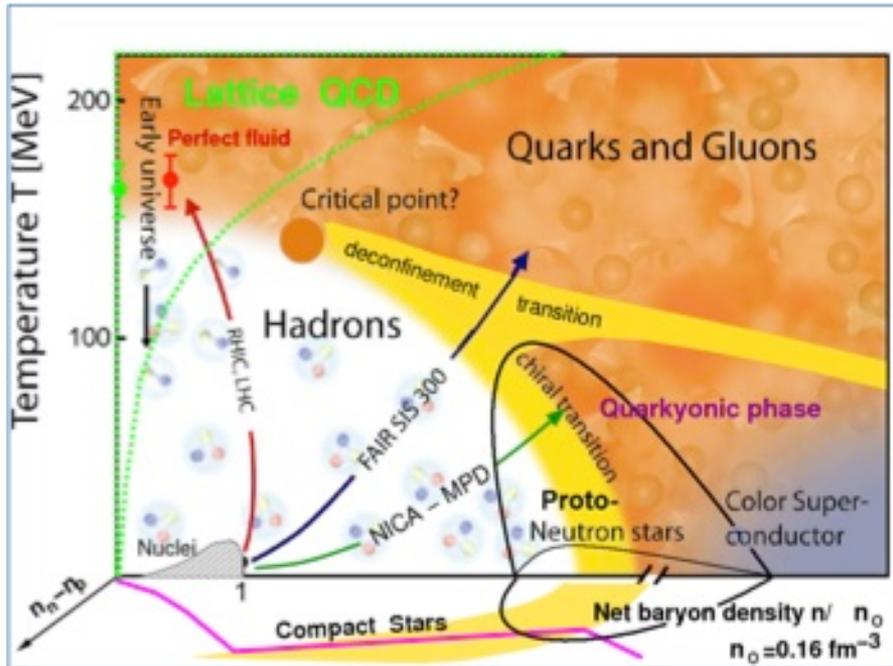


# SPC perspective on USQCD thermodynamics

Peter Petreczky, BNL

Tools : LQCD, Heavy ion experiments and phenomenology

LQCD results → models of dynamical evolution → RHIC experiments



Strategic goals outlined in 2013 White paper, “Computational Challenges in QCD Thermodynamics”:

1) EoS at zero chemical potentials in the continuum limit  
⇒ Hydro models in HIC at top energies

2) Thermodynamics at non-zero chemical potentials, fluctuations of conserved charges  
⇒ Freezout condition in HIC, BES@RHIC

3) Universal properties of the chiral transition,  $T_c(\mu)$   
Freezout condition in HIC, BES@RHIC

4) In-medium hadron properties  
⇒ dileptons/quarkonia

# Physics of heavy ion collisions and LQCD

high temperature QCD  
weak coupling ?

