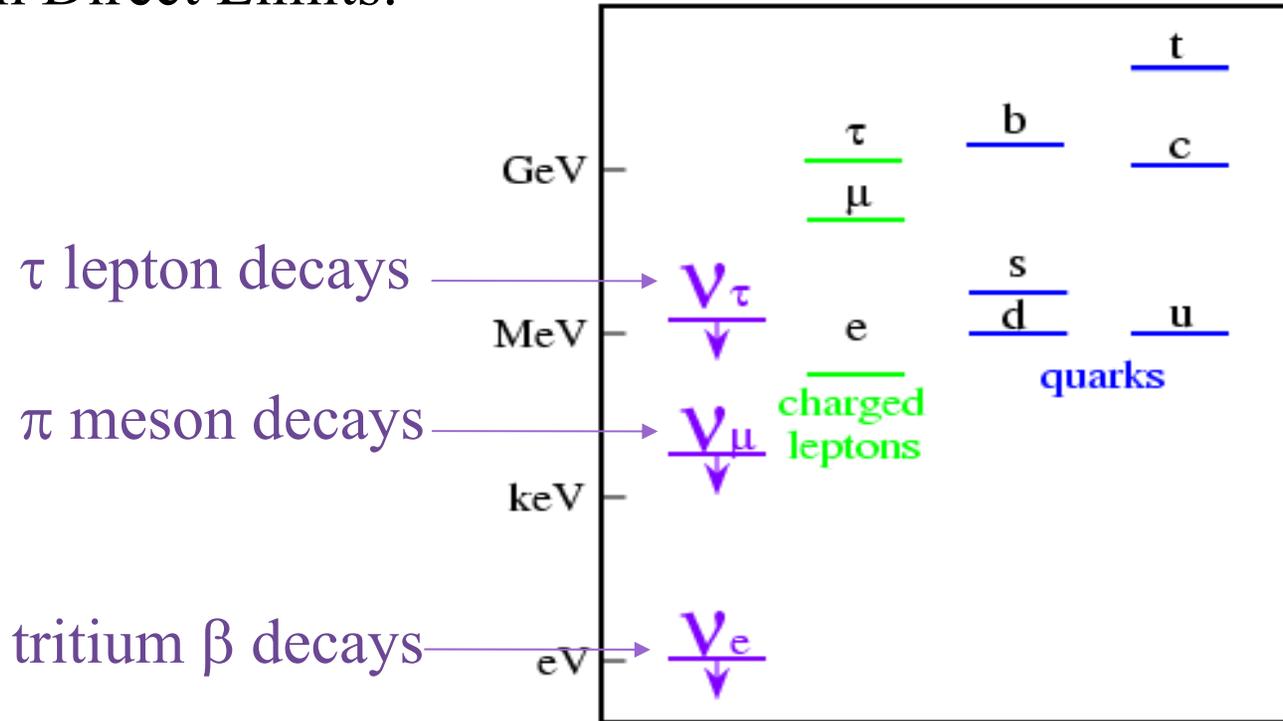
"The W only shakes with the left hand"



The neutrino mass model is simply wrong...

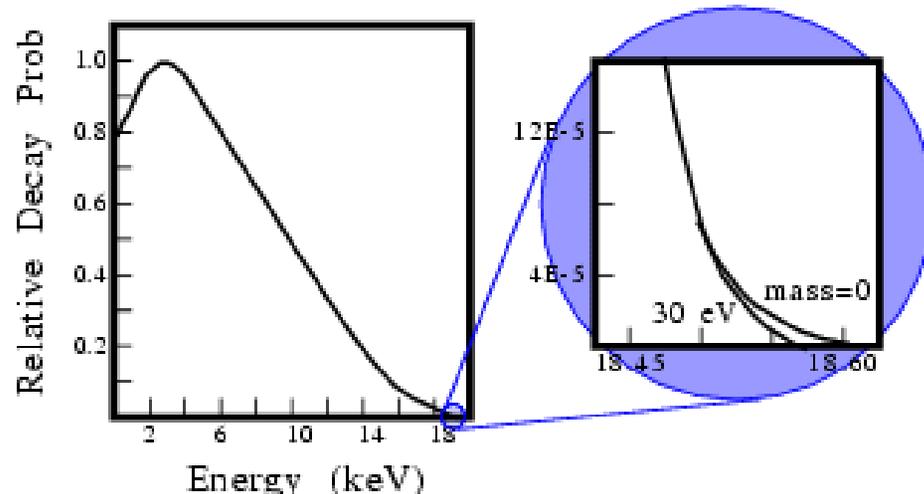
- Direct mass measurements are consistent with zero
- But we observe neutrino oscillations
- And flavor transitions in the Sun

From Direct Limits:



*If neutrinos have Dirac masses,
it is small relative to the charged partners...
why?*

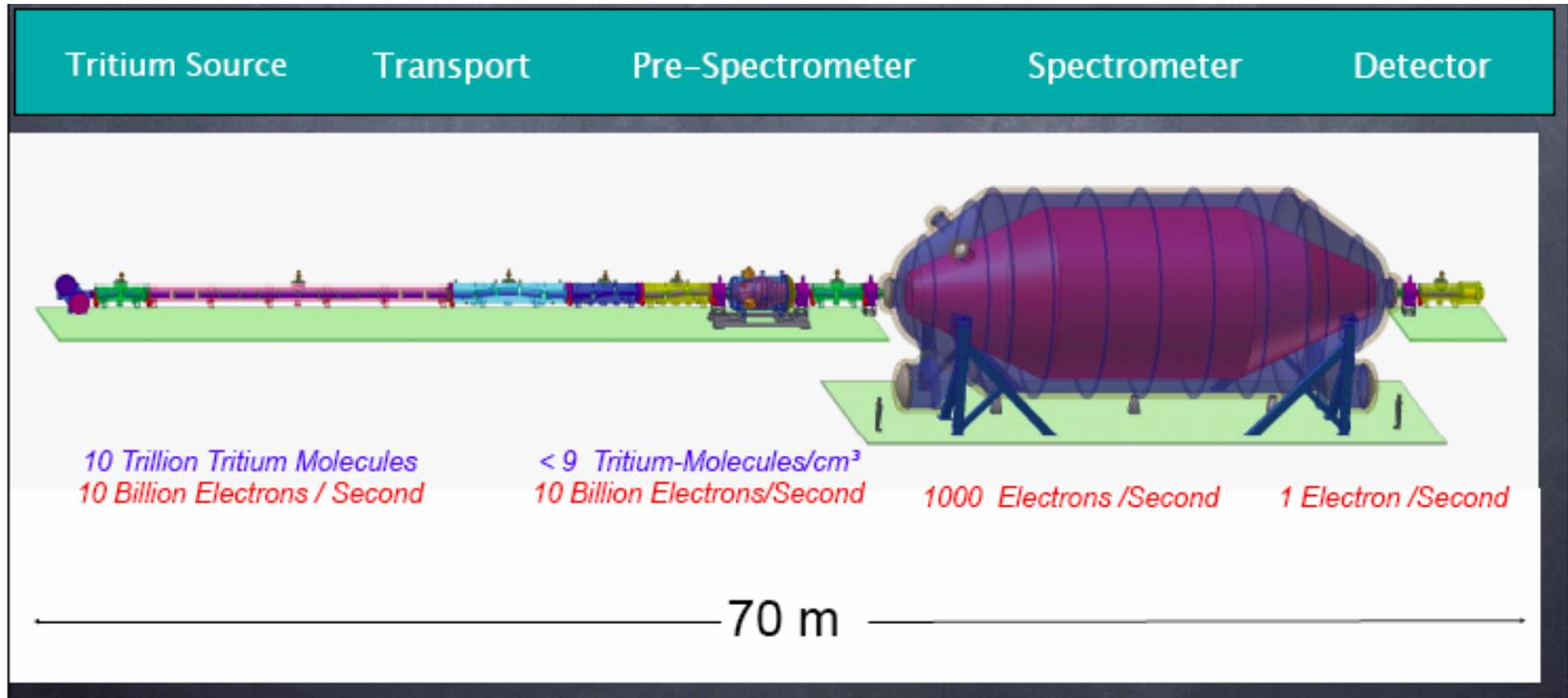
ν_e mass from Tritium



- Measurements of m^2 are systematically negative:

Experiment	measured mass squared (eV^2)	limit (eV), 95% C.L.	Year
Mainz	$-0.6 \pm 2.2 \pm 2.1$	2.2	2004
Mainz	$-0.1 \pm 3.8 \pm 1.8$	2.8	1998
Troitsk	$-2.1 \pm 3.7 \pm 2.3$	2.5	1998
Livermore	$-130 \pm 20 \pm 15$	7.0	1995
China	$-31 \pm 75 \pm 48$	12.4	1995
Zrich	$-24 \pm 48 \pm 61$	11.7	1992
Tokyo INS	$-65 \pm 85 \pm 65$	13.1	1991
Los Alamos	$-147 \pm 68 \pm 41$	9.3	1991

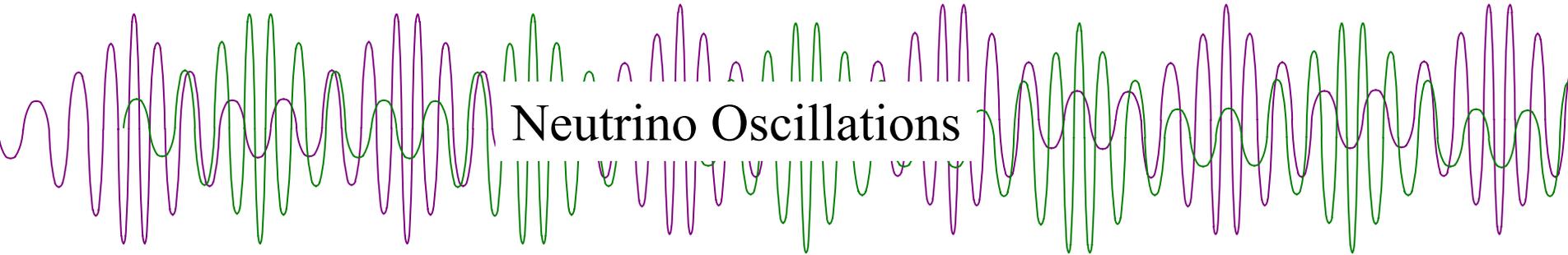
The future of this type of experiment is Katrin:



Probes to $m_\nu < 0.25$ eV @90% CL

- improved statistics (stronger source, longer running)
- improved resolution (electrostatic spectrometer with $\Delta E = 1$ eV)
- background reduction (materials choices, veto)

But in the meantime...



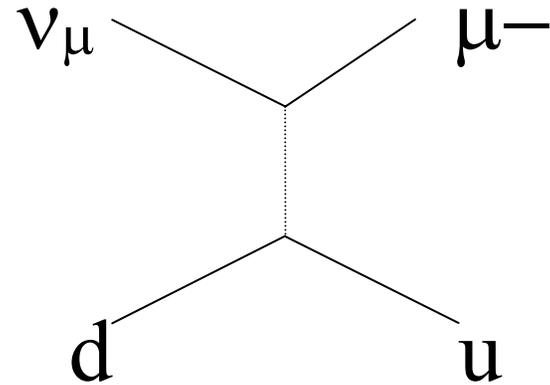
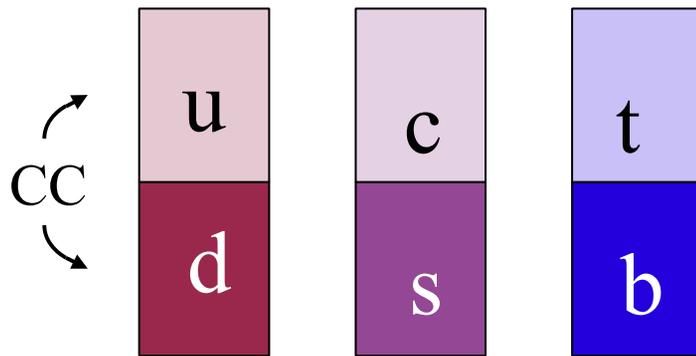
Which may result if we postulate:

- Neutrinos have (different) mass

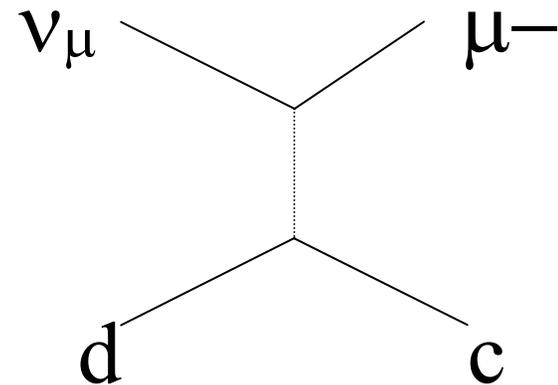
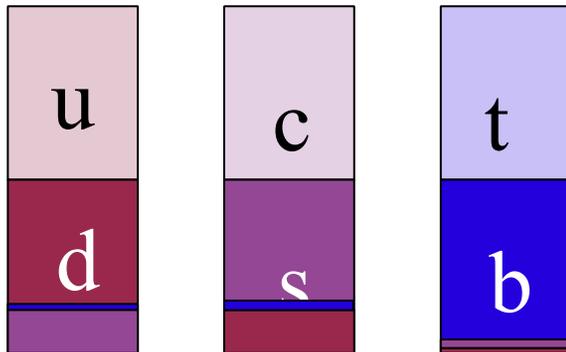
$$\Rightarrow \Delta m^2 = m_1^2 - m_2^2$$

- The *Weak Eigenstates* are a mixture of *Mass Eigenstates* in analogy with the quark sector...

Quarks in theory....



Quarks in practice....



Assume mixing can also happen in the neutrino sector

Take the mixing matrix to be:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

At production (t=0): $|\nu_\mu(0)\rangle = -\sin \theta |\nu_1\rangle + \cos \theta |\nu_2\rangle$

At a later time, with $\hbar = c = 1$:

$$\begin{aligned} |\nu_\mu(t)\rangle &= -\sin \theta e^{-iE_1 t} |\nu_1\rangle + \cos \theta e^{-iE_2 t} |\nu_2\rangle \\ &= (\cos^2 \theta e^{-iE_1 t} + \sin^2 \theta e^{-iE_2 t}) |\nu_\mu\rangle + \\ &\quad \sin \theta \cos \theta (e^{-iE_2 t} - e^{-iE_1 t}) |\nu_e\rangle \end{aligned}$$

And the probability is:

$$\begin{aligned} P_{osc} &= |\langle \nu_e | \nu_\mu(t) \rangle|^2 \\ &= \frac{1}{2} \sin^2 2\theta (1 - \cos(E_2 - E_1) t) \end{aligned}$$

Use $E_i = \sqrt{p^2 + m_i^2} \approx p + m_i^2/2p$ and $t/p = (tc)/(pc) = L/E$; then convert units by adding $1/\hbar c$:

$$\begin{aligned} P_{osc} &= \frac{1}{2} \sin^2 2\theta \left(1 - \cos \left(\frac{(m_2^2 - m_1^2)L}{4E} \right) \right) \\ &= \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E) \end{aligned}$$

