



# Berndt Müller: hunting for the Quark Gluon Plasma



*Chasse a la Licorne*

932.12

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QGP

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QGP

# Some of Berndt's notable contributions

- '86: Müller & Rafelski, strangeness enhancement in AA: first *real* signal for QGP!
- '86: Plunien, Müller & W. Greiner, Casimir effect
- '92: Geiger & Müller, *seminal* work on parton cascades
- '03: Fries, Müller, Nonaka & Bass, recombination - *amazingly* successful

## Former post-docs:

### Tenured:

Alec Schramm (Occidental College)  
Klaus Kinder-Geiger (Deceased)  
Xin-Nian Wang (LBL)  
Sen-Ben Liao (National Chung-Cheng Univ, Taiwan)  
Carsten Greiner (Frankfurt)  
Dirk Rischke (Frankfurt)  
Steffen Bass (Duke)  
Chiho Nonaka (Nagoya)  
Rainer Fries (Texas A&M)

### TBT (to be tenured):

Thorsten Renk (Jyväskylä)  
Abhijit Majumder (Ohio State Univ.)

Industry: Jörg Ruppert

# A recent example: chiral magnetic effect

Asakawa, Majumder, & Müller, arXiv:1003.2436; Müller & Schäfer, 1009.1053

Considered anomalous  $\pi$ - $\gamma$ - $\rho$  coupling  $\mathcal{L}_{eff} \sim \epsilon^{\alpha\beta\gamma\delta} F_{\alpha\beta} \partial_\gamma \pi^0 \rho_\delta^0$

Wess-Zumino-Witten model: general effective Lagrangian for anomalous couplings

$$\mathcal{L}_{eff} \sim \frac{e^2 N_c}{48\pi^2 f_\pi} \epsilon^{\alpha\beta\gamma\delta} \pi^0 F_{\alpha\beta} F_{\gamma\delta} - \frac{2ieN_c}{\pi^2 f_\pi^3} \epsilon^{\alpha\beta\gamma\delta} A_\alpha \partial_\beta \pi^0 \partial_\gamma \pi^+ \partial_\delta \pi^- + \dots$$

First term:  $\pi^0 \rightarrow \gamma \gamma$ . Second term:  $\omega \rightarrow \gamma \gamma \gamma$ . Integrate 2nd term by parts

$$\pi^0 \epsilon^{\alpha\beta\gamma\delta} F_{\alpha\beta} \partial_\gamma (\pi^+ \partial_\delta \pi^-) \sim \pi^0 B_i \partial_0 J_i + \pi^0 \epsilon^{ijk} E_i \partial_j J_k$$

$J$  is the pion e.m. current;  $J \sim \rho$  by VMD

$B \partial J$  is the chiral magnetic effect;  $E \cdot \partial \times J$ , is the chiral electric effect.

AMM: need domains of  $\langle \pi^0 \rangle$ . Too small to explain STAR data by  $\sim 10^{-4}$ .

See, also, Schlichting & Pratt, arXiv:1005.5431 & 1009.4283.

# For Heavy Ions, will LHC be “*like*” RHIC?

1. *Yes*: small increase in elliptic flow, (appropriately scaled) multiplicity  
(Nearly) ideal hydro works  
Approach from *strong* coupling. Gyulassy: “Diving into the Black Hole”
2. *Sorta*: elliptic flow smaller, (scaled) multiplicity higher  
Viscous hydro applies: how much does  $\eta/s$  increase?  
“Semi”-QGP: *partial* deconfinement near  $T_c$ : today

With A. Dumitru, Y. Guo, Y. Hidaka, C. Korthals Altes (DGHKP), 1011....

With Y. Hidaka, 0803.0453, 0906.1751, 0907.4609, 0912.0940

Semi-classical approach in *intermediate* coupling:

Hietanen, Kajantie, Laine, Rummukainen, & Schröder, ph/0503061...0811.4664

Andersen, Leganger, Strickland, & Su: ...0911.0676, 1005.1603, 1009.4644

3. *Nothing* like it: elliptic flow *much* larger; (scaled) multiplicity - *much* higher?  
Not “Wit-less”: Busza, arXiv: 0907.4719  
Terra incognita: *non-equilibrium* distribution

# The semi-, versus the complete, Quark Gluon Plasma

Typical plasma in QED: e.g., of H atoms

Completely ionized plasma, e<sup>-</sup>'s and p's move freely of one another

*Partially* ionized plasma: *some* H atoms, *some* free charges.