Chiral transition,  $T_c$  fluctuations of conserved charges

Initial State:  
colliding nuclei

Quark Gluon Plasma &  
hydrodynamic expansion

EoS,  
viscosity

hadronic rescattering  
& freeze-out

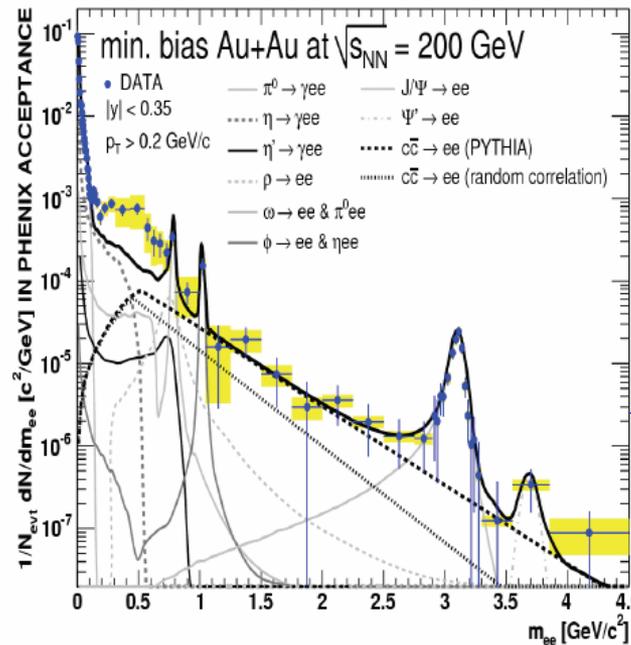
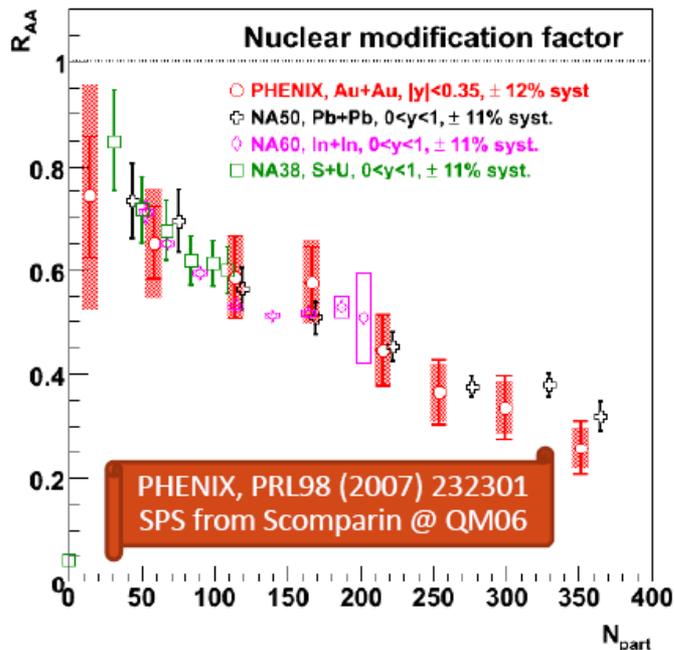
Equilibration:  
turbulent color fields