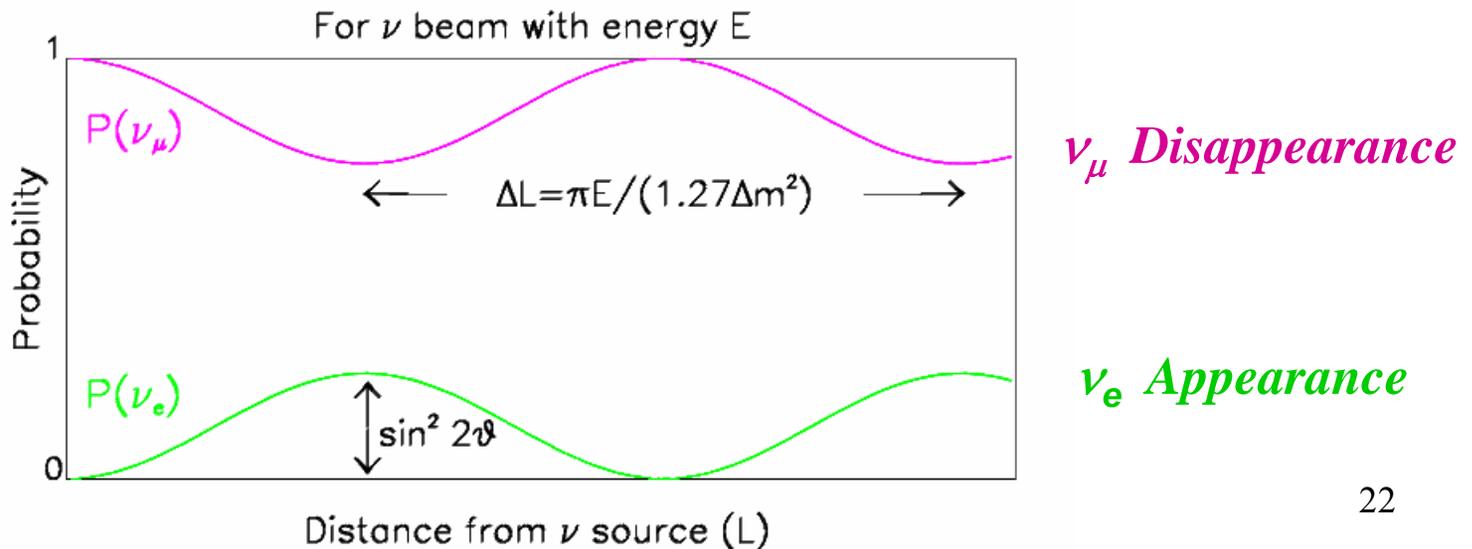
$$P_{Osc} = \sin^2 2\theta \sin^2 \left(1.27 \Delta m^2 L / E \right)$$

...Depends Upon Two Experimental Parameters:

- L – The distance from the ν source to detector (km)
- E – The energy of the neutrinos (GeV)

...And Two Fundamental Parameters:

- $\Delta m^2 = m_1^2 - m_2^2$ (eV^2)
- $\sin^2 2\theta$



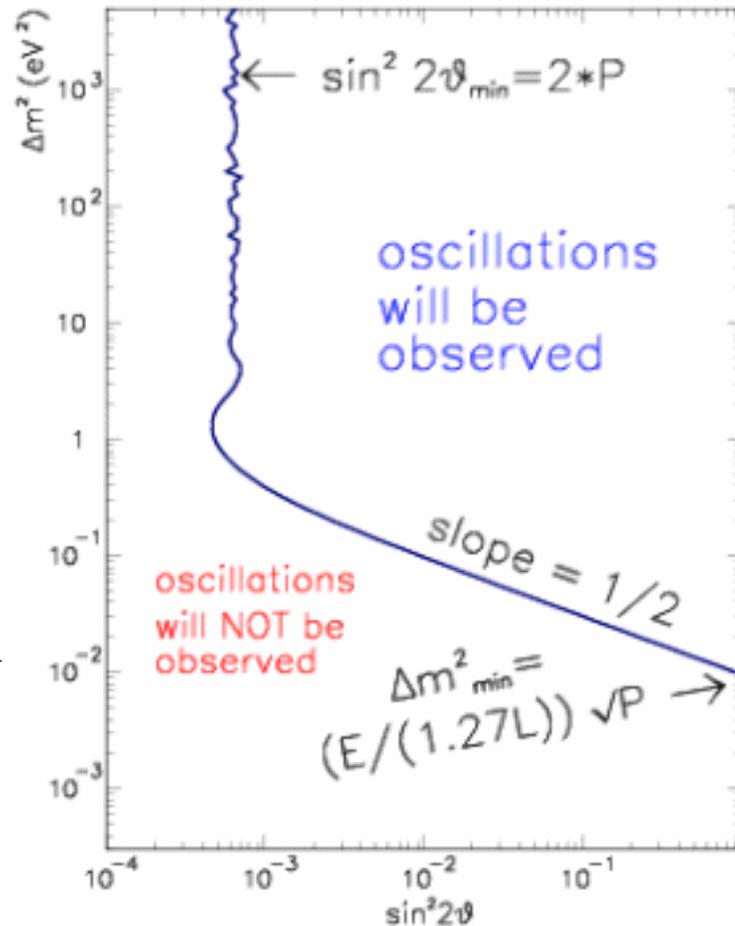
$$P_{Osc} = \sin^2 2\theta \sin^2 \left(1.27 \Delta m^2 L / E \right)$$

at high Δm^2 ,
 $\langle \sin^2(1.27 \Delta m^2 L / E) \rangle = 1/2$

1 measurement
 and
 2 parameters...

Allowed regions will
 look like "blobs"

Exclusions by experiments
 with no signal are indicated
 by lines...



At low Δm^2
 use the
 small angle
 approx.

$$P_{Osc} = \sin^2 2\theta \sin^2 \left(1.27 \Delta m^2 L / E \right)$$

How to design your experiment...

if Δm^2 is small, you need large L/E

if Δm^2 is large, you want relatively small L/E to have sensitivity to Δm^2

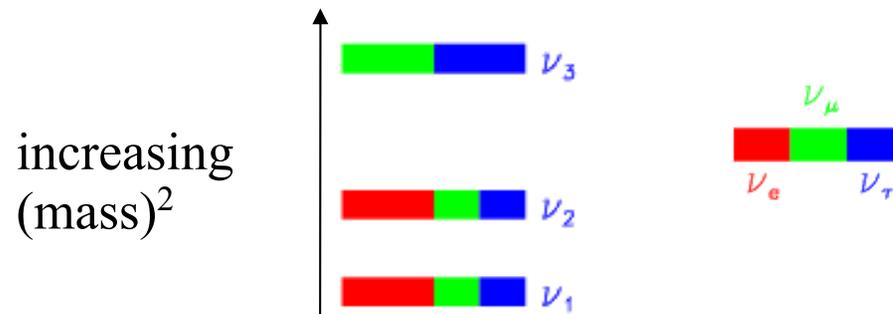
A value of $(\Delta m^2 L/E) \sim 1$
is preferable.

if θ is small, P is small & life is very hard

This is a simplistic view....

There are 3 neutrinos, so...

there are 3 mass states and 3 weak states
and three mixing angles θ_{12} , θ_{13} and θ_{23}

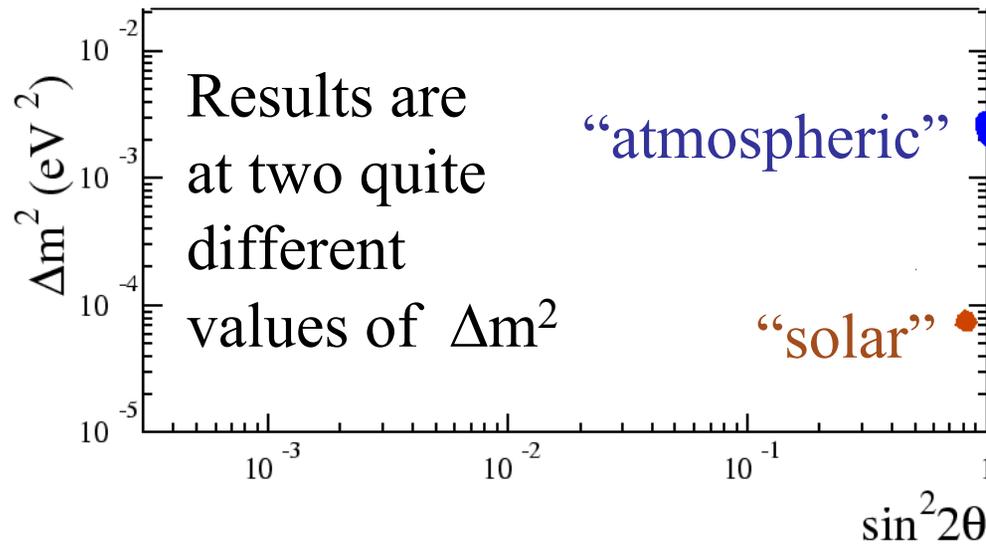


$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

Evidence for neutrino oscillations is now very strong...

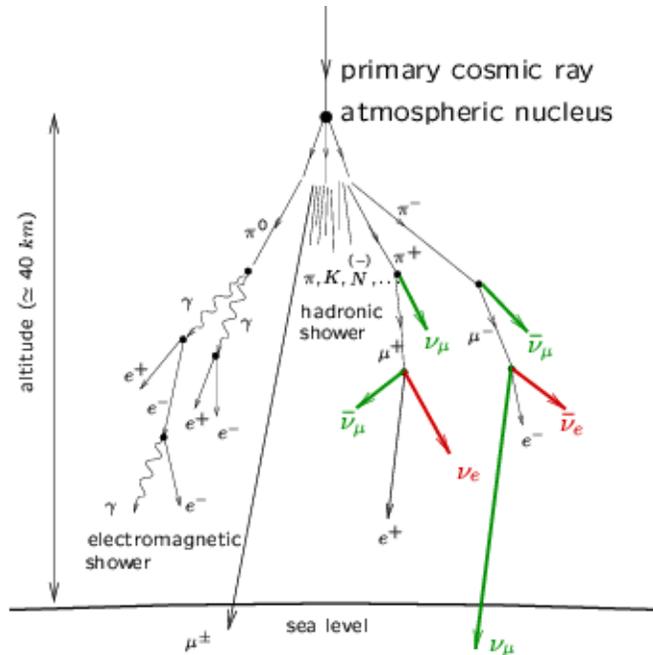
High significance experiments (many $>5\sigma$)

Experiments have differing systematics



“Atmospheric” $>5\sigma$ Experiment: Super K

Also:
IMB,
Kamioka
MACRO

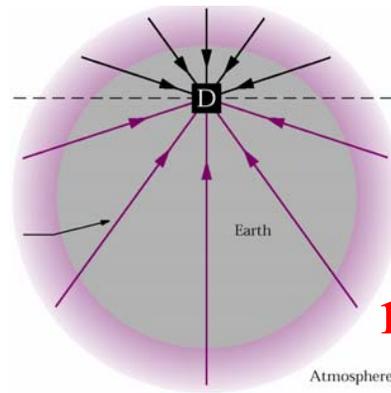


Below 1 GeV, simple counting gives 1:2 $\nu_e:\nu_\mu$
Above 1 GeV, ratio gradually goes to 1:1 because μ 's do not have opportunity to decay

Average path length d of a 1 GeV muon:

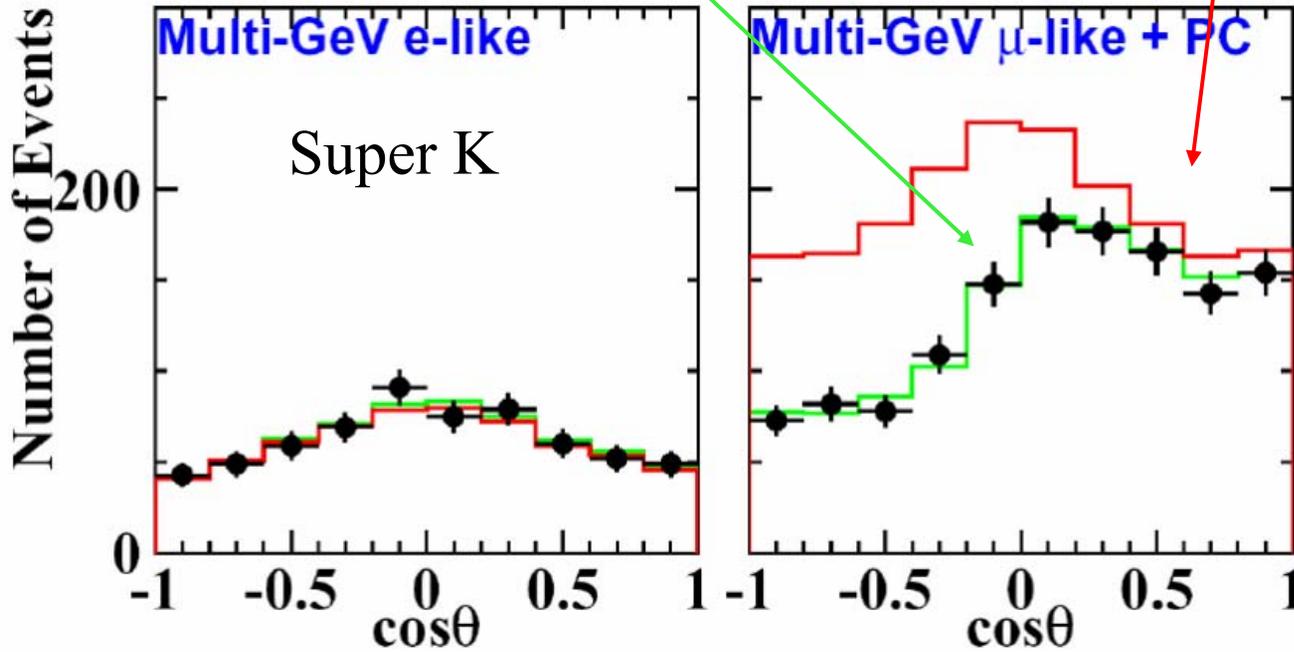
$$\begin{cases} \gamma\beta \simeq \gamma = E/m \sim 10 \\ c\tau \sim 600 \text{ m} \end{cases} \Rightarrow d = \gamma\beta c\tau \sim 6 \text{ km}$$

length dependence in
 ν_μ oscillation
 probability
 consistent with
 ν_μ disappearance

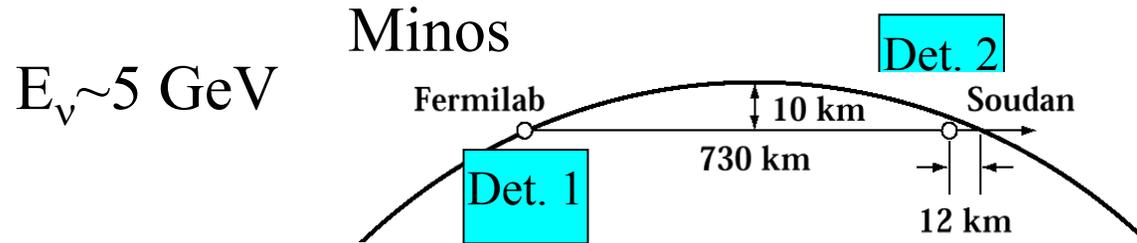


no oscillations

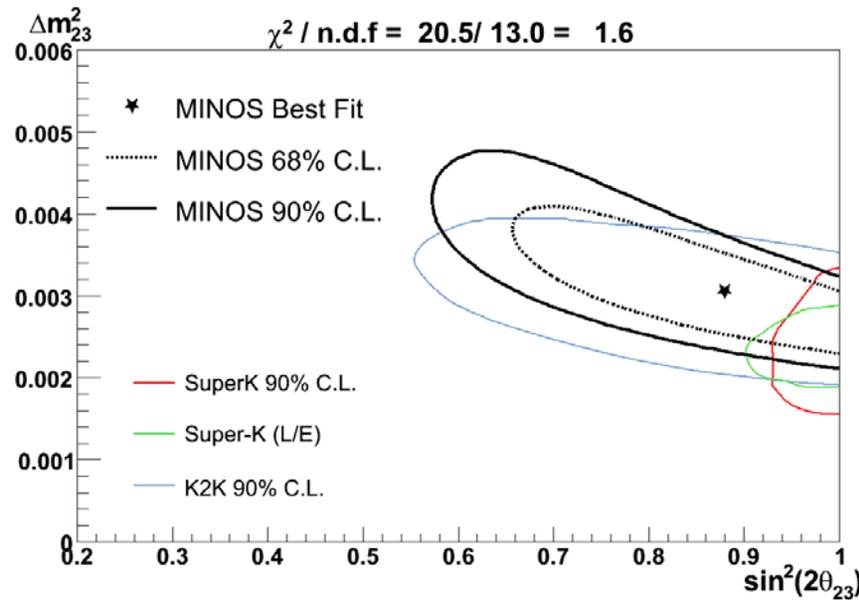
$\nu_\mu \rightarrow \nu_\tau$ oscillations

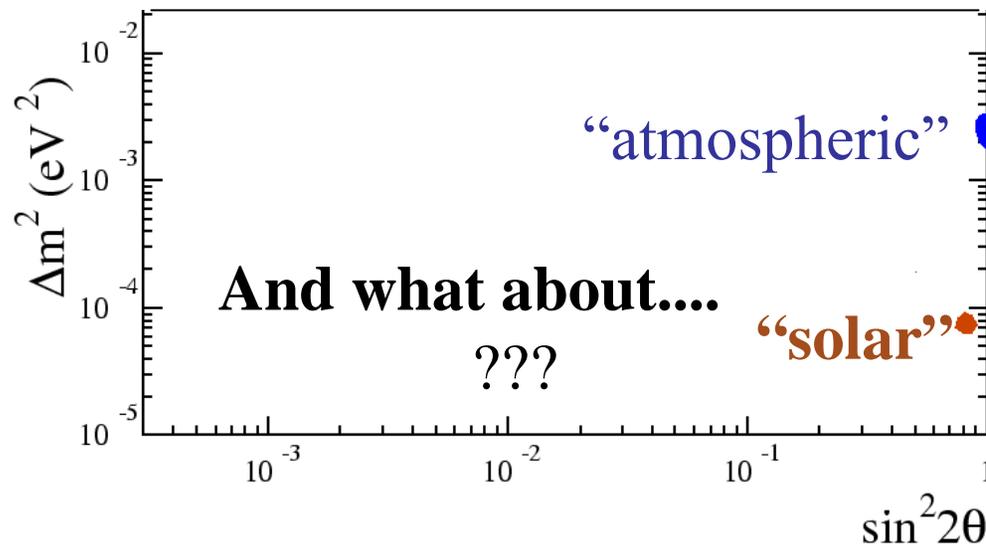


K2K and Minos are Long-baseline beam experiments running at L/E appropriate for $\Delta m^2 \sim 10^{-3}$



Minos is just bringing out results now!