QCD: deconfinement is the ionization of *color* charge

*No* ionization: confined phase: below  $T_c$

Total ionization: “*complete*” Quark-Gluon Plasma

Lattice: complete QGP above a “few” times  $T_c$

*Partial* ionization: “*semi*”-QGP

From a little bit *below*  $T_c$ , to a “few” times  $T_c$

What is a “few” times times  $T_c$ ?

Conclusion: used to think semi-QGP *broad*,  $T_c^+$  to  $\sim 4.0 T_c$

Today: *narrow*,  $T_c^+$  to  $\sim 1.5 T_c$  .

If RHIC starts in the semi-QGP, and LHC starts in the complete QGP, then for heavy ions, LHC will *not* be like RHIC.

(Many, many qualifications: LHC always cools through semi-QGP, etc....)

# SU(3) gauge theory as a 3-state “clock” model

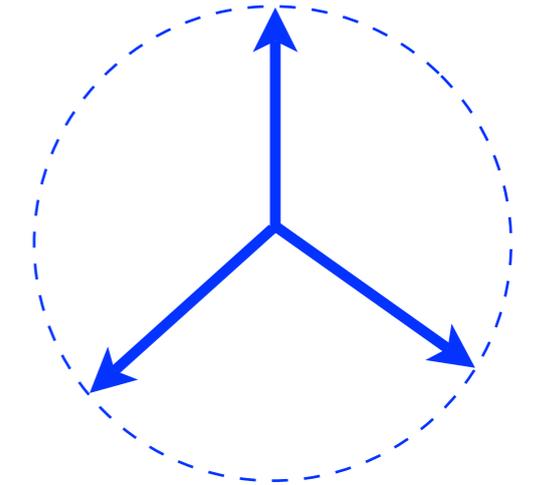
Let  $U_c =$  gauge transf. = *constant* phase.

SU(3):  $\det U_c = 1$ , so  $U_c$  *third* root of unity:

$$U_c = \left( e^{2\pi i/3} \right)^j, \quad j = 0, 1, 2$$

Under  $U_c$ , gluons *invariant*:  $A_\mu \rightarrow e^{-2\pi i/3} A_\mu e^{2\pi i/3} = A_\mu$