EM and heavy  
flavor probes

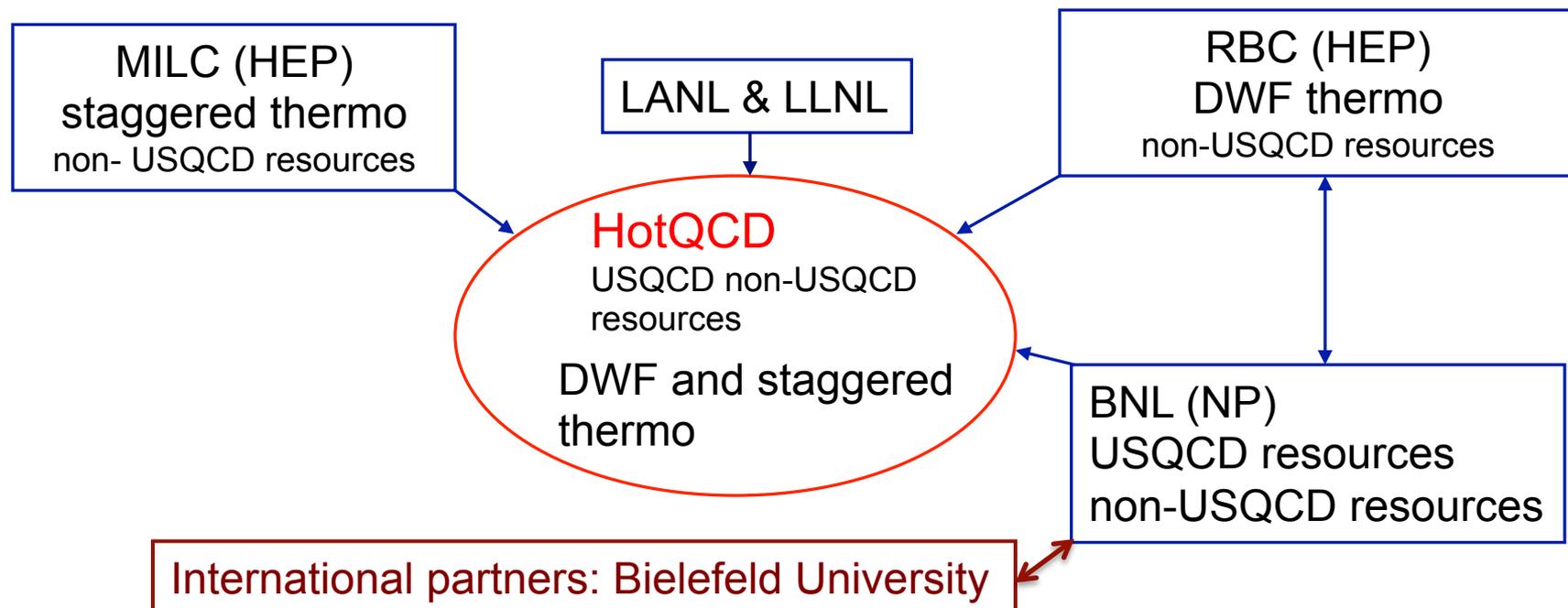
Hadronization

test of Hadron  
Resonance Gas  
(HRG)  
using LQCD

quarkonium spectral  
functions,  
heavy quark diffusion,  
thermal dileptons



# Structure of thermo LQCD community and USQCD proposals



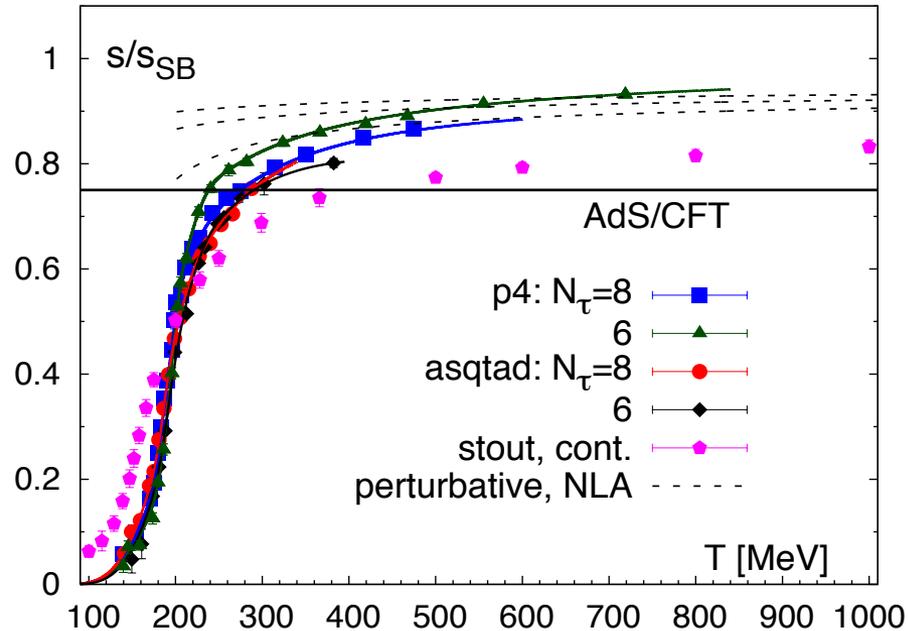
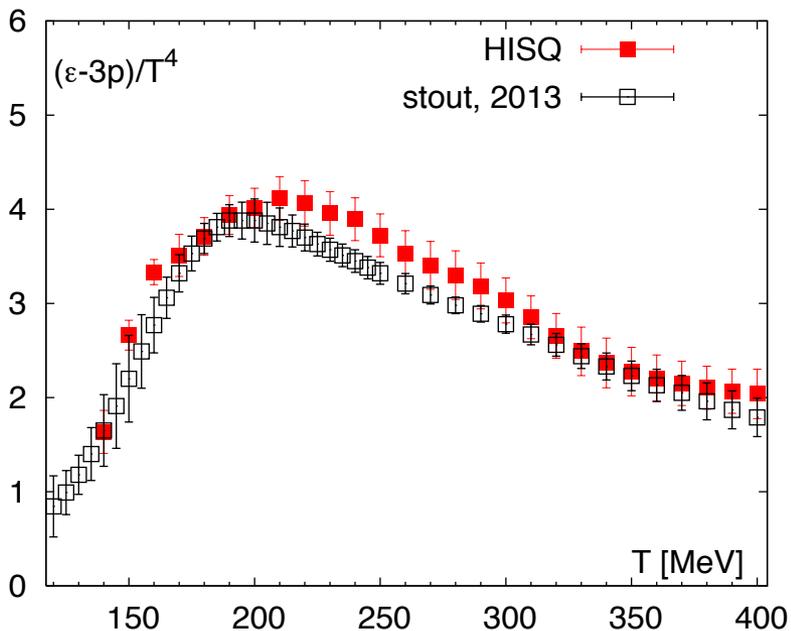
USQCD proposals in 2013 (time requested in M J/psi core h and GPU node h) :