If what was happening with solar neutrinos was pure neutrino oscillations...

$$L \sim 1.5 \times 10^{11} \text{ m}$$

$$E \sim 5 \text{ MeV}$$

To be sensitive to oscillations $(\Delta m^2 L/E) \sim 1$

This would imply $\Delta m^2 \sim 3 \times 10^{-10} \text{ eV}^2$

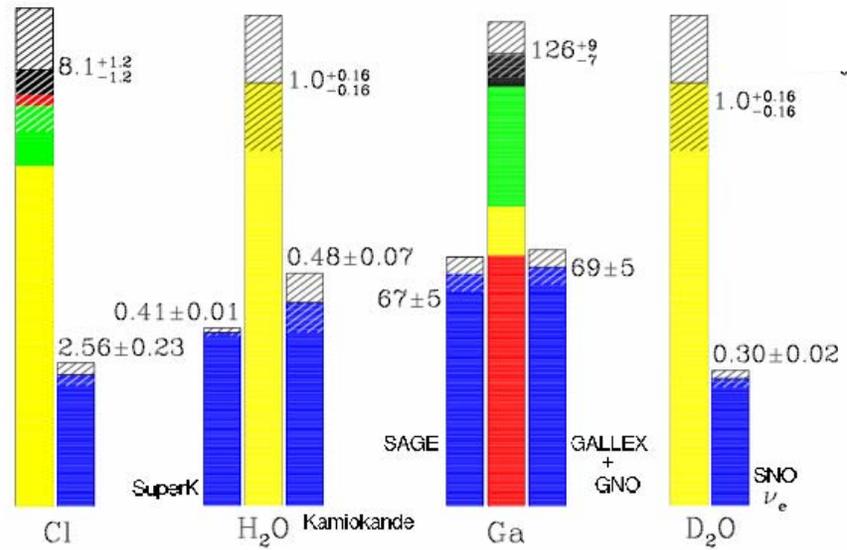
But solar experiments **do** see flavor changing effects!

Suppression in the solar neutrino rate is now well established...

But it isn't pure oscillations!

These experiments are all sensitive to ν_e CC interactions

Total Rates: Standard Model vs. Experiment
Bahcall-Serenelli 2005 [BS05(OP)]



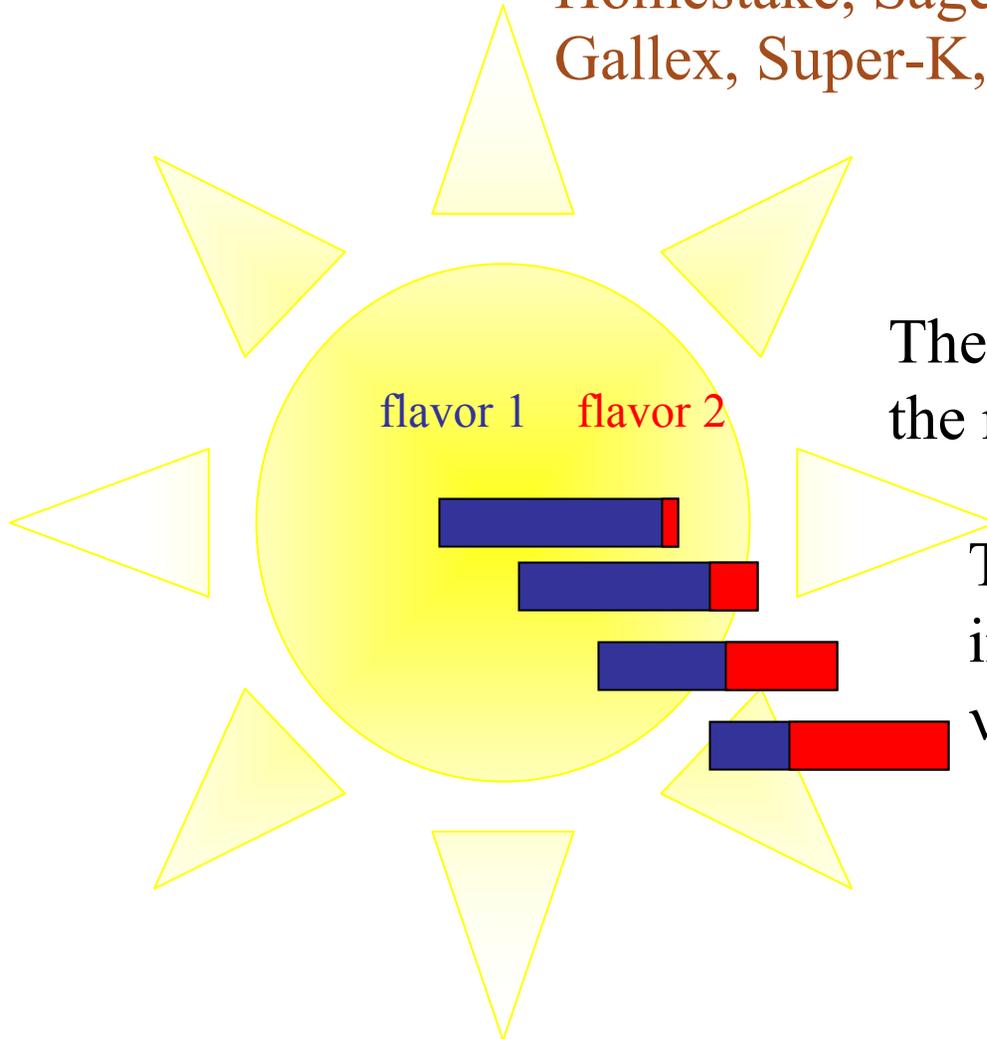
Theory	■ ${}^7\text{Be}$	■ p-p, pep	Experiments	■
	■ ${}^8\text{B}$	■ CNO	Uncertainties	

solar processes

Something extra is happening to neutrinos in the sun!
Matter effects....

Homestake, Sage,
Gallex, Super-K, SNO

“The LMA MSW
solution”



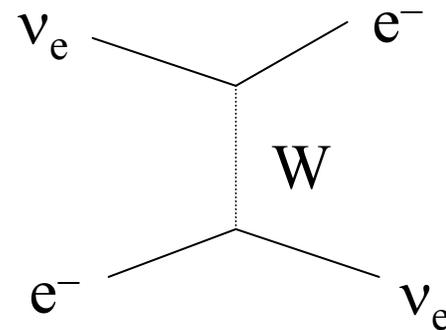
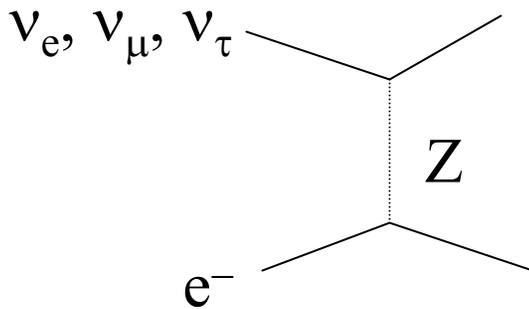
There is flavor evolution as
the neutrinos traverse the sun.

The result is disappearance
in detectors sensitive to only
 ν_e flavors...

Matter effects will occur

whenever one type of neutrino can interact in ways the other “types in the mix” cannot...

In the case of ν_e 's in the plasma of the sun, this is because the CC interaction for μ and τ are kinematically suppressed...



How can we be sure the Solar suppression is due to neutrinos?
Maybe something is wrong with the solar model...

Sudbury Neutrino Observatory (SNO) can measure the solar flux
regardless of the neutrino species:

$$\nu_{\text{sol}} d \rightarrow \nu n p \Rightarrow \phi_{\nu_e} + \phi_{\nu_\mu} + \phi_{\nu_\tau}$$

$$\text{SNO: } \phi_{\nu_e} + \phi_{\nu_\mu} + \phi_{\nu_\tau} = (4.94 \pm 0.21 \pm 0.36) \times 10^6/\text{cm}^2\text{sec}$$

$$\text{Theory: } \phi_{\text{total}} = (5.69 \pm 0.91) \times 10^6/\text{cm}^2\text{sec}$$

Bahcall, Basu, Serenelli

You see disappearance in experiments sensitive to CC
But not in experiments sensitive to NC!

Ok, what's happening in the sun is not “pure oscillations,”
 but if you go to the L/E on earth,
 corresponding to the solar parameters
 you ought to see oscillations...

$$\Delta m^2 \sim 10^{-5} \text{ eV}^2, \text{ large mixing}$$

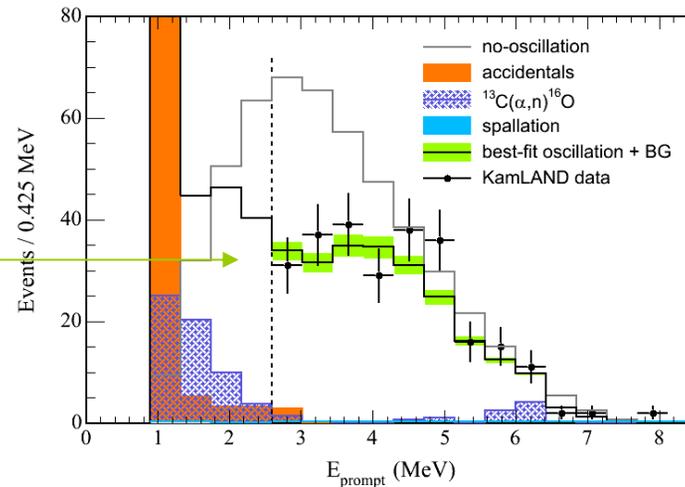
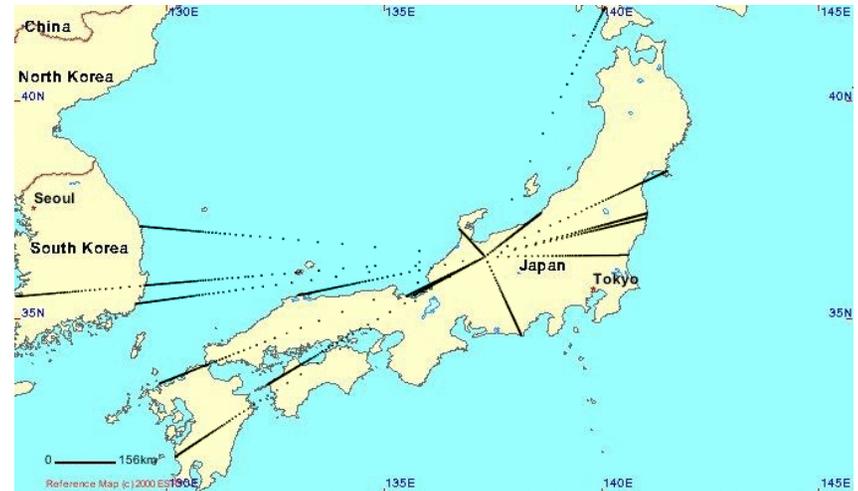
You can see this if you have....

$$L \sim 100 \text{ km}$$

$$E \sim 0.001 \text{ GeV}$$

... The Kamland experiment

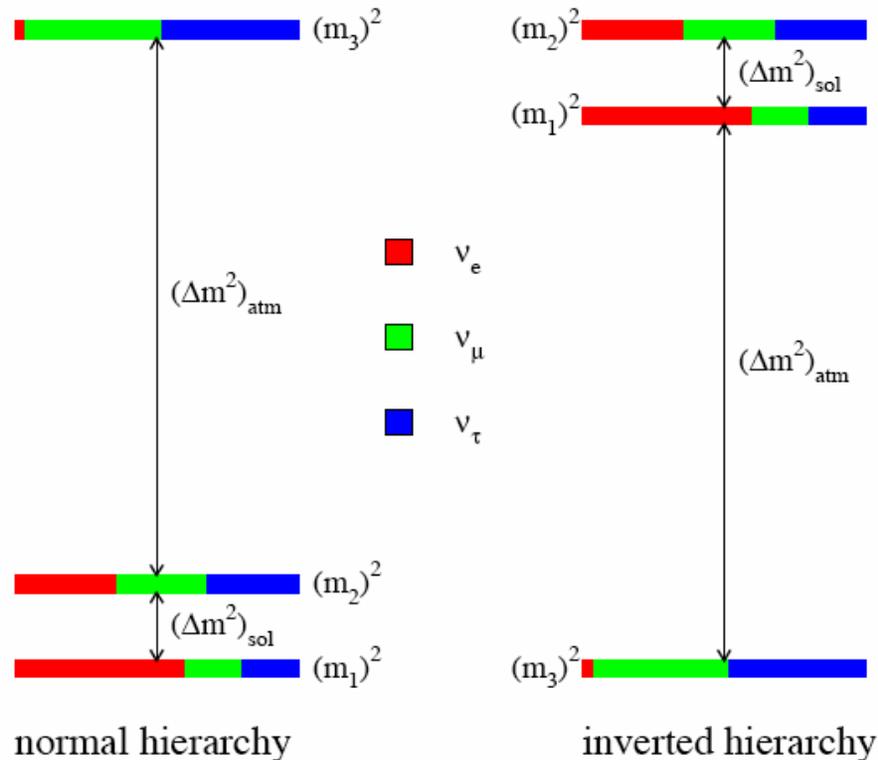
A clear signal at the
 solar parameters!



(There are other oscillation results,
but let's stick at those which are 5σ for now...)

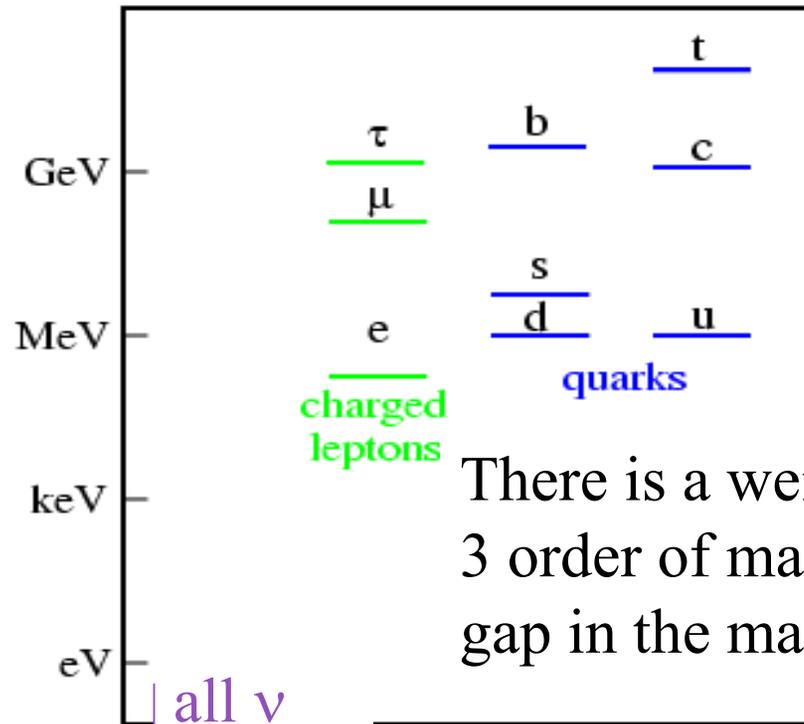
What can we conclude?