but quarks *not*.  $\psi \rightarrow e^{2\pi i/3} \psi$

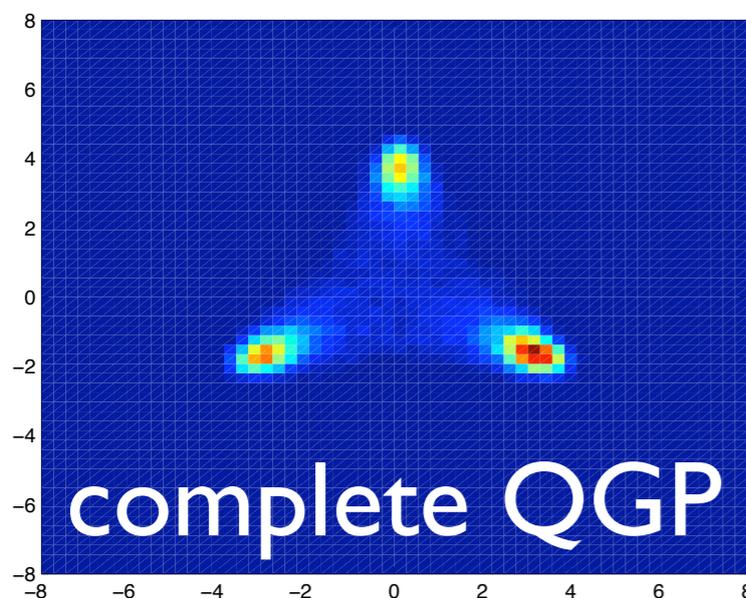


‘t Hooft: Z(3) spin from SU(3) color

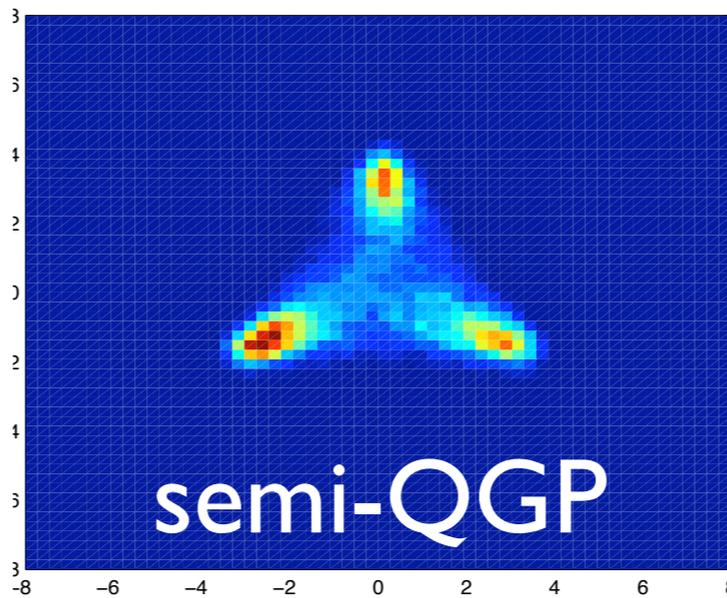
Lattice: Z(3) spin symmetry  $\sim$  ok with three light flavors.

Measure with thermal Wilson line

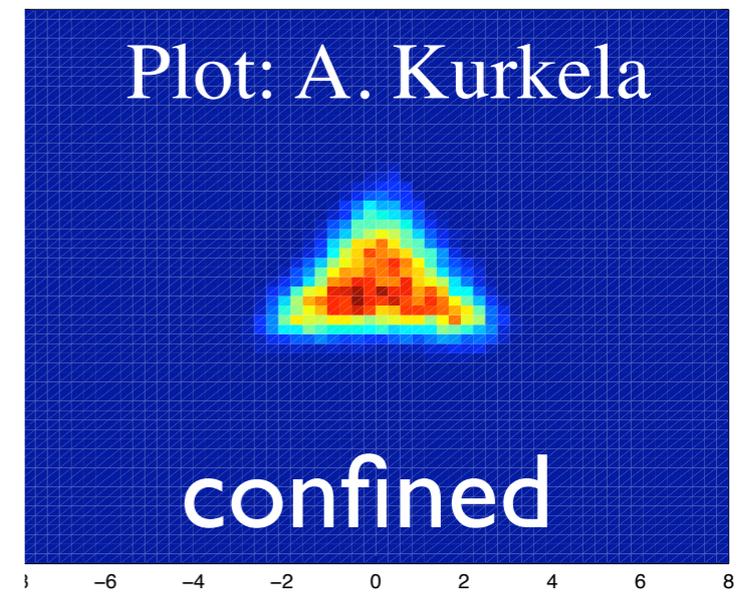
$$\mathbf{L} = e^{ig \int_0^{1/T} A_0 d\tau}$$