HotQCD (PI Karsch) Charge fluctuations : BG/Q, 25M; Titan, 44.5M (INCITE)

BNL (PI H. Ohno) Universal Behavior of the chiral transition : USQCD clusters, 37.4M

BNL (PI S. Mukherjee) Taylor Expansion : GPUs 2.4M GPU hours

# Status of the EoS calculations



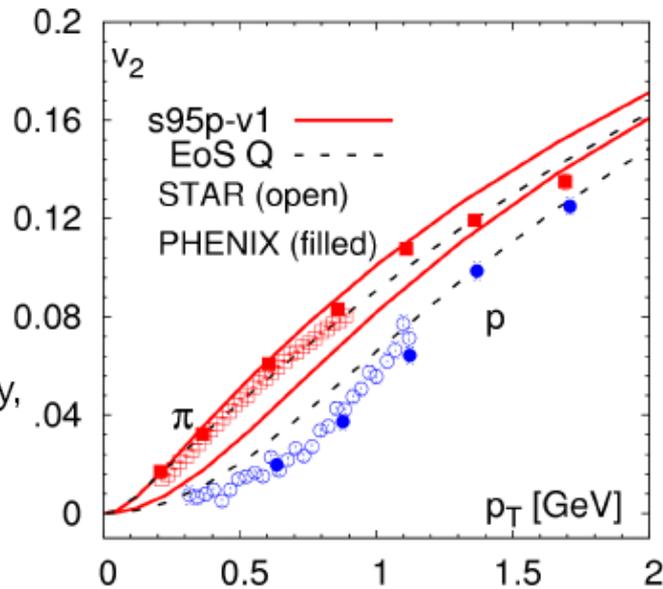
Running is finished analyzing data for the final publication

2013 White paper:

- 1) What is the nature of the QGP at  $T > 300$  MeV ? (LHC)
- 2) What is the speed of sound ? (RHIC and LHC)

LQCD based parametrization of the EoS  
Used in most of hydro models for HIC

P. Huovinen, P. Petreczky,  
NP A837, 26 (2010)



Future: include the effect of charm quark  
(see 2013 White paper)

# QCD thermodynamics at non-zero chemical potential

Taylor expansion :