Two possible successful 3 neutrino mixing models:



The combination of the tritium and the oscillation experiments constrains all ν masses to be small

This plot should show $\nu_1, \nu_2,$ and ν_3 not $\nu_e, \nu_\mu,$ and ν_τ



There is a weird 3 order of magnitude gap in the masses

all ν masses are down here

These results confounded all theoretical expectations!

In the mid-1990's:

- Neutrinos don't have mass... **Wrong**
- But if they did, then
natural scale for $\Delta m^2 \sim 10 - 100 \text{ eV}^2$
since needed to explain dark matter **Wrong**
- Oscillation mixing angles must be small
like the quark mixing angles **Wrong**
- Solar neutrino oscillations must be
small mixing angle MSW solution
because it is "elegant" **Wrong**
- Atmospheric neutrino anomaly must be
other physics or experimental problem
because it needs such a large mixing angle **Wrong**

Let's face it...
Nature isn't elegant...

Let's face it...
Nature isn't elegant...

... or maybe we just don't have the
right taste!

Neutrinos and the “New Paradigm”:

The last of the mid-90's ideals

The defining assumption: Neutrinos are Majorana Particles

ν and $\bar{\nu}$ are the two helicities of the same particle...

Why?

This would explain 100% parity violation OK!

“if it can happen it will happen” ummmm...

This makes neutrinos “even more different”
then the other particles in the Standard Model

The result is new “mass-like” terms in the Lagrangian

▷ Dirac Mass terms like $m(\bar{\psi}_L\psi_R + \dots)$

▷ and things which look like:

$$(M_L/2)(\bar{\psi}_L^c\psi_L) + (M_R/2)(\bar{\psi}_R^c\psi_R) + \dots$$

“Majorana mass terms”

To improve notation, use:

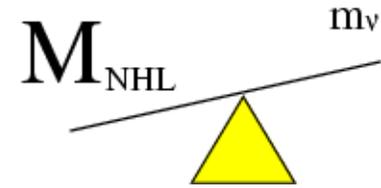
$$\phi = (\psi_L^c + \psi_L)/\sqrt{2} \text{ and } \Phi = (\psi_R^c + \psi_R)/\sqrt{2}$$

Which allows you to write the mass terms as

$$(\bar{\phi} \ \bar{\Phi}) \begin{pmatrix} M_L & m \\ m & M_R \end{pmatrix} \begin{pmatrix} \phi \\ \Phi \end{pmatrix}$$

Diagonalize this to get the physical mass states...

Now you can connect
to see-saw models,
that motivate mass matrices like...



$$\begin{pmatrix} 0 & m_\nu \\ m_\nu & M \end{pmatrix}$$

- $\mu_{light} \approx m_\nu^2/M$
- $\mu_{heavy} \approx M$

Three happy theoretical consequences:

- 1) You get a neutrino which is apparently very light, even though $m_\nu \sim$ other lepton masses...
- 2) You get a natural connection to GUT models
- 3) There is a mechanism for leptogenesis

Experiments addressing this model:

1. Neutrinoless double beta decay

The “clinging” signature for Majorana neutrinos

2. Precision measurements of the mixing angles

“Selects” classes of models for the higher theory

3. Is there CP Violation?

“A smoking gun” for Leptogenesis

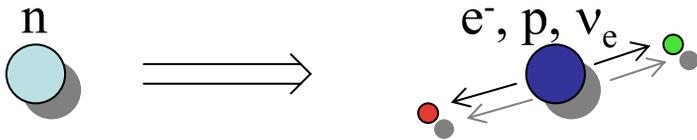
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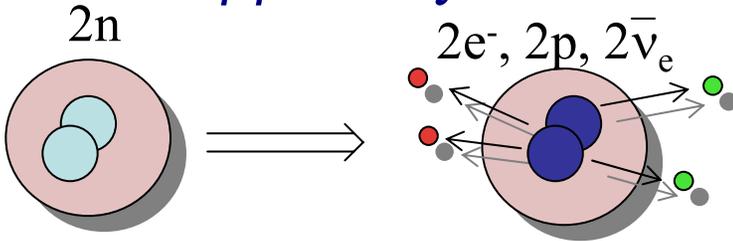
Double Beta Decay, 101

Single β Decay

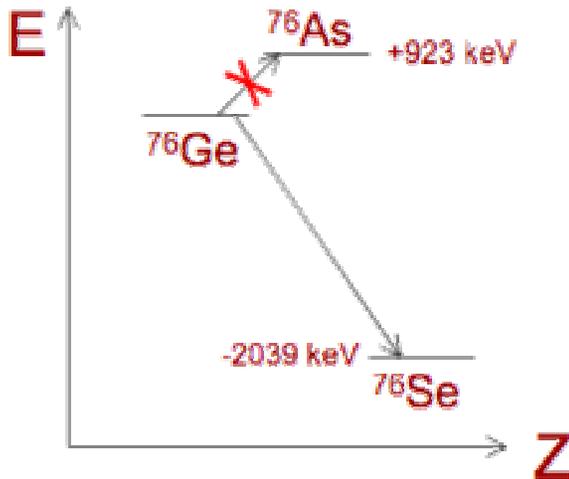


Half-life: About 10 minutes

$2\nu\beta\beta$ Decay



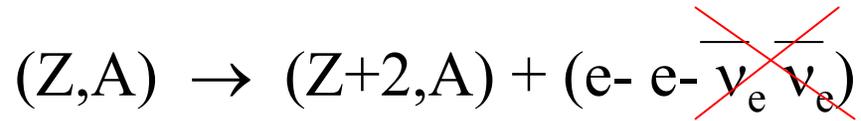
Can occur if single β decay is energetically forbidden



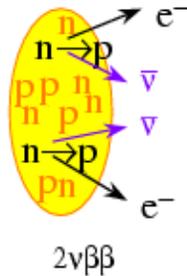
Half-life: 10^{18-24} years

⁴⁸Ca, ⁷⁶Ge, ⁸²Se, ⁹⁶Zr,
¹⁰⁰Mo, ¹¹⁶Cd, ¹²⁸Te, ¹³⁰Te,
¹⁵⁰Nd, ²³⁸U, ²⁴²Pu

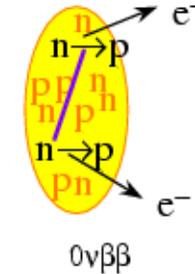
Neutrinoless Double Beta Decay



Nuclei that do this...

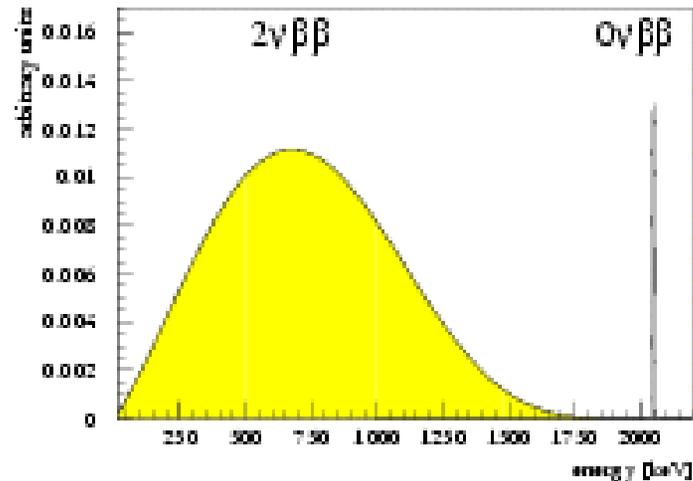


Can sometimes also do this



IF neutrinos are their own antiparticles

The tell-tale signature is in the decay spectrum:



The lifetime for this process is given by:

$$\frac{1}{T_{1/2}^{0\nu}} = G^{0\nu}(E_o, Z) |M^{0\nu}|^2 \left| \langle m_{\nu, \beta\beta} \rangle \right|^2$$

The phase space factor
($3 \times 10^{-26}/\text{y}$ in Ge)

$$|M^{0\nu}|^2 = \left| M_{GT}^{0\nu} - \left(\frac{g_V}{g_A} \right)^2 M_F^{0\nu} \right|^2$$

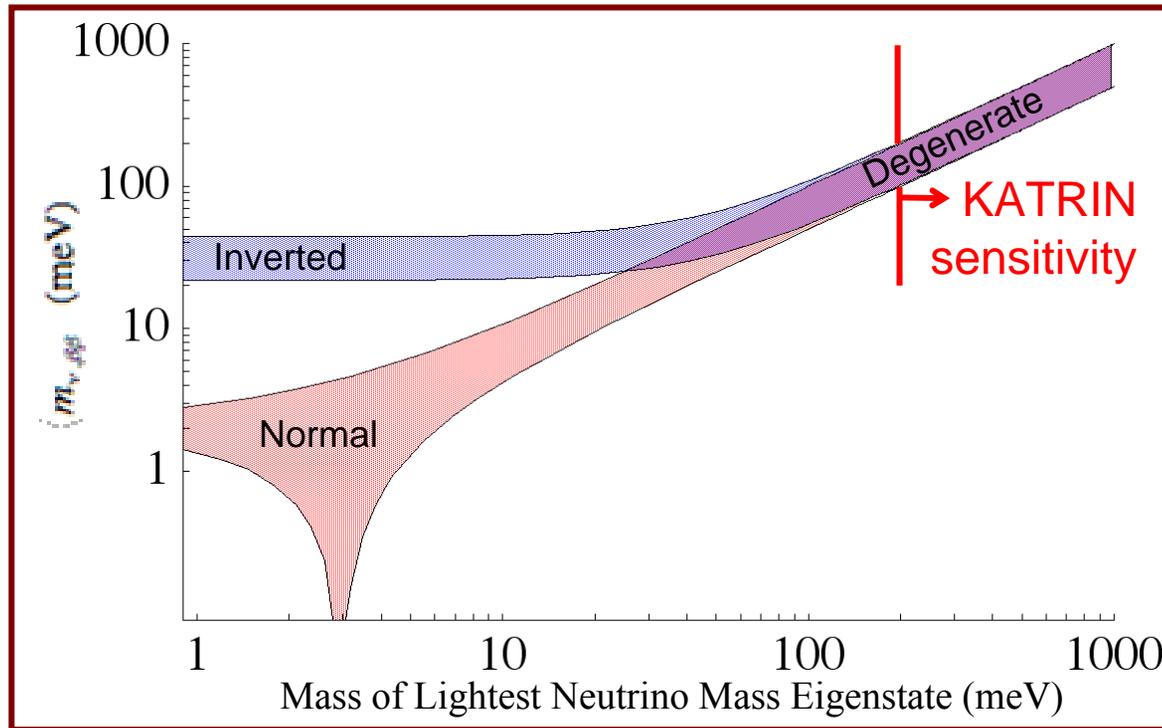
The nuclear matrix element,
can be calculated at some level,
can be measured from
excited states of $2\nu\beta\beta$

$$\left| \langle m_{\nu, \beta\beta} \rangle \right| = \left| \sum_i \lambda_i^{CP} m_i |U_{ei}^L|^2 \right|$$

Weights the mass w/ the mixing
(what's the contribution from
the ν_e ?)

$$\left| \langle m_{\nu, \beta\beta} \rangle \right| = \left| \sum_i \lambda_i^{CP} m_i |U_{ei}^L|^2 \right|$$

This is a big deal for $0\nu\beta\beta$ experiments...



Bornschein, *Nucl. Phys. A* **752** (2005) 14c-23c.

Many experiments have not seen $0\nu\beta\beta$:

Most recently:

CUORICINO: $^{130}\text{Te} \geq 1.8 \times 10^{24}$ yr, *PRL* **95** 142501 (2005).

NEMO-3: $^{100}\text{Mo} \geq 3.5 \times 10^{23}$ yr, $^{82}\text{Se} \geq 1.9 \times 10^{23}$ yr, hep-ex/0412012.

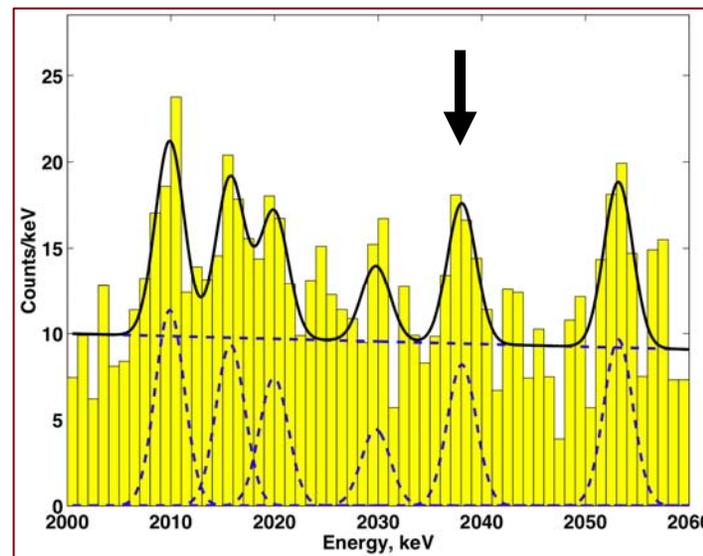
One experiment claims a signal:

Klapdor-Kleingrothaus *et al.*,
hep-ph/0403018

Germanium

Half-life = 1.19×10^{25} years,

4.2 σ result



(Germanium is the only $0\nu\beta\beta$ “source” that is its own detector!)

Janet's opinions:

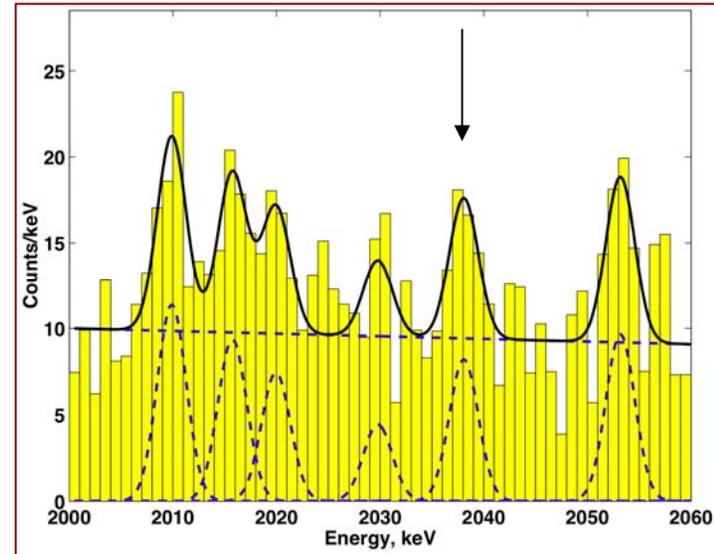
You know exactly where to look.
This is a blessing and a curse.