$T \gg T_c$

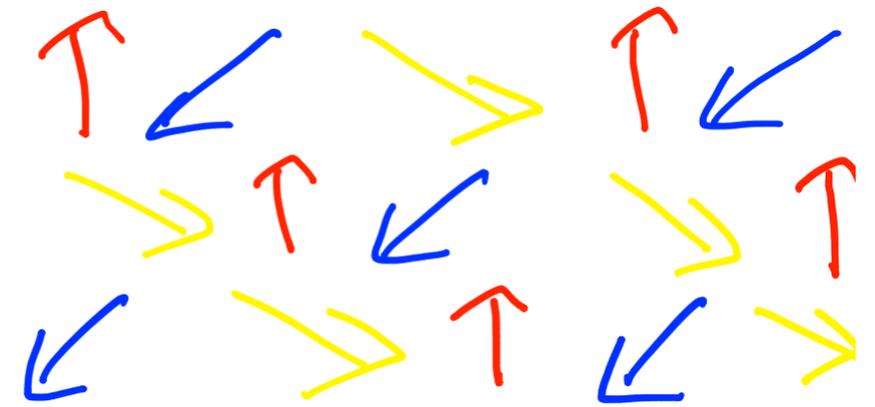
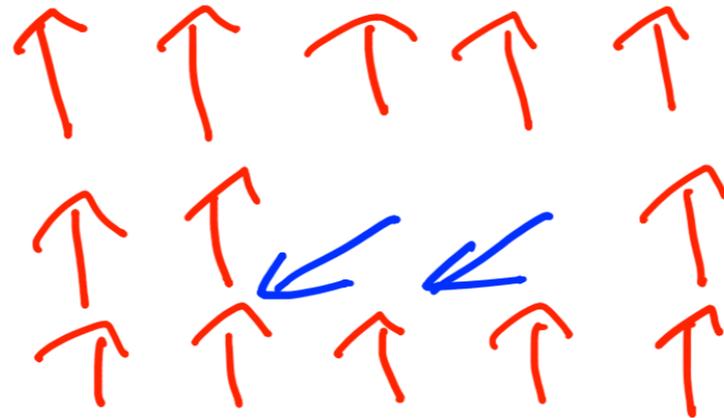
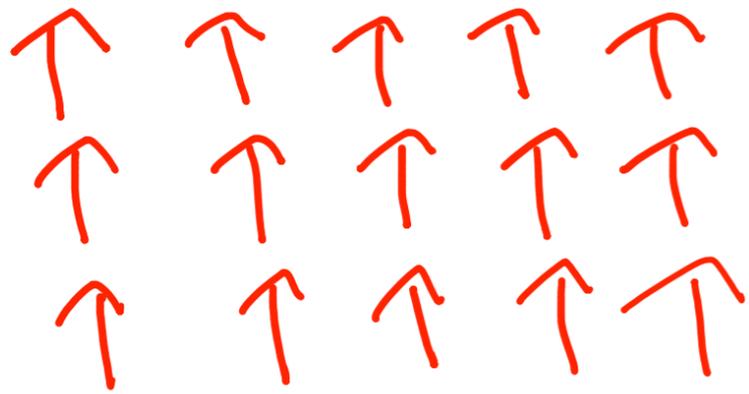


$T \sim T_c$



$T < T_c$

# Deconfining transition as a clock model



Complete QGP ↑  
ordered spin system  
 $T \gg T_c$

“Semi”-QGP ↑  
Some spin defects  
 $T > T_c$

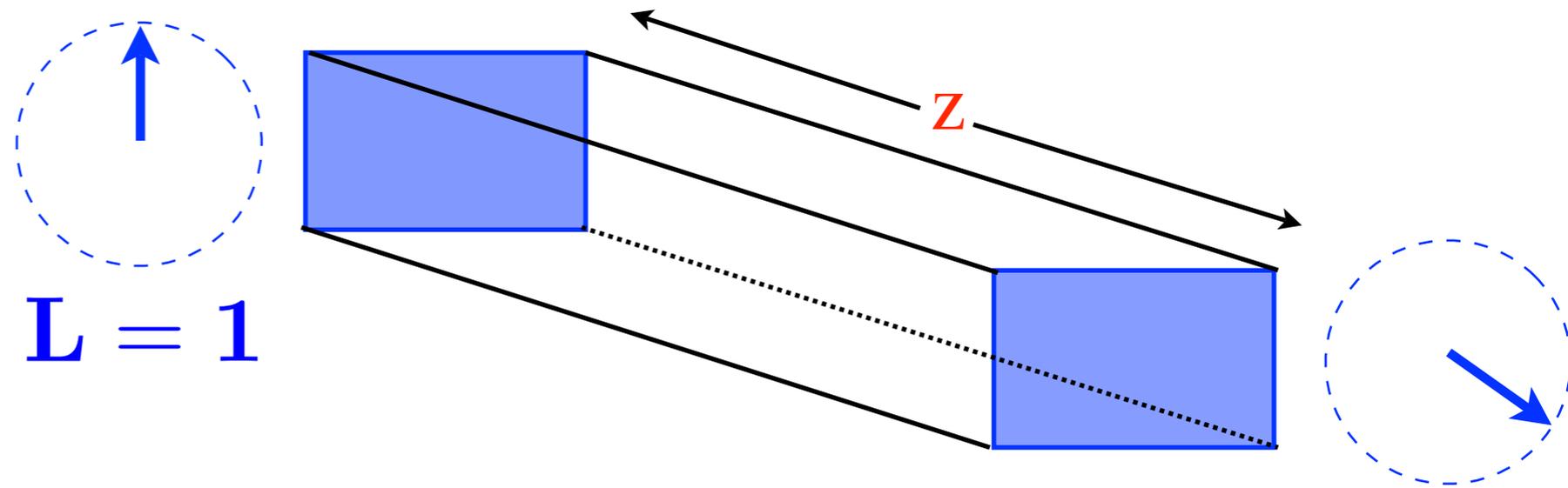
Confined Phase ↑  
completely disordered spins  
 $T < T_c$