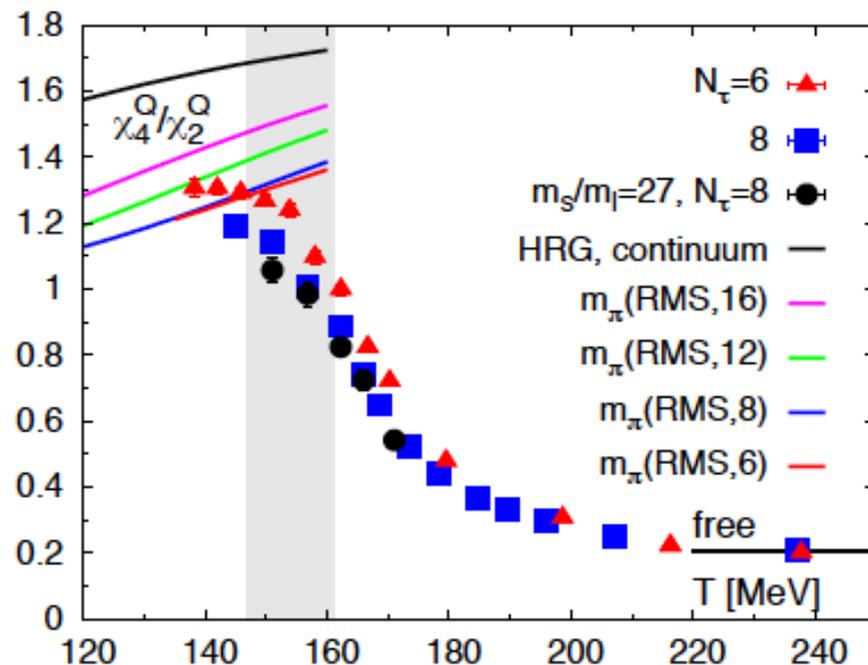
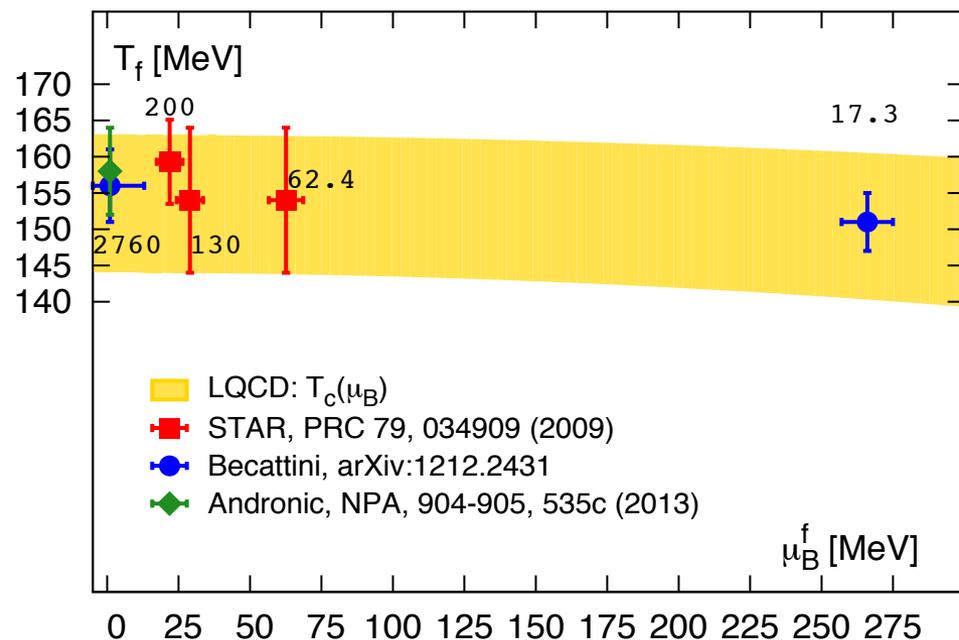
$$\frac{p(T, \mu_B, \mu_Q, \mu_S)}{T^4} = \sum_{i,j,k} \frac{1}{i!j!k!l!} \chi_{ijk}^{BQS} \cdot \left(\frac{\mu_B}{T}\right)^i \cdot \left(\frac{\mu_Q}{T}\right)^j \cdot \left(\frac{\mu_Q}{T}\right)^k$$

Taylor expansion coefficients give the fluctuations and correlations of conserved charges, e.g.

$$\frac{\chi_2^X}{T^2} = \frac{\chi_X}{T^2} = \frac{1}{VT^3} (\langle X^2 \rangle - \langle X \rangle^2) \quad \frac{\chi_{11}^{XY}}{T^2} = \frac{1}{VT^3} (\langle XY \rangle - \langle X \rangle \langle Y \rangle) \quad \Rightarrow \quad R_{nm} = \chi_n^Q / \chi_m^Q \quad \text{BES @ RHIC and freezeout conditions}$$