It is easy to make cuts that bias
the significance of the signal

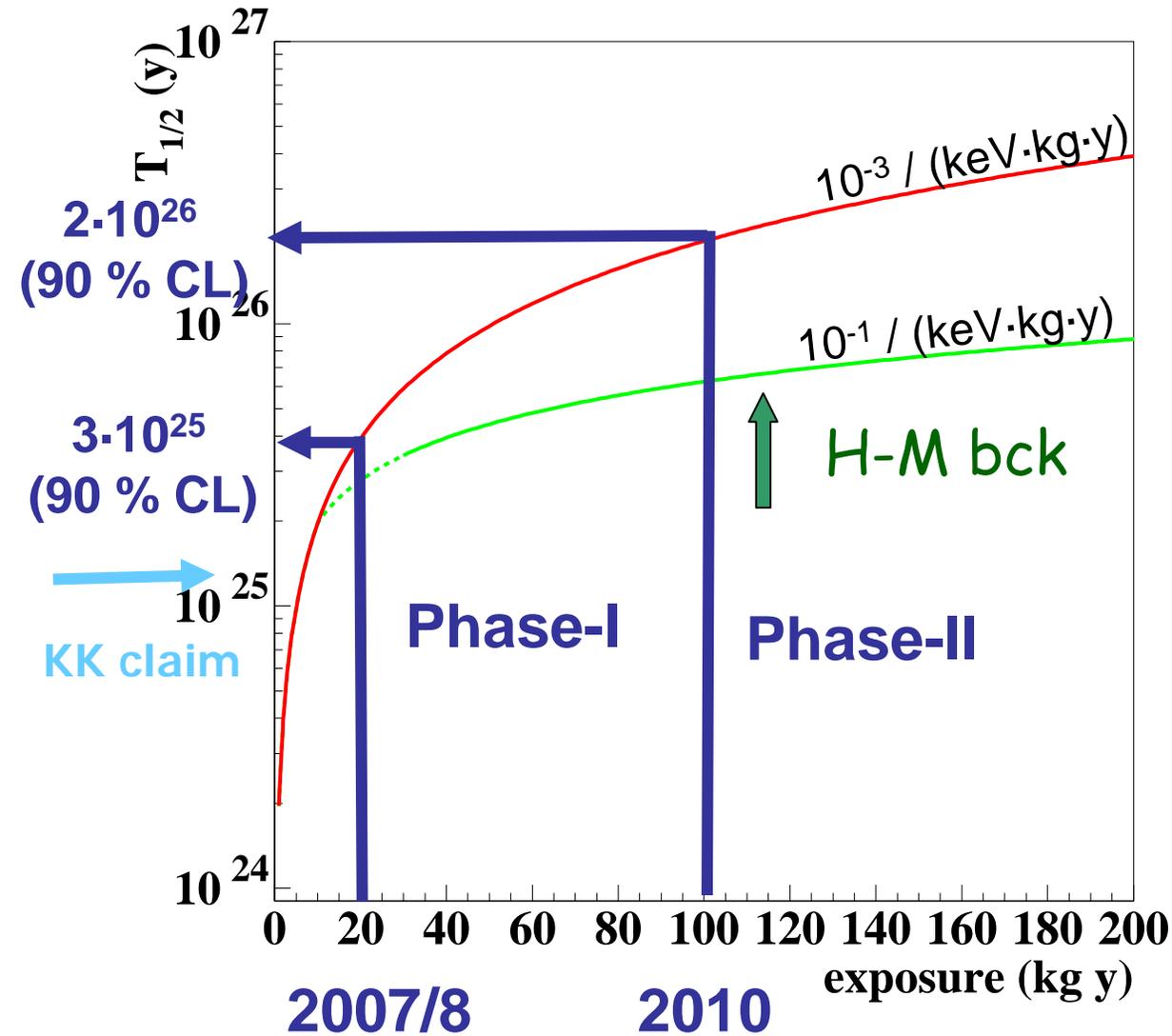
This is an experimental question...
And there are experiments planned to answer it.

GERDA and Majorana

Both use Germanium, like KK's experiment,
but with segmentation and other improvements

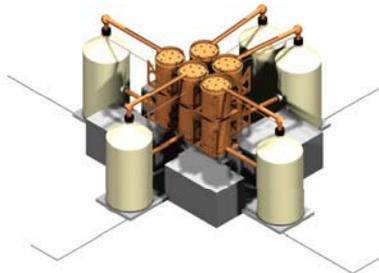


GERDA



- Phase I:** existing detectors
- Phase II:** new detectors
- Phase III:** worldwide new collaboration **O(ton) experiment** $\rightarrow 10^{27}$ y.
Cooperation with Majorana

$0\nu\beta\beta$ is a big industry for the future!

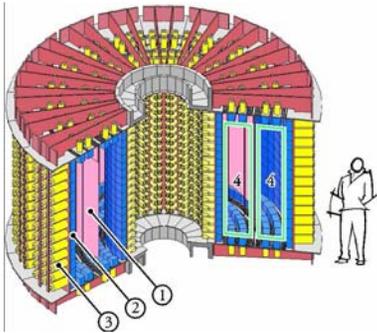


GERDA: Bare Ge crystals in LN

Majorana: Ge detector in a cryostat

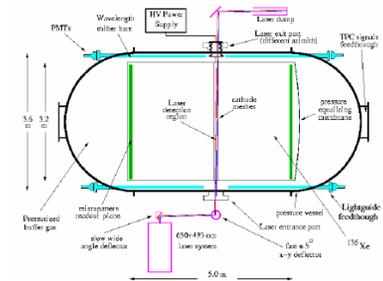
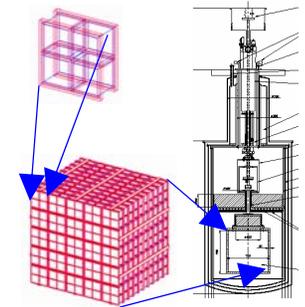
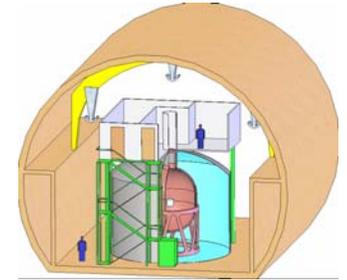
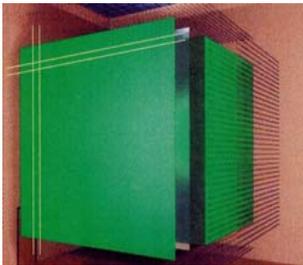
CUORE: TeO₂ crystal bolometer

SuperNemo: Many types of foils, with tracking and scintillator



EXO: Liquid Xenon with Ba tagging

Moon: Mo foils sandwiched between scintillator



Experiments addressing this model:

2. Precision measurements of the mixing angles

“Selects” classes of models for the higher theory

The MNS Matrix for neutrinos

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1}^{\text{BIG}} & U_{e2}^{\text{BIG}} & U_{e3}^{\text{small}} \\ U_{\mu 1}^{\text{BIG}} & U_{\mu 2}^{\text{BIG}} & U_{\mu 3}^{\text{BIG}} \\ U_{\tau 1}^{\text{BIG}} & U_{\tau 2}^{\text{BIG}} & U_{\tau 3}^{\text{BIG}} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Doesn't look much like the CKM matrix for quarks...

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} U_{ud} & U_{us} & U_{ub} \\ U_{cd} & U_{cs} & U_{cb} \\ U_{td} & U_{ts} & U_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} = \begin{pmatrix} 0.97 & 0.22 & 0.003 \\ -0.22 & 0.97 & 0.04 \\ 0.01 & -0.04 & 0.999 \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

At present-day energies

But *if* the values are related to the masses,
and the masses evolve with energy scale...

You can get quark-lepton “complementarity”

These theories generally want $\sin^2 2\theta_{13} \gtrsim 0.01$
and $\sin^2 2\theta_{23} < 1$

$$\begin{aligned}
 U &= \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \\
 &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}
 \end{aligned}$$

From Atmospheric and Long Baseline Disappearance Measurements

From Reactor Disappearance Measurements

From Long Baseline Appearance Measurements

From Solar Neutrino Measurements

Overview of expected values of $\sin^2 2\theta_{13}$

Model(s)	Refs.	$\sin^2 2\theta_{13}$
Minimal SO(10)	[22]	0.13
Orbifold SO(10)	[23]	0.04
SO(10) + Flavor symmetry	[24]	$1.2 \cdot 10^{-8}$
	[25]	$7.8 \cdot 10^{-4}$
	[26–28]	0.01 .. 0.04
	[29–31]	0.09 .. 0.18
SO(10) + Texture	[32]	$4 \cdot 10^{-4}$.. 0.01
	[33]	0.04
	[34]	0.09
Flavor symmetries	[35–37]	0
	[38–40]	$\lesssim 0.004$
	[41–43]	10^{-4} .. 0.02
	[40, 44–47]	0.04 .. 0.15
Textures	[48]	$4 \cdot 10^{-4}$.. 0.01
	[49–52]	0.03 .. 0.15
3×2 see-saw	[53]	0.04
	[54] (n.h.)	0.02
	(i.h.)	$> 1.6 \cdot 10^{-4}$
Anarchy	[55]	> 0.04
Renormalization group enhancement	[56]	0.03 .. 0.04
M-Theory model	[57]	10^{-4}

Blue:
Wants a large
value

Red:
Tolerates
or favors
small values

In this section, I want to talk about

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

THIS

From Atmospheric and Long Baseline Disappearance Measurements

From Reactor Disappearance Measurements

From Long Baseline Appearance Measurements

From Solar Neutrino Measurements

In this section, I want to talk about

And then THIS

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

From Atmospheric and Long Baseline Disappearance Measurements

From Reactor Disappearance Measurements

From Long Baseline Appearance Measurements

From Solar Neutrino Measurements

One mixing angle is not yet observed: θ_{13}

This governs the transition between ν_e and other species
at the atmospheric Δm^2

A very clean measurement comes from ν_e flavor disappearance
and a very clean $\bar{\nu}_e$ beam comes from a reactor

$$P_{\text{reactor}} \simeq \sin^2 2\theta_{13} \sin^2 \Delta_{\text{atm}} + \alpha^2 \Delta_{\text{atm}}^2 \cos^4 \theta_{13} \sin^2 2\theta_{12},$$

$$\alpha \equiv \Delta m_{21}^2 / \Delta m_{23}^2$$

$$\Delta \equiv \Delta m_{31}^2 L / (4E_\nu).$$

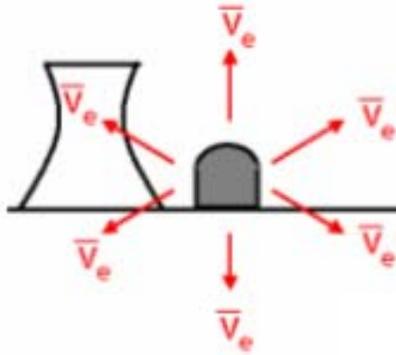
One mixing angle is not yet observed: θ_{13}

This governs the transition between ν_e and other species
at the atmospheric Δm^2

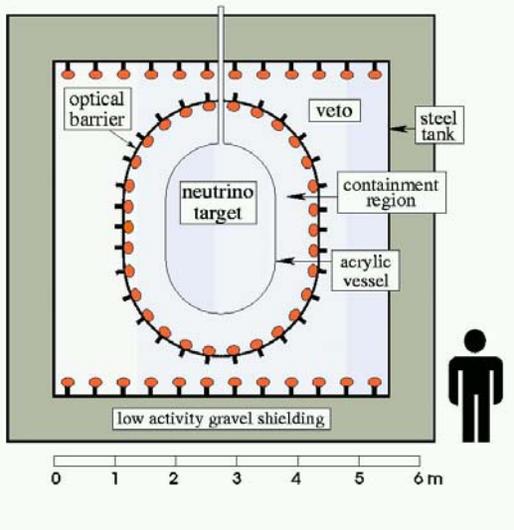
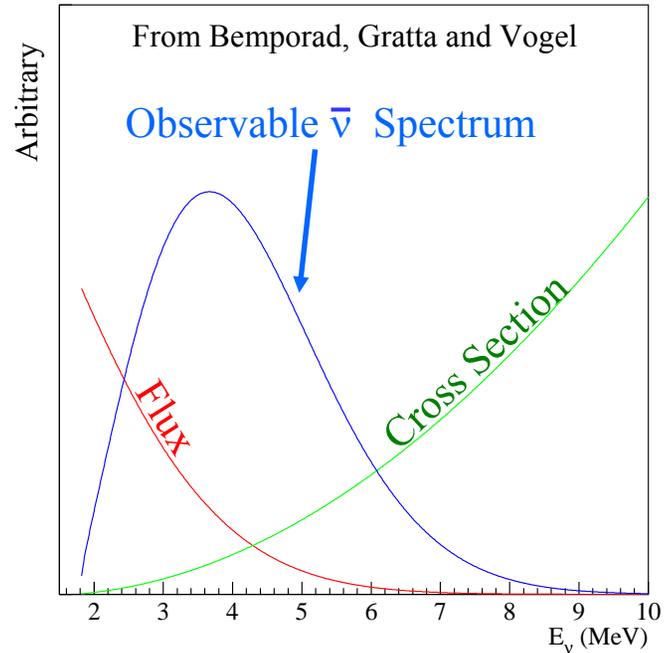
There are 2 types of experiments used for these studies:

1. Reactor-based experiments
2. Long Baseline Experiments

Reactors: Disappearance ($\bar{\nu}_e \rightarrow \bar{\nu}_e$) at $\Delta m^2 \approx 2.5 \times 10^{-3} \text{ eV}^2$



for $\Delta m^2 L/E \sim 1$
you need $L \sim 1000 \text{ m}$

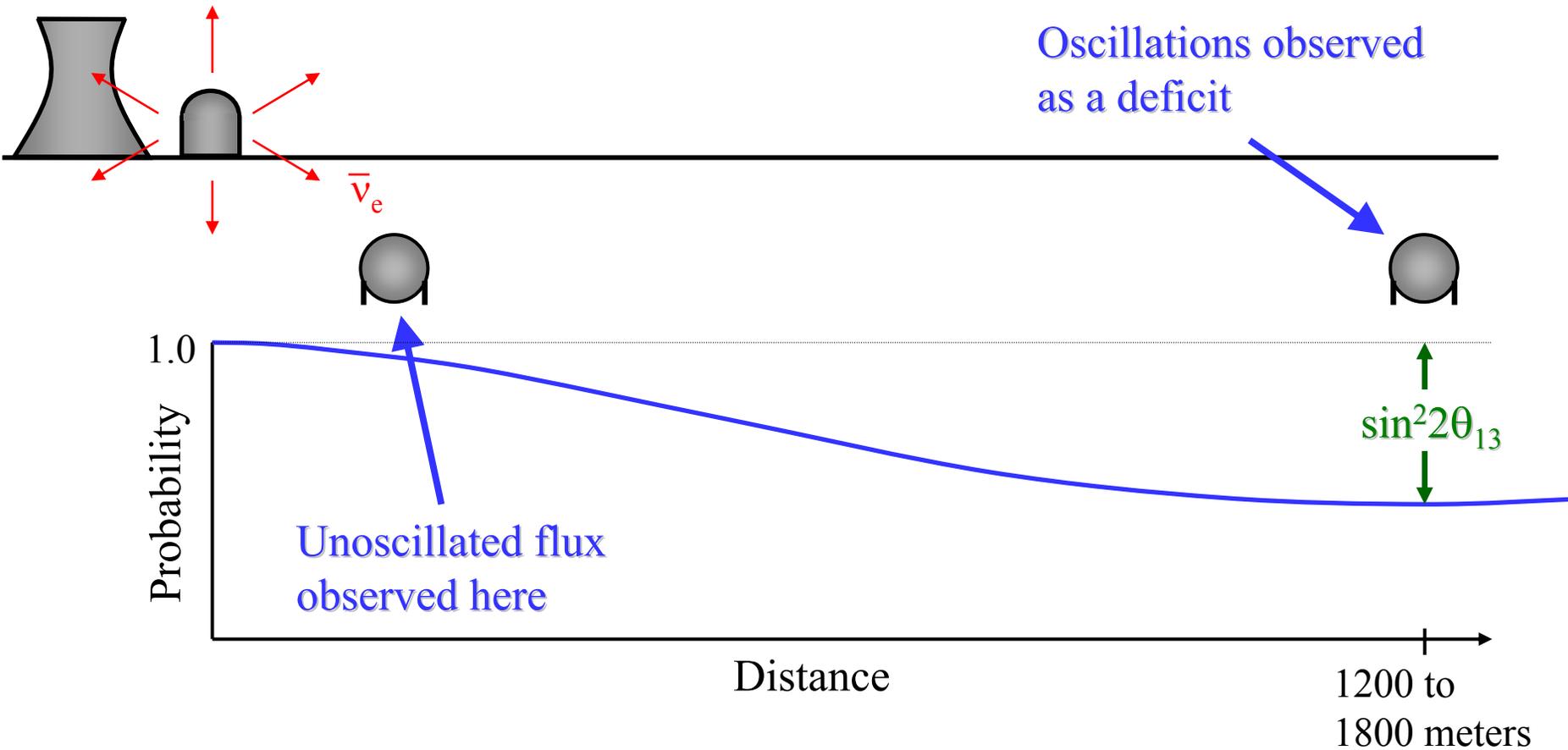


A nice method for observing the $\bar{\nu}$:
 $\bar{\nu} + p \rightarrow e^+ + n$ (then n captures)
 Use Gd-doped Scintillator oil detectors

Ways to improve:

- near and far detectors
- ability to switch detectors
- better shielding from cosmic rays

*the art is in control
of the systematics*



Janet's opinion:

Knowing if $\sin^2 2\theta_{13} > 1\%$ at 3σ is important physics

This is a very difficult measurement.