How to compute defects? Consider a box, long in one spatial direction.

Put one spin at one end,  
another spin at the other.

Degenerate vacua at  
both ends. In between,  
an interface forms, tunnel  
between degenerate vacua.

Can compute this (order-order) “interface tension”.



$$\mathbf{L} = e^{\frac{2\pi i}{3}} \mathbf{1}$$

## Path for $Z(3)$ interface

Consider a background field,

$$A_0^{cl} = \frac{2\pi T}{3g} q t_8 \quad t_8 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

Along this  $t_8$  direction,

$$\mathbf{L}(q) = e^{\frac{2\pi i}{3} q t_8} \quad \mathbf{L}(1) = e^{2\pi i/3} \mathbf{1}$$

Hence the boundary conditions are  $q = 0$  at one end of the box,  $q = 1$  at the other.

Compute one loop determinant in background field:

$$V_{eff} \sim \# T^4 (ct. + q^2(1 - q)^2)$$

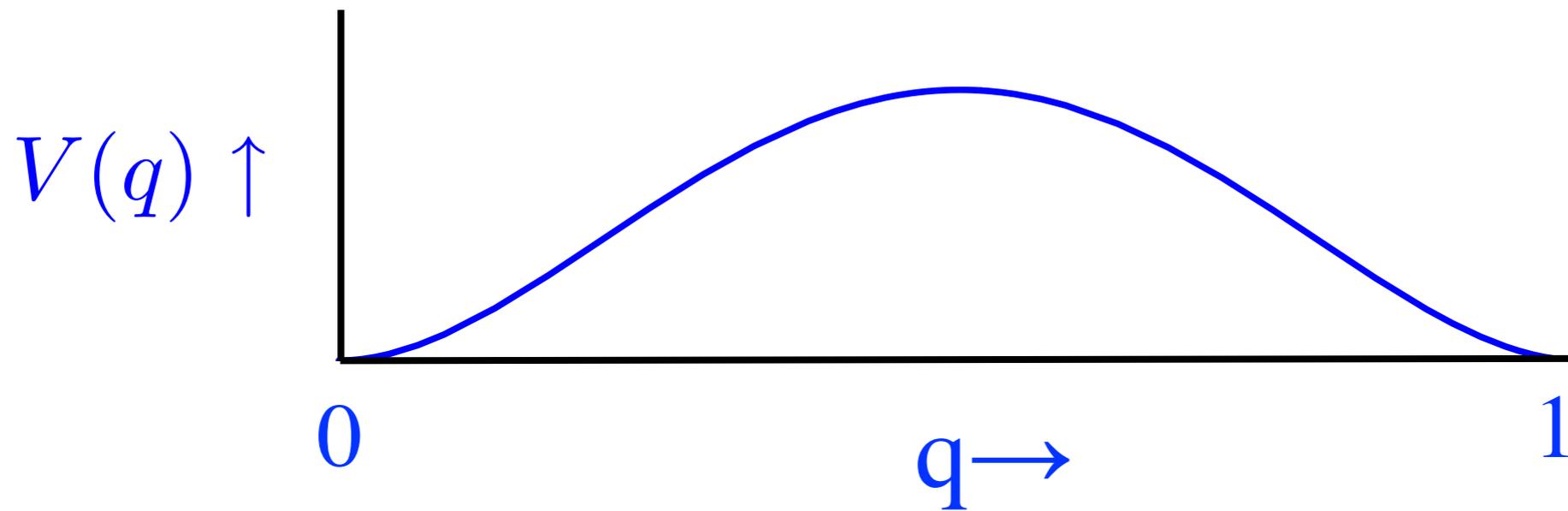
Constant = ideal gas term for gluons.