can be done very efficiently on GPUs

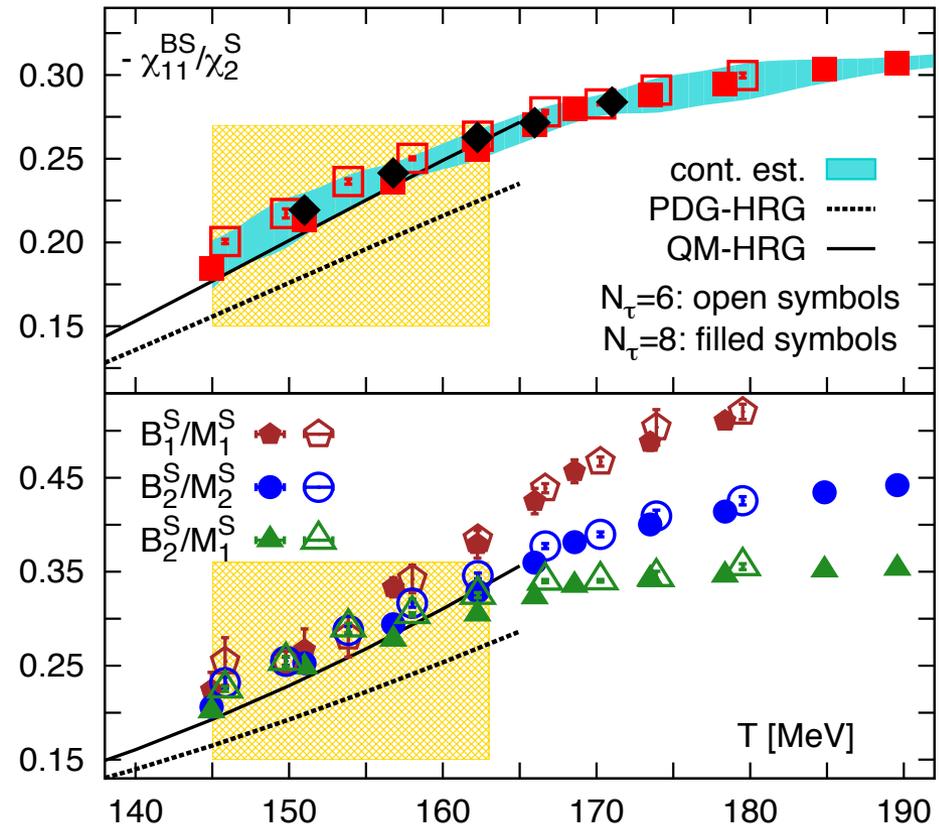
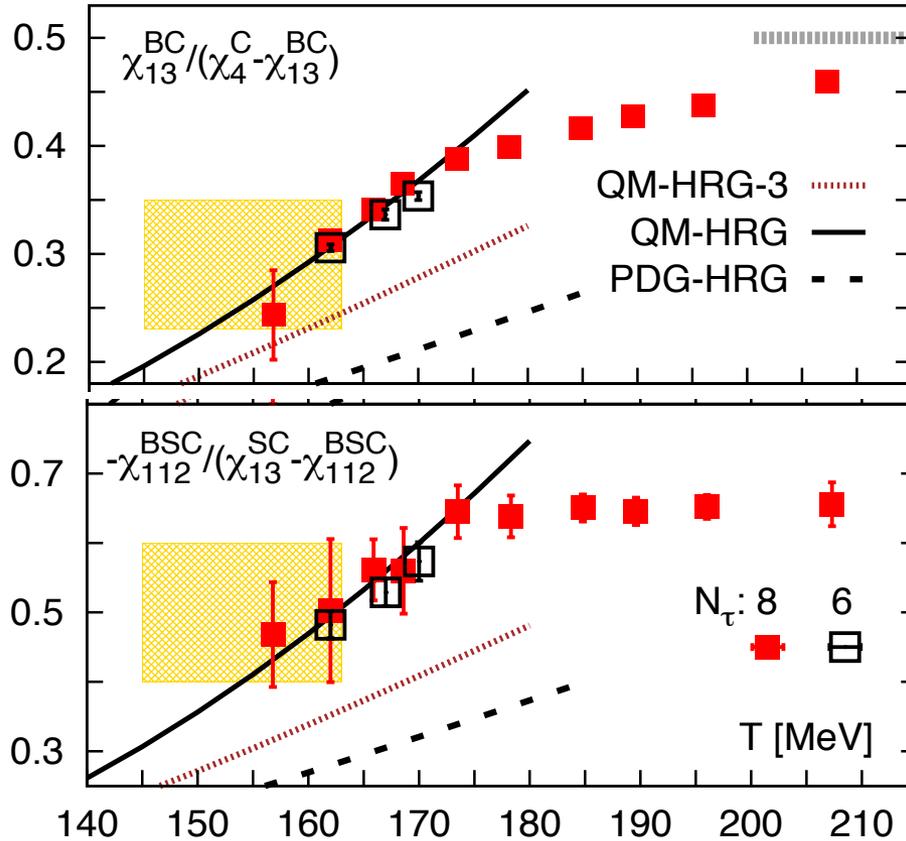
HotQCD proposal (PI: Karsch)



# Charge and strangeness fluctuations and missing hadrons

Bazavov et al, arXiv:1404.4043v1

$N_\tau=6,8, m_\pi = 160$  MeV



Experimental knowledge of strange and charm hadron spectrum is rather incomplete !

HRG that includes hadron states predicted by quark model (also LQCD) agrees better with lattice results than HRG with PDG states only !