You simply cannot skimp on the systematic checks.

Reactor experiments have a bad reputation for false signals!

The one experiment that could reach this level, Braidwood, was regarded by DOE as too expensive (\$60M)

This leaves two other lesser reactor experiments:

- Double Chooz which reaches $\sin^2 2\theta_{13} > 2.5\%$ at 90% CL
*(Purposely designed to cover $\sim 1/3$ of the models
speedily and inexpensively: if “yes” get it quick!)*
- Daya Bay, which may reach $\sin^2 2\theta_{13} > 0.9\%$ at 90% CL⁶⁷
(But has no demonstrated design for this goal yet)

So if we can't get at θ_{13} via reactors, what can we do?

It can be measured in accelerator-based $\nu_\mu \rightarrow \nu_e$
long-baseline experiments:

$$P_{long-baseline} \simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta$$
$$+ \alpha \sin 2\theta_{13} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin^2 \Delta$$
$$+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta$$

$$\alpha \equiv \Delta m_{21}^2 / \Delta m_{23}^2$$

$$\Delta \equiv \Delta m_{31}^2 L / (4E_\nu).$$

But the situation is clearly messy!

Remember: you are trying to measure $P < 0.01$!

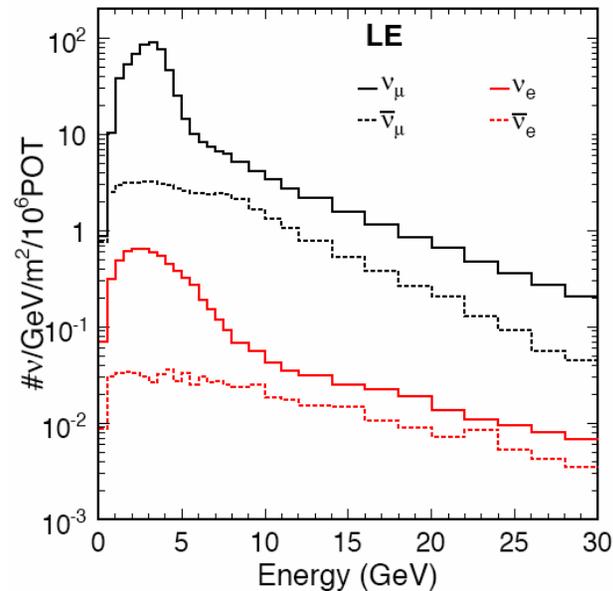
Problem 1: The typical wide-band LB beam...

Has a lot of ν_e contamination

Kaon decays

Muon decays

Has a high energy tail that leads to high rates of π^0 production \Rightarrow mis-ids

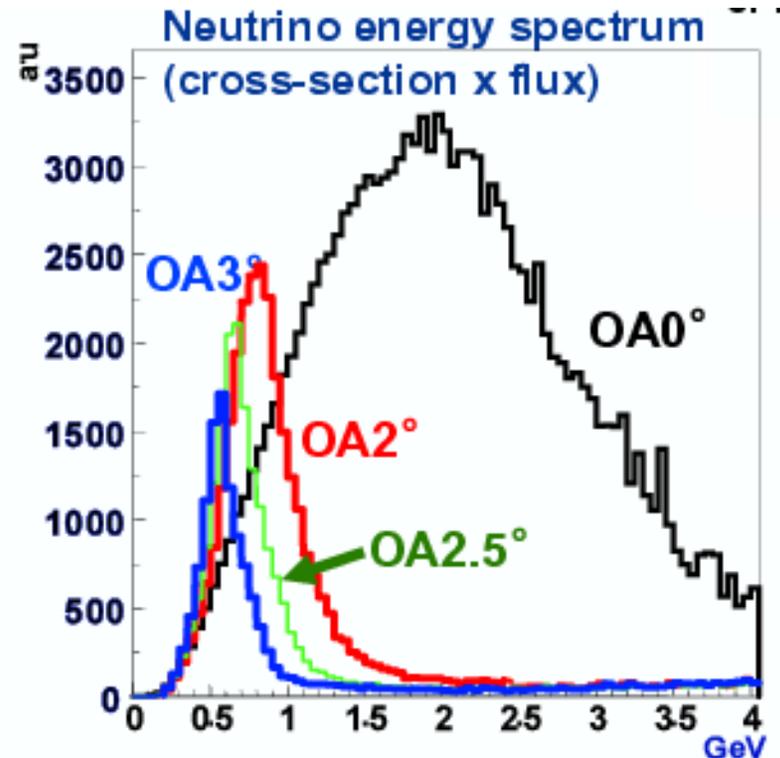


Going “off axis” makes the ν_μ beam monoenergetic
-- easier to pick out signal from background --
but less intense!



Approved Dec, 2003
Expected to run: 2009

Plan is to use a 2.5° off-axis beam
& the existing Super K detector



Problem 2: Knowing θ_{23} ...

Not squared.

$$\begin{aligned}
 P_{long-baseline} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta \\
 &+ \alpha \sin 2\theta_{13} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin^2 \Delta \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta
 \end{aligned}$$

angle not
multiplied
by two

$$\alpha \equiv \Delta m_{21}^2 / \Delta m_{23}^2$$

$$\Delta \equiv \Delta m_{31}^2 L / (4E_\nu).$$

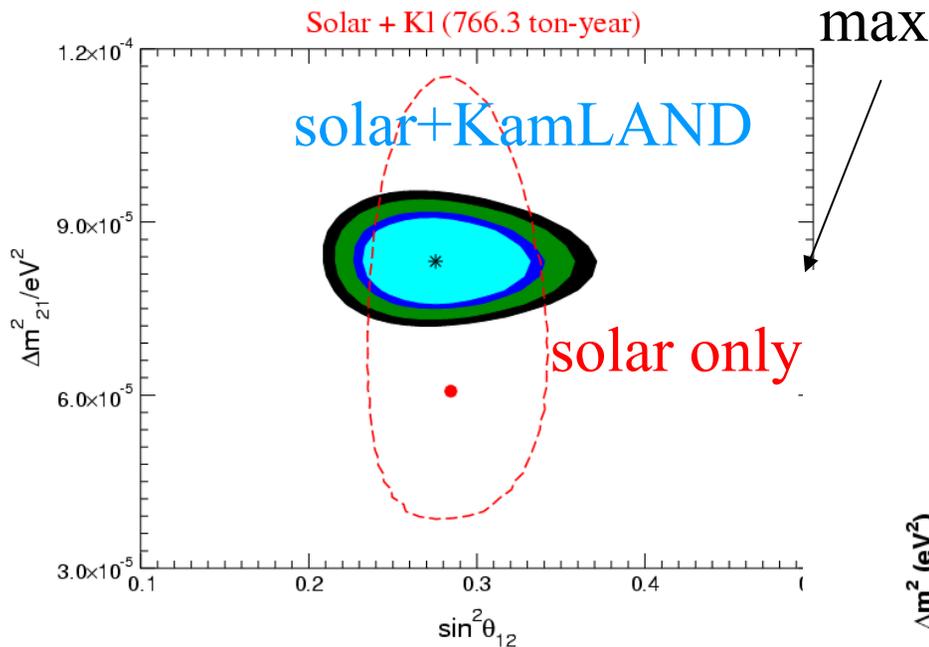
θ_{23} -- Minos will measure $d(\sin^2 2\theta_{23}) \sim 5\%$ (6 years)

T2K will measure $d(\sin^2 2\theta_{23}) \sim 1\%$ (3+5 years)

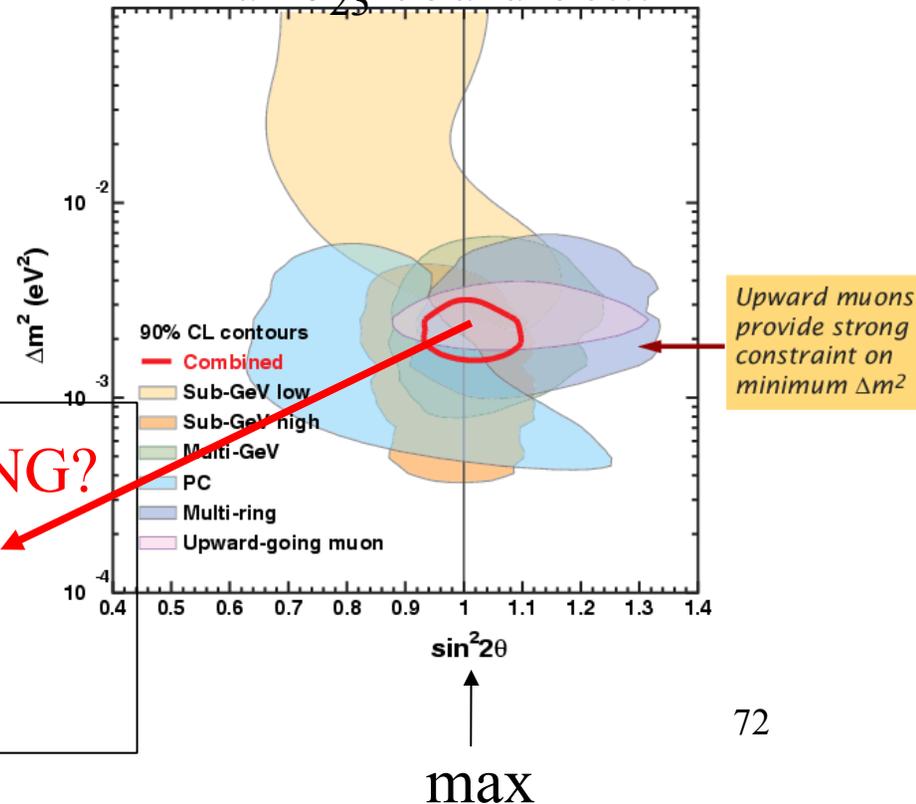
but you cannot tell if $\theta_{23} > 45^\circ$ or $< 45^\circ$!!! -- it's degenerate

θ_{23} is interesting
in and of itself...

None of the "well-measured" angles
in the quark sector
& the one "well measured angle"
in the neutrino sector,
are "maximal"



But θ_{23} could be...



Implications of MAXIMAL MIXING?

A new symmetry group
connecting the μ and τ

Problem 3: the precise value of $\Delta m^2_{\nu 23}$

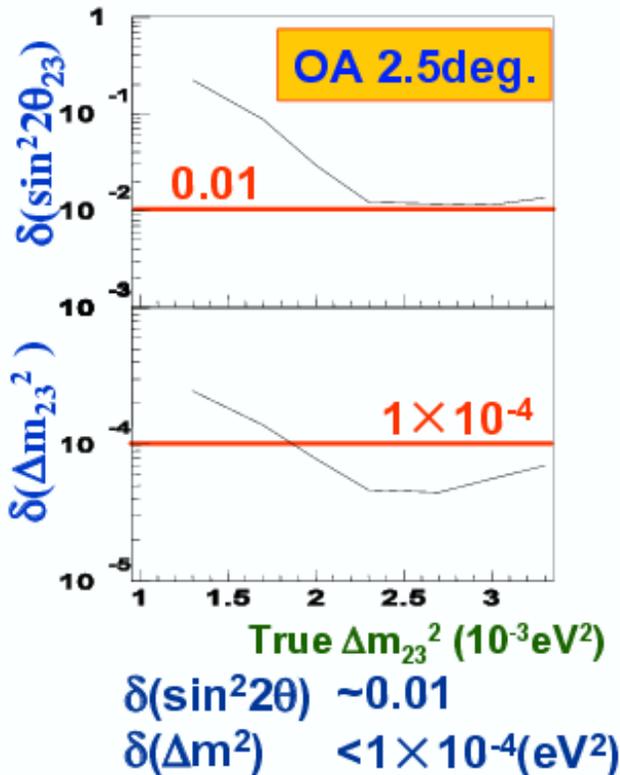
what can be
achieved at T2K
(3+5yrs)

$$P_{long-baseline} \simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta$$

$$+ \alpha \sin 2\theta_{13} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin^2 \Delta$$

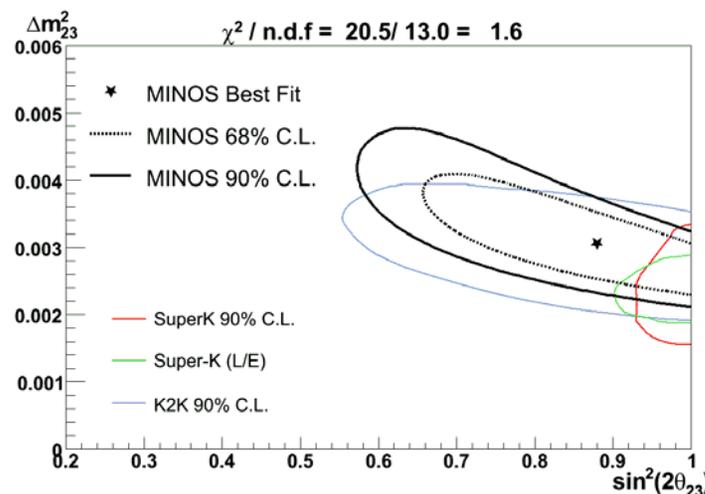
$$+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta$$

ν_μ disappearance

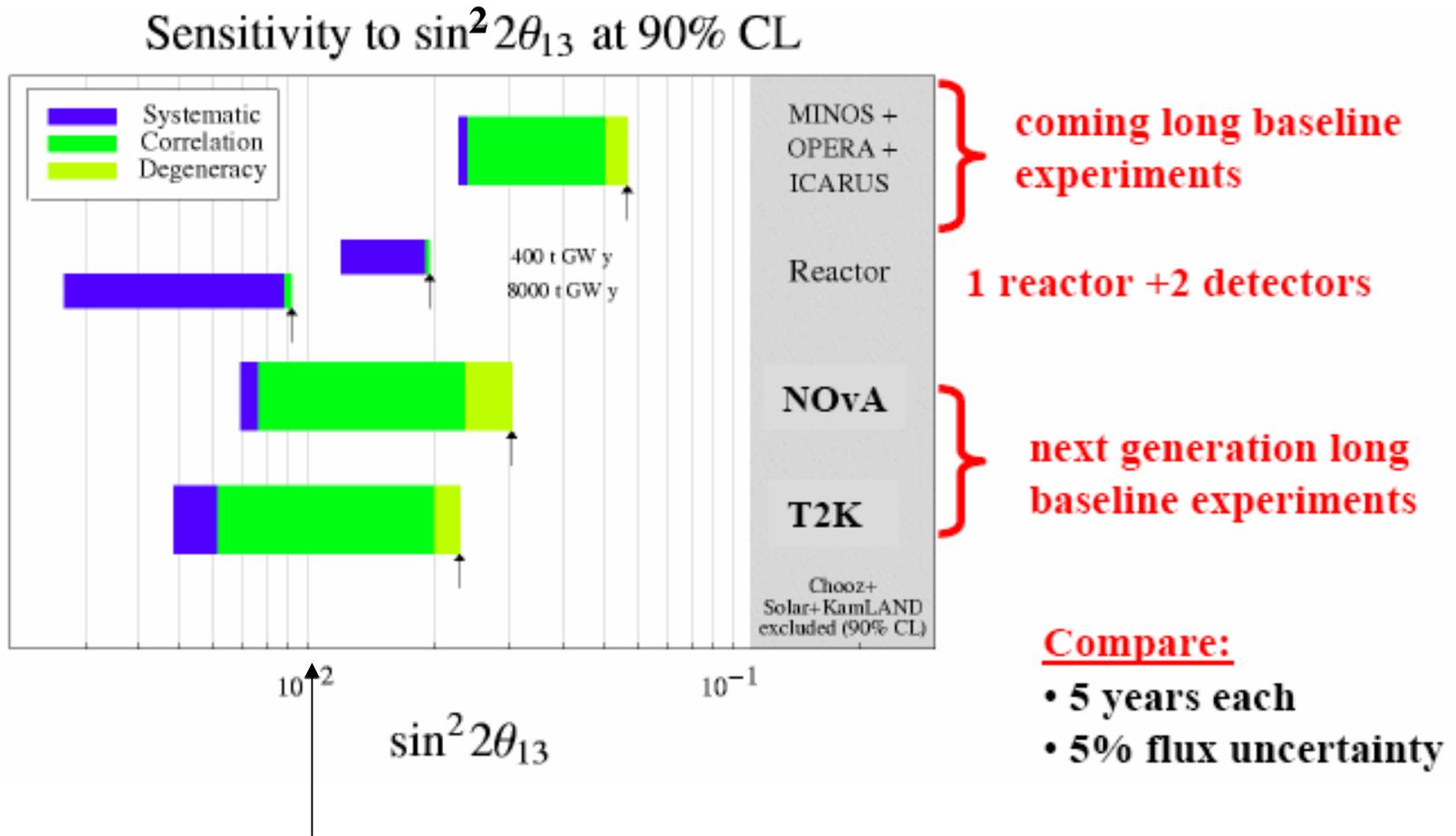


$$\alpha \equiv \Delta m^2_{21} / \Delta m^2_{23}$$

$$\Delta \equiv \Delta m^2_{31} L / (4E_\nu)$$



Manfred's summary of what you can expect



The combination is unlikely to get you 3σ if the right value is here... That's a worry.