Bhattacharya, Gocksch, Korthals-Altes & RDP, hep-ph/9205231

# Interface tension

Electric field  $\partial_i A_0 \sim (1/g) dq/dz$ ,  
so effective Lagrangian

$$L_{eff} \sim \frac{T^2}{g^2} \left( \frac{dq}{dz} \right)^2 + \# T^4 q^2 (1 - q)^2$$



Standard tunneling problem in 1 dimension.  
Action for tunneling interface tension:

$$\alpha_{inter} \sim \frac{T^3}{\sqrt{g^2}}$$

Interface tension equivalent to 't Hooft loop,  
wrapping around center of box: measures response to  $Z(3)$  magnetic charge

Korthals-Altes, Kovner & Stephanov, hep-ph/9909516

# Path to confinement

Now consider another background field

$$A_0^{cl} = \frac{2\pi T}{3g} q_c t_3 \quad t_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Along the  $t_3$  direction,

$$\mathbf{L}(q_c) = e^{\frac{2\pi i}{3} q_c t_3} \quad \mathbf{L}(q_c = 1) = e^{\frac{2\pi i}{3} t_3} = \begin{pmatrix} e^{2\pi i/3} & 0 & 0 \\ 0 & e^{-2\pi i/3} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Note:  $\mathbf{L}(1) = e^{\frac{2\pi i}{3}} \mathbf{L}(1)$       Hence:  $\text{tr } \mathbf{L}(1) = \text{tr } \mathbf{L}^2(1) = 0$

Thus  $q_c = 1$  is the *confined* vacuum for SU(3).

$q_c = 0$  is the usual perturbative vacuum.

$$V_{eff} \sim \# T^4 (ct. + q_c^2 (1 - q_c)^2)$$

$V_{eff}$  to  $\sim g^3$ : Giovannangeli & Korthals Altes, hep-ph/0412322

$\sim g^4$ : Korthals-Altes, Schroder, & Vuorinen, in progress

# Effective matrix model for confinement

In pert. thy, perturbative vacuum stable: need *new* terms to drive confinement.

Meisinger, Miller, & Ogilvie (MMO), hep-ph/0108009:

Add, *by hand*, a non-pert. potential,  $\sim T^2$  (“Fuzzy Bag”: RDP, hep-ph/0612191)

$$V_{\text{non-pt}} = T^2 \Lambda^2 (c_1 q(1-q) + c_2 q^2(1-q)^2 + c_3)$$

$\Lambda$  mass parameter;  $c_1, c_2, c_3$  dim.’less parameters. Fix one by  $p(T_c) = 0$ .

MMO: only one parameter,  $c_1$ . Can add  $\infty$  series of polynomials in  $q(1-q)$ .

*Need term*  $\sim c_1$  : with  $c_1, \langle q \rangle \sim 1/T^2$ .

Otherwise, phase *transition* from complete ( $\langle q \rangle = 0$ ) to semi- ( $\langle q \rangle \neq 0$ ) QGP

$$V_{\text{pt}} = \# T^4 q^2(1-q)^2$$

$V_{\text{eff}} = V_{\text{pt}} + V_{\text{non-pt}}$ .  $V_{\text{eff}}$  function of  $q$ ,  $q \in$  Lie *algebra*, not Lie group.