⇒ Extend the calculations to physical pion mass and close to the continuum limit

proposal by Mukherjee

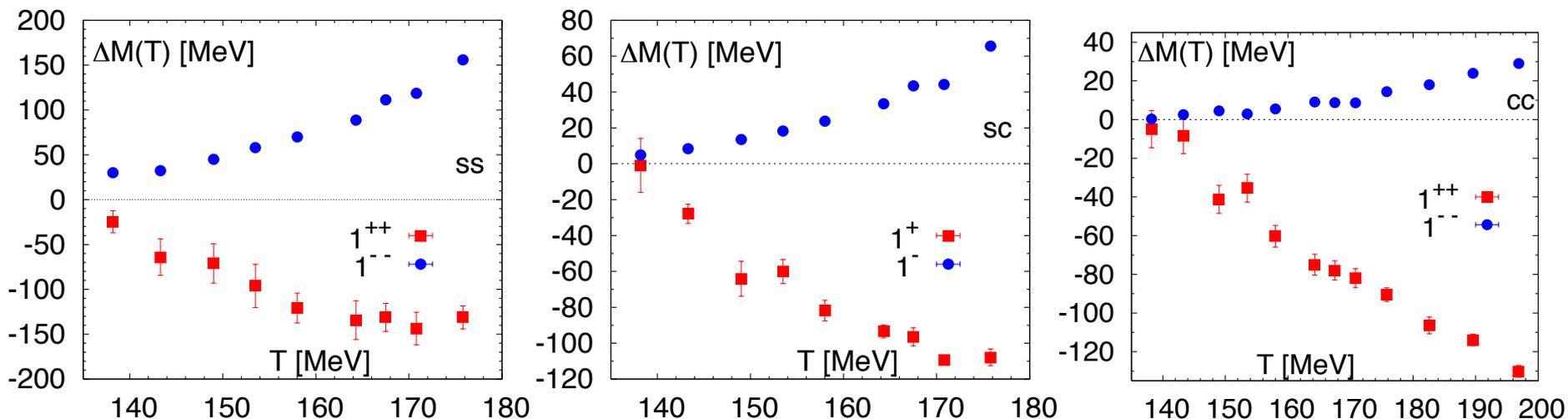
# Meson correlators and spectral functions

No new proposals have been submitted, last year B-type proposal by Maezawa: calculations of spatial meson correlators which are related to the spectral functions

$$G(z, T) = \int_{-\infty}^{\infty} e^{ipz} \int_0^{\infty} d\omega \frac{\sigma(\omega, p, T)}{\omega}$$

$$G(z, T) \sim \exp(-M_{scr} z)$$

Significant change in the meson screening masses  $\Delta M = M_{scr}(T) - M_{T=0}$  close to  $T_c$  except for  $J/\psi$



However,  $T > 0$  HISQ configuration are being used for related analysis:

- 1) Calculations of the static potential at  $T > 0$ . [arXiv:1303.5500](https://arxiv.org/abs/1303.5500), [arXiv:1404.4267](https://arxiv.org/abs/1404.4267)
- 2) Calculation of bottomonium correlators using NRQCD at  $T > 0$ , [arXiv:1310.6461](https://arxiv.org/abs/1310.6461)

# What is the transition temperature ?

$T_c$  determination requires the study of the chiral transition as function of the quark mass (now HISQ, later DWF):

$$M_b = \frac{m_s \langle \bar{\psi} \psi \rangle_l}{T^4} = h^{1/\delta} f_G(t/h^{1/\beta\delta}) + f_{M,reg}(T, H)$$

$$H = m_l/m_s, \quad h = H/h_0, \quad t = (T - T_c^0)/(T_c^0 t_0)$$

Zero net baryon density, HotQCD:

Bazavov et al, Phys. Rev. D85 (2012) 054503

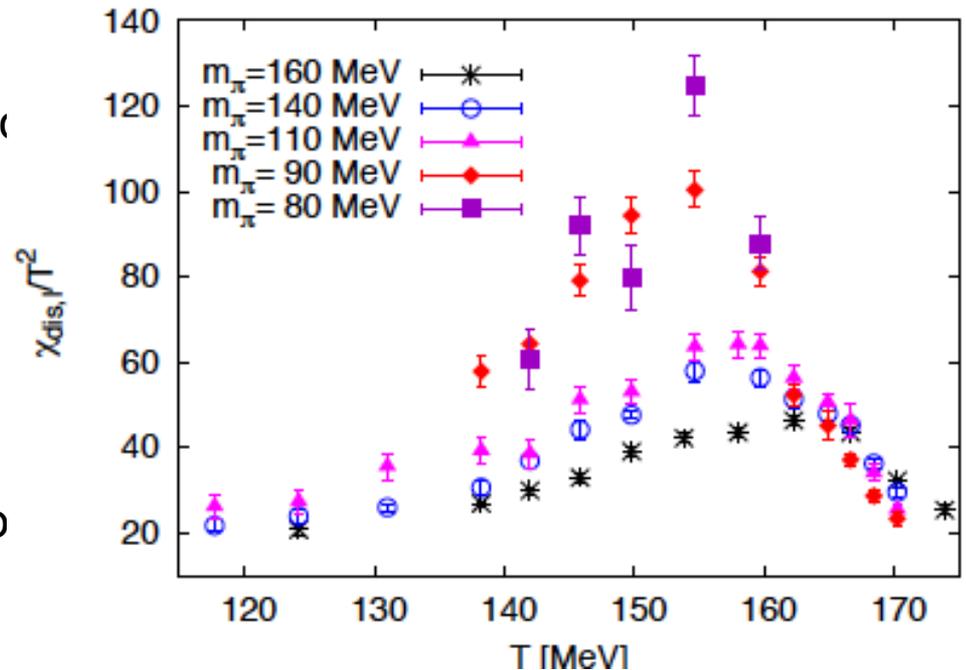
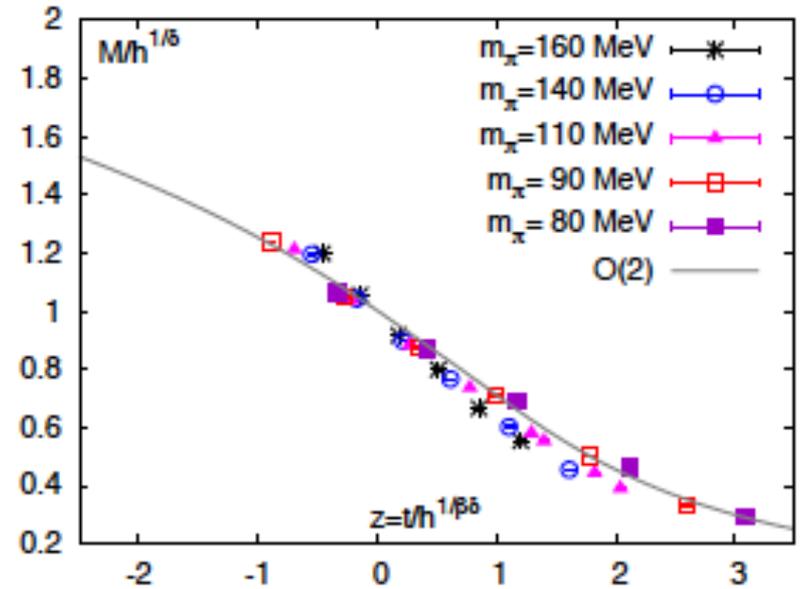
$$T_c = (154 \pm 8 \pm 1(\text{scale})) \text{MeV}$$

How well is the regular part under control, what is the nature of the transition  
In the chiral limit, what is the role of the axial anomaly ?

Need more smallest  $m_l$  :

USQCD Proposal by H. Ohno:  
down to  $m_l = m_s/100$  ( $m_\pi = 80 \text{ MeV}$ )

$\Rightarrow$  crucial for understanding the transition at non-vanishing baryon density,  $T_c(\mu)$



## Conclusions

Lattice QCD starts to provide quantitative results that provide important input for interpreting the experimental results from HIC

$T_c$ , EoS, fluctuation of conserved charges, spectral functions

How sensitive is the QCD transition at physical quark masses to the universal properties in the chiral limit ?

How the transition is modified by baryon chemical potential ?

How the hadronic spectral functions are modified when  $T$  is increased ?

Use improved staggered fermions to achieve sufficiently small lattice spacing and large  $N_T$  (*now*)

Use chiral fermions to control the symmetries of QCD (*future*)