Experiments addressing this model:

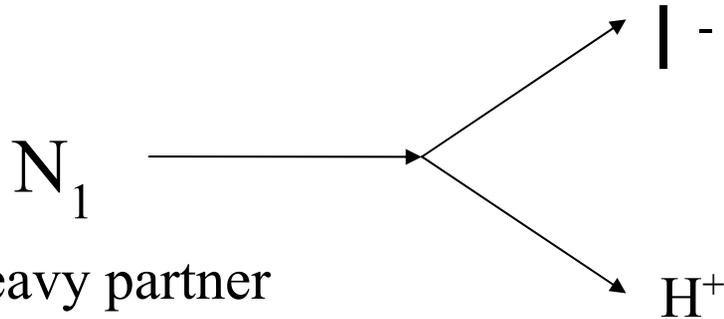
3. Is there CP Violation?

“A smoking gun” for Leptogenesis

The idea:

Before the electroweak phase transition...

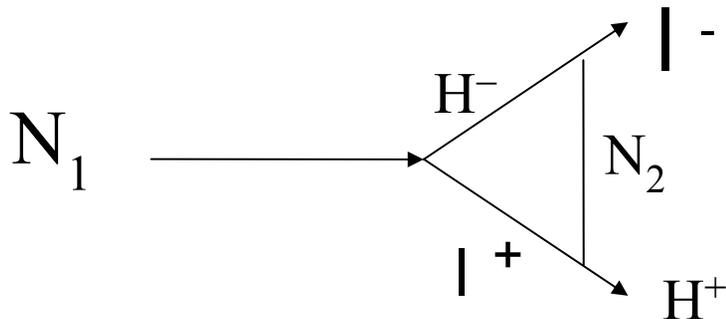
These are massless:



a heavy partner
to the ν (getting
mass from the
Majorana term)

Interference between these two
types of diagrams can lead to
**a different rate of decay to
particles than antiparticles**
→ **CP Violation**

"Leptogenesis"



*Today,
we cannot study the N 's
but we can study the ν 's...*

Putting CP violation into the light neutrino Mixing Matrix:

The CP Violation Parameter

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

From Atmospheric and Long Baseline Disappearance Measurements

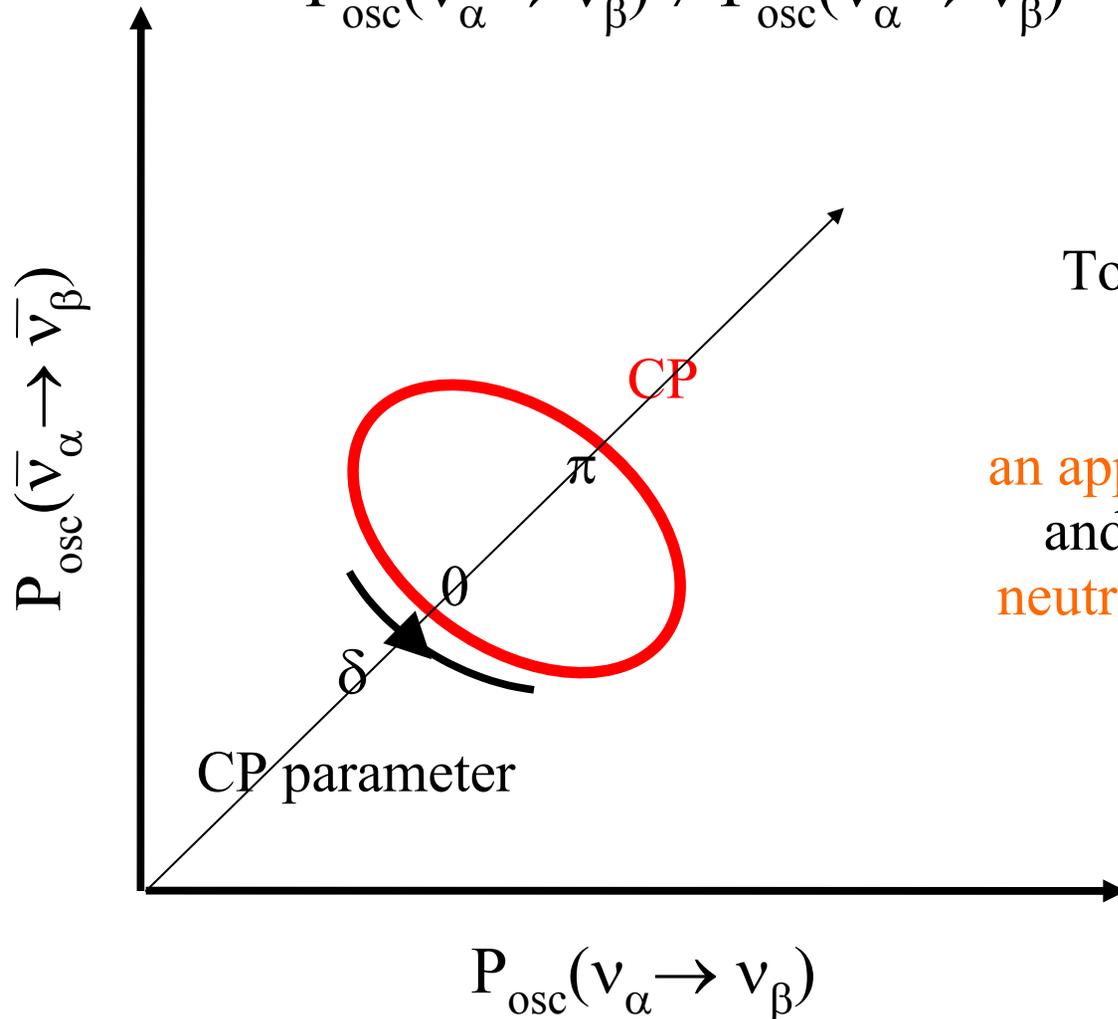
From Reactor Disappearance Measurements

From Long Baseline Appearance Measurements

From Solar Neutrino Measurements

CP violation
& light neutrinos \searrow

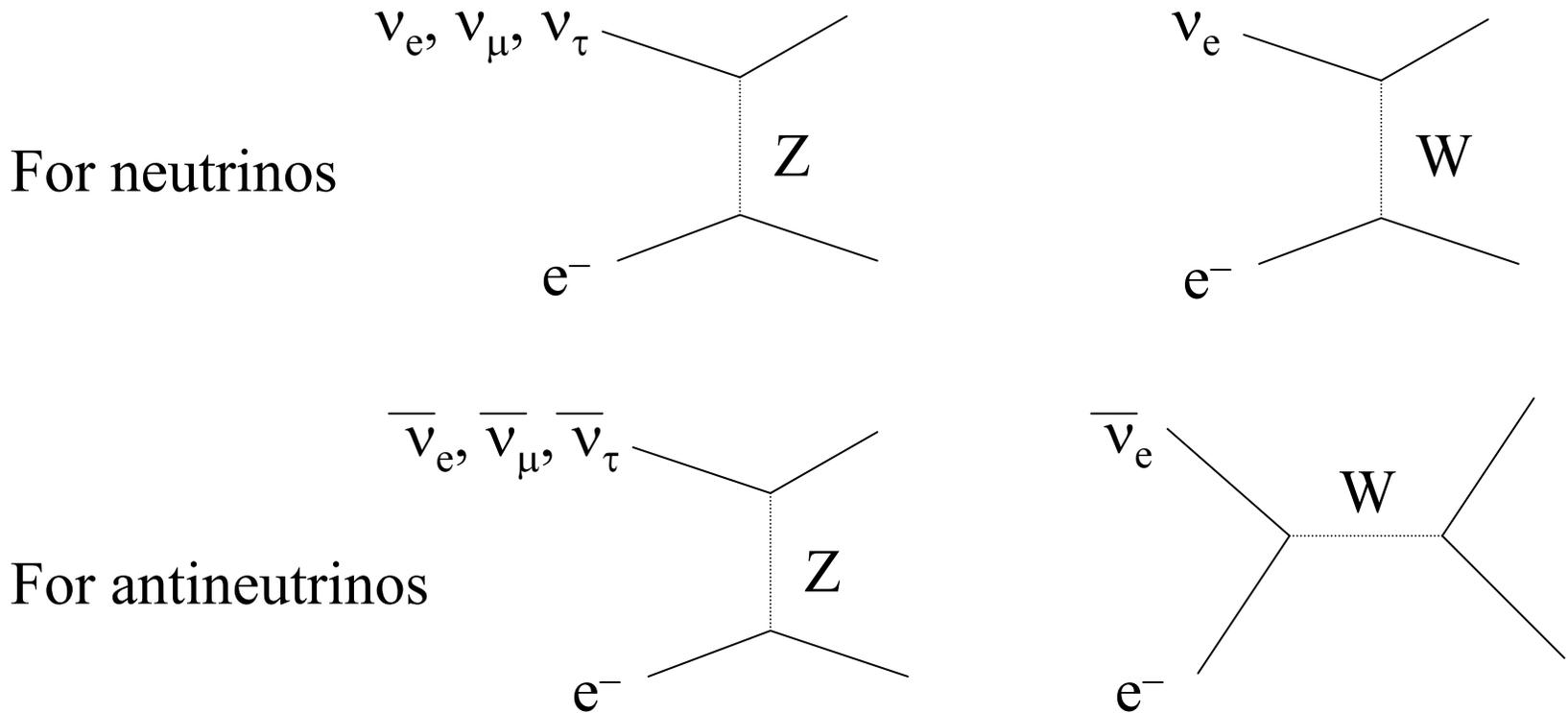
$$P_{\text{osc}}(\nu_{\alpha} \rightarrow \nu_{\beta}) \neq P_{\text{osc}}(\bar{\nu}_{\alpha} \rightarrow \bar{\nu}_{\beta})$$



To see CP violation
in oscillations
you need
an appearance experiment
and results from both
neutrino and antineutrino
running

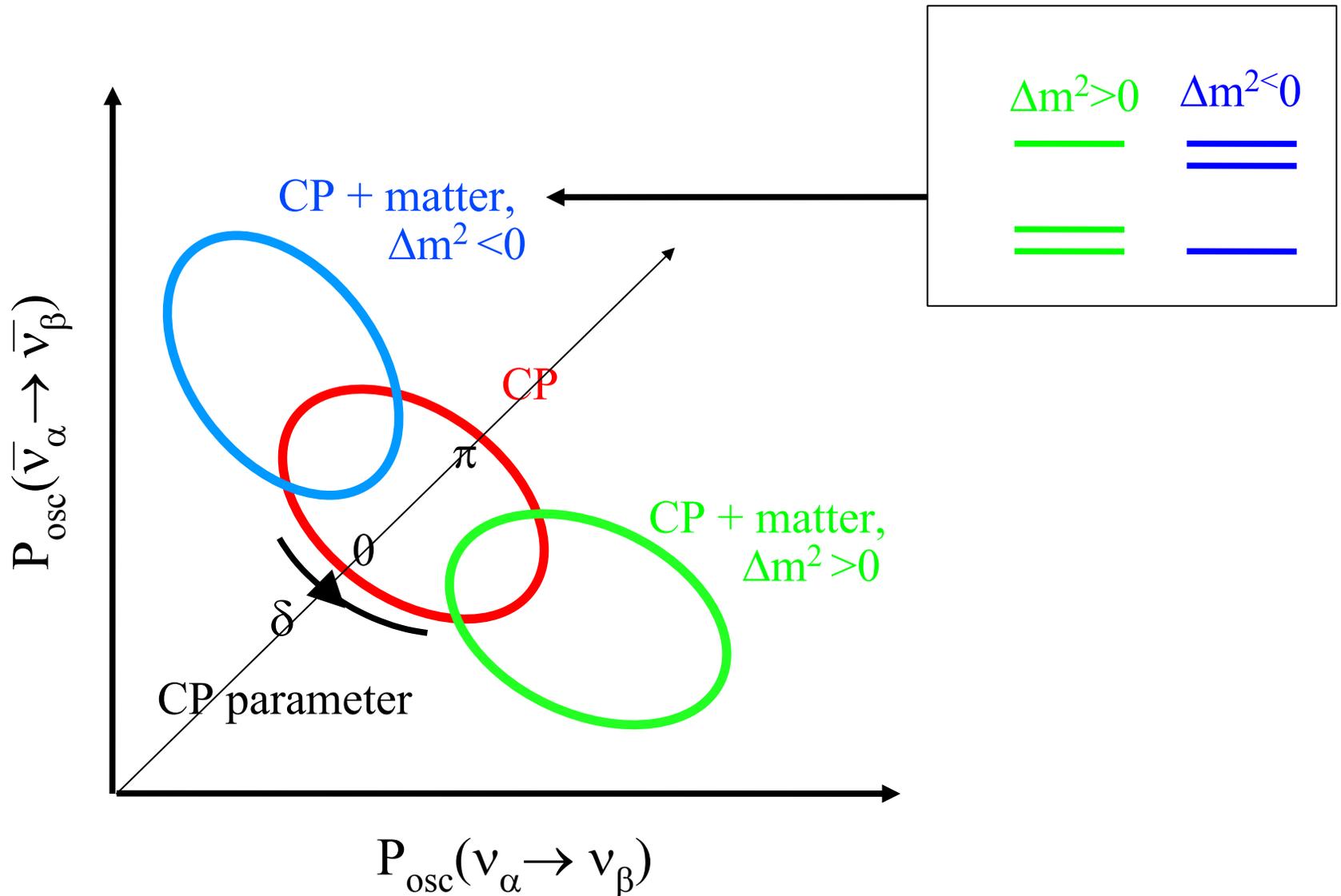
But matter effects also cause $P_{\text{osc}}(\nu_\alpha \rightarrow \nu_\beta) \neq P_{\text{osc}}(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$

There are two diagrams for the “electron” flavor...



But one is t-channel and the other s-channel

And to make matters worse, the sign for each depends on Δm^2 !

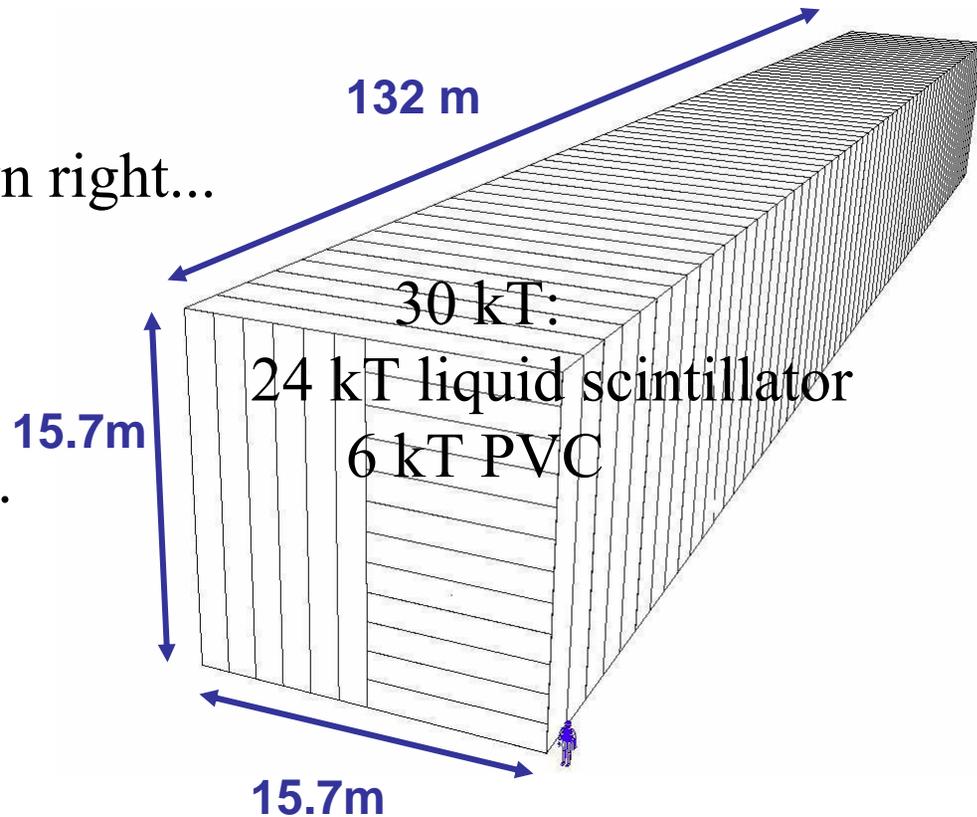


Matter effects are only an important for baselines >500 km

Specifically, the **NOvA Experiment**: $\langle E_\nu \rangle = 2.3$ GeV, $L = 810$ km

Arguably,
the mass hierarchy
is interesting in its own right...

It may help
discriminate
between GUT models.



Janet's opinion:

CP violation is going to be hard to measure,
and so it is best to do this in an experiment
without matter effects...

With CP violation

$$\begin{aligned} P_{\text{long-baseline}} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta \\ &\mp \alpha \sin 2\theta_{13} \sin \delta_{CP} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \Delta \\ &+ \alpha \sin 2\theta_{13} \cos \delta_{CP} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin^2 \Delta \\ &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta \end{aligned}$$

... another good reason to know θ_{13} well!
(note: if it is small, you don't see ~~CP~~)

$$\begin{aligned}
P_{\text{long-baseline}} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta \\
&\mp \alpha \sin 2\theta_{13} \sin \delta_{CP} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \Delta \\
&+ \alpha \sin 2\theta_{13} \cos \delta_{CP} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin^2 \Delta \\
&+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta
\end{aligned}$$

1 equation and a whole lot of unknowns.

Pick 2 unknowns to plot against one another:

$$\text{CP } \delta \text{ vs } \sin^2 2\theta_{13}$$

Assume T2K measures $d(\sin^2 2\theta_{23}) \sim 1\%$ (3+5 years)

Look at various scenarios...

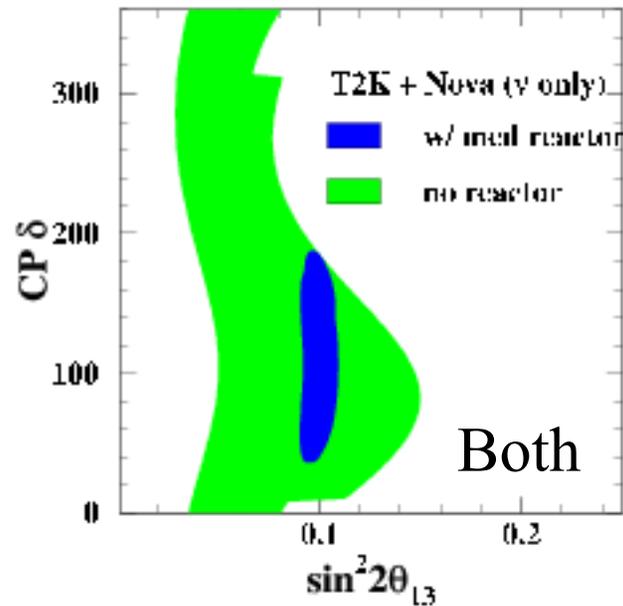
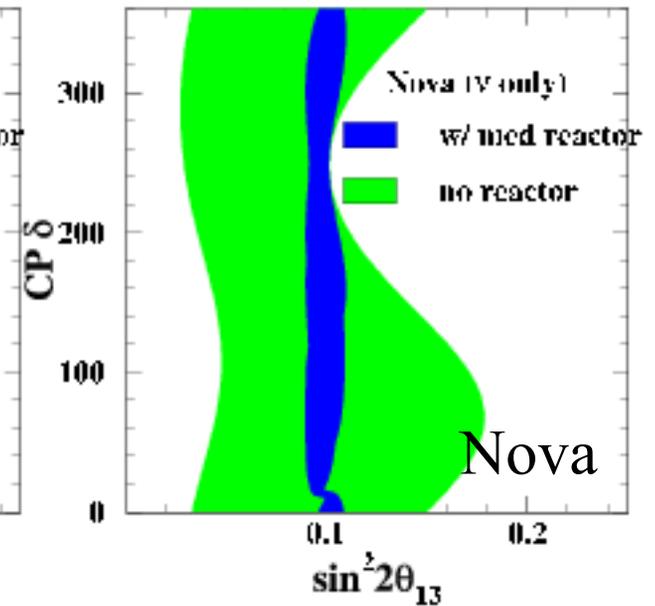
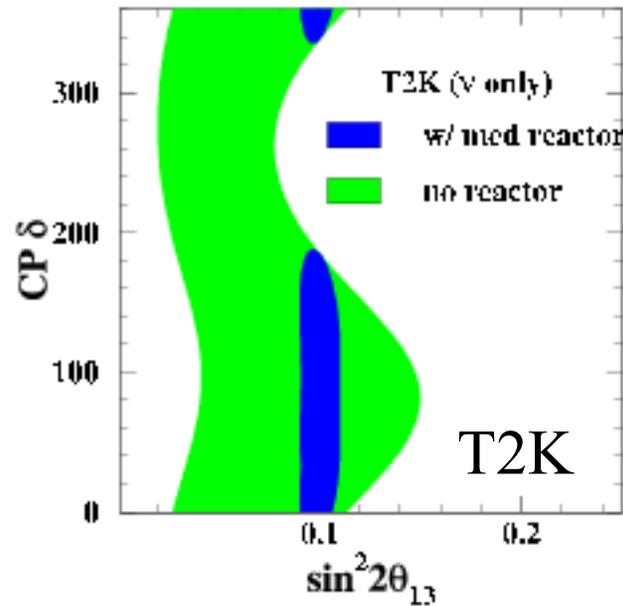
- without a mid-scale reactor
- with a mid-scale reactor

If the real value is 90°

This is what experiments extract...

If θ_{13} is too small, the long-baseline experiments have no sensitivity

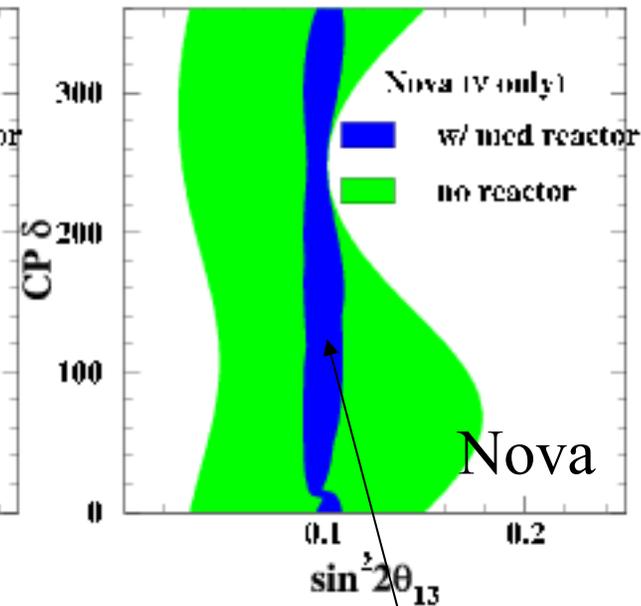
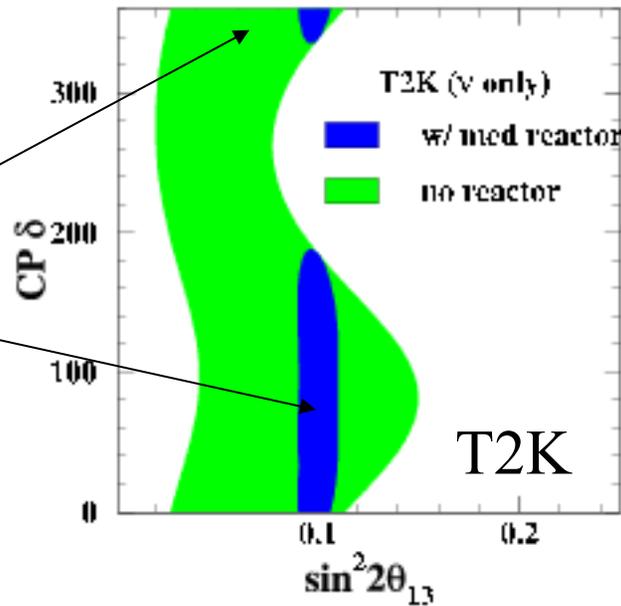
90% CL regions for $\sin^2 2\theta_{13}=0.1, \delta=90$



If θ_{13} is large enough, the reactor slice allows non-zero CP to be distinguished.

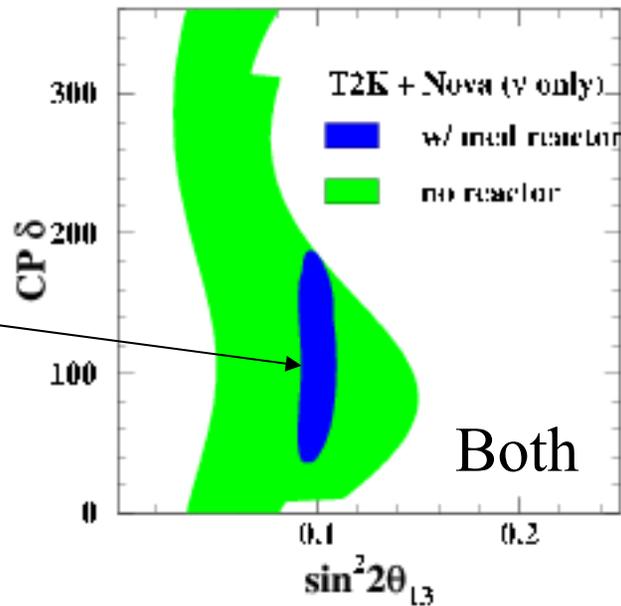
90% CL regions for $\sin^2 2\theta_{13}=0.1, \delta=90$

You could have just these regions by 2015



Or this region by 2020

Or this by 2020 with both experiments....



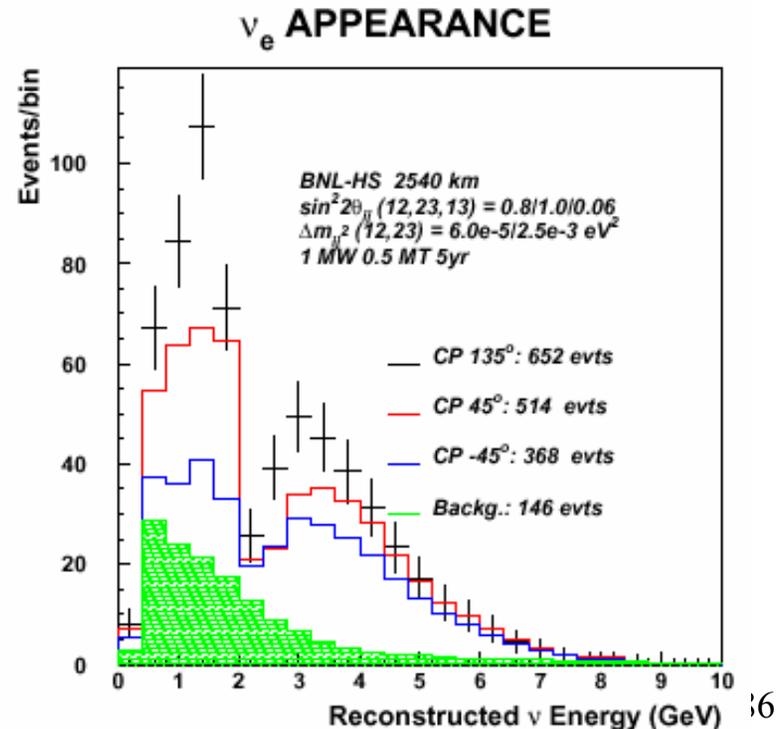
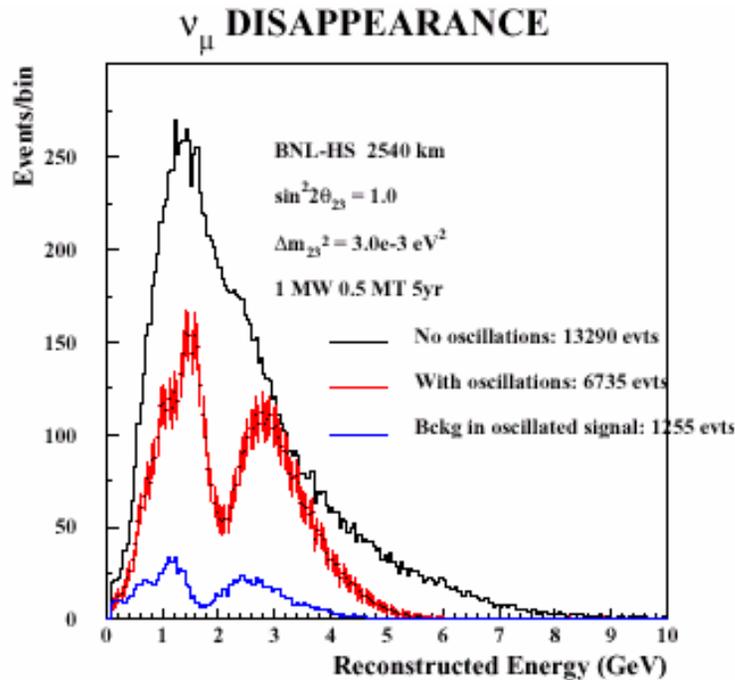
We will have to get lucky!

If the CP Violation signal is not 90 or 270 degrees, How can we see it?

2450km baseline
 1MW source
 MT detector
 5×10^7 s exposure

VLBvO

A beam from BNL or Fermilab to Homestake or Henderson



A word of caution:

The CP violation accessible in the oscillation matrix, is not the same as the CP-violation in the Majorana sector that produced leptogenesis.

But existence of CP-violation in the the oscillation matrix would make leptogenesis very plausible.

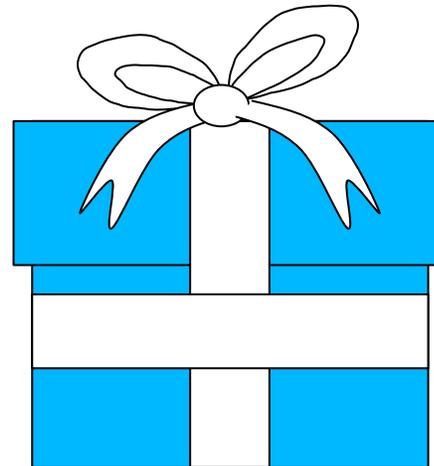
Conclusions for Today

Neutrino mass and mixing must be due to some higher scale physics.

A “natural” candidate is Majorana-neutrino inspired, and makes definite predictions:

- 1) Neutrinoless double beta decay should be observed.
- 2) θ_{13} should be relatively large
- 3) CP violation in oscillations may be observable

Which leads to a very pretty package of experiments....



The Plan for the Future:

Neutrinoless Double Beta Decay:

GERDA/Majorana, CUORE, EXO and others

Reactor (θ_{13}):

Double Chooz, Daya Bay

Long Baseline:

Minos, T2K, Nova, VLBvO