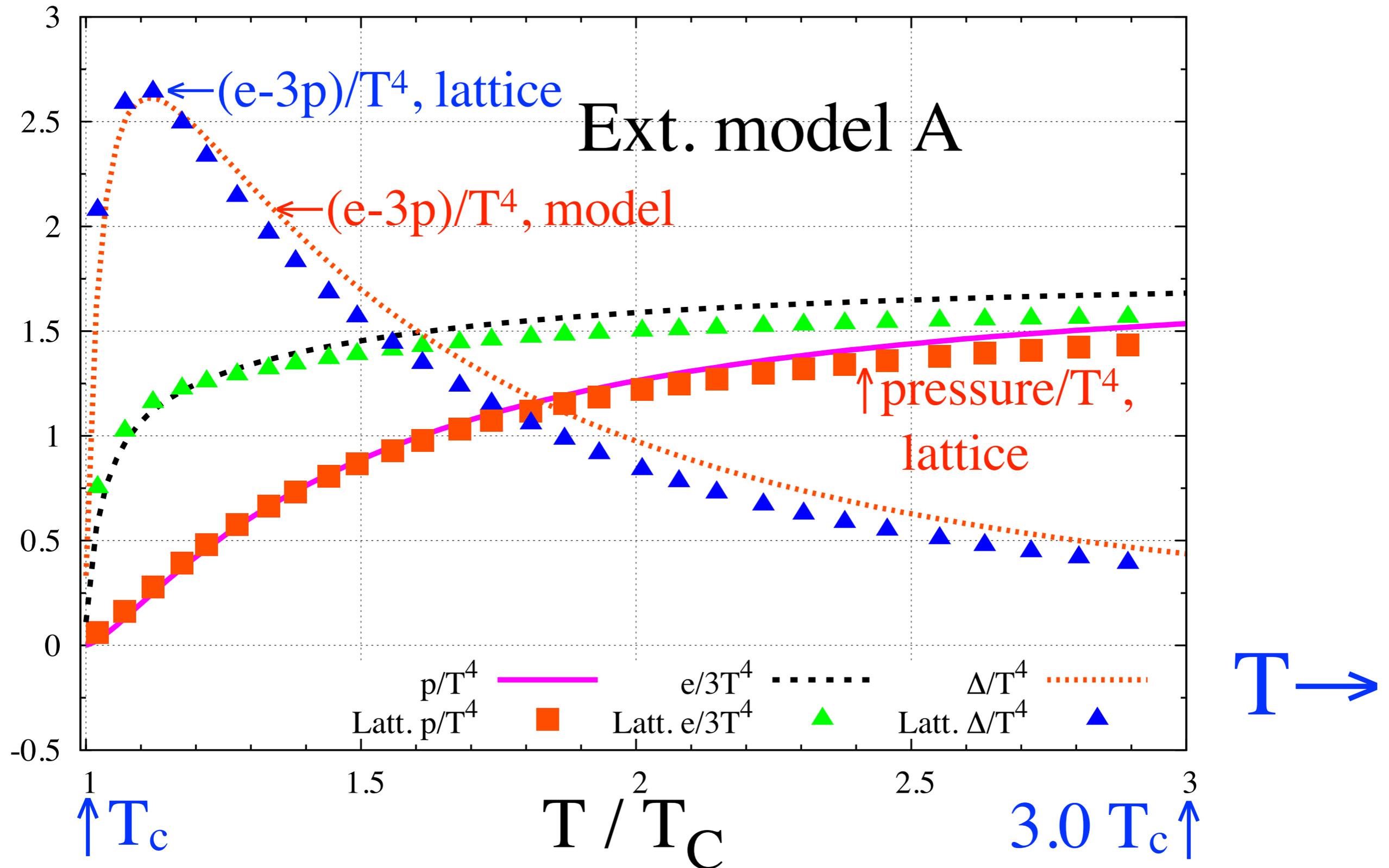
Fit parameters from pressure (or better, interaction measure,  $(e-3p)/T^4$ )

*Then* compute interface tension and gluons masses. Only *effective* theory, *not*

complete: vs Liao & Shuryak: ph/0611131,0804.0255,0804.4890,0810.4116

# Effective matrix model, pure SU(3) glue

Can tune parameters of eff. model to obtain reasonable agreement with pressure:



# Results: 't Hooft loop, two colors

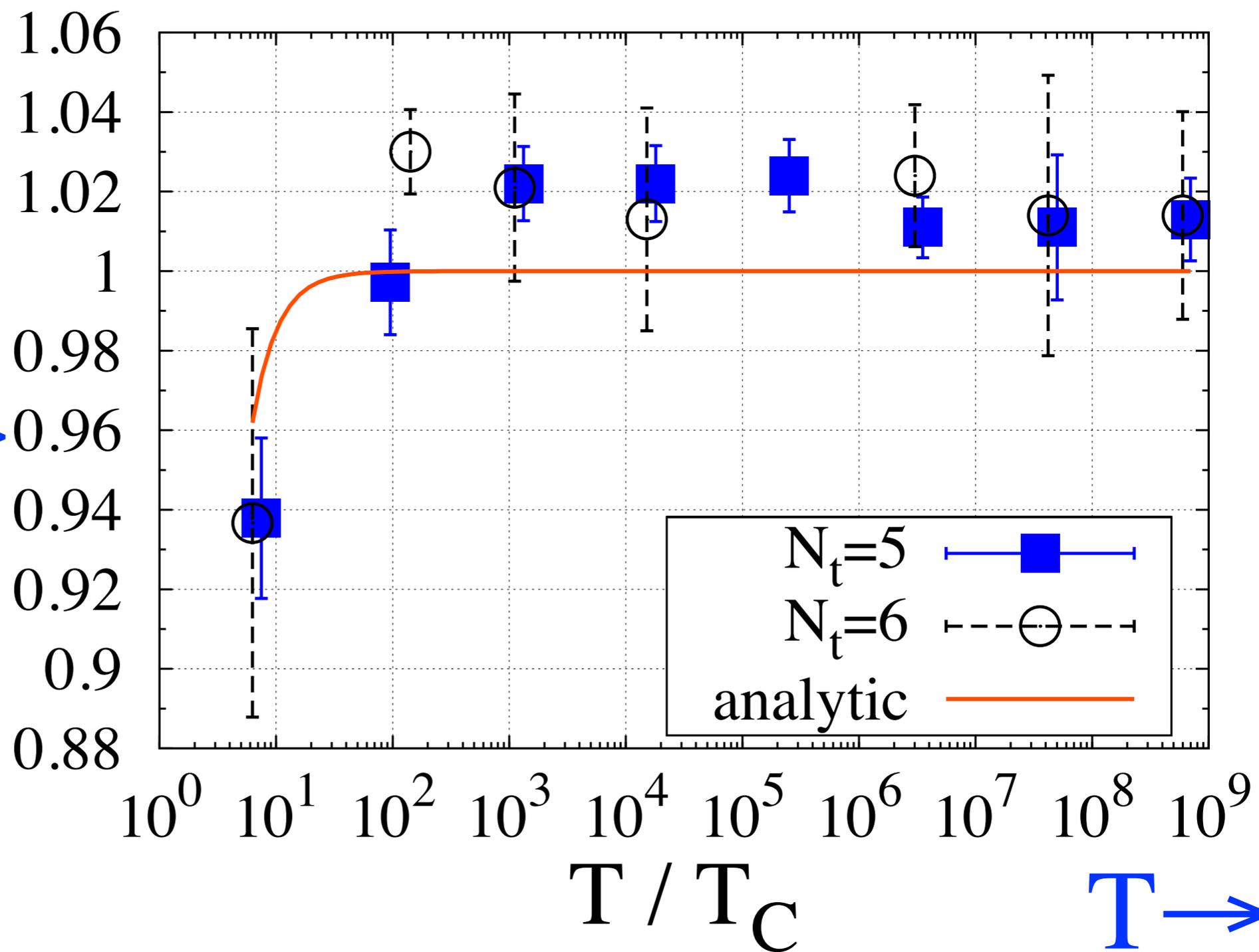
Pure SU(2): 't Hooft loop on lattice, [de Forcrand & Noth hep-lat/0506005](#)

Below: comparison between lattice and effective model: good, need better data.

't Hooft loop =  
Z(2) interface  
tension:

Ratio  
lattice/semi-class. →  
in complete QGP

~ agreement.



## Two types of gluon modes near $T_c$

Compute quantum fluctuations above background field,  
(energy  $p_0 = 2 \pi n T$ ,  $n = 0, \pm 1, \pm 2 \dots$ )

$$(A_0^{cl})_{ab} = \frac{2\pi T}{g} q_a \delta_{ab}$$

$$\langle A_0^{ab}(\vec{x}) A_0^{ba}(0) \rangle$$

$$\sim \int \frac{d^3 p}{(2\pi)^3} e^{i\vec{p}\cdot\vec{x}} \sum_{n=-\infty}^{+\infty} \frac{e^{-ip_0\tau}}{(\vec{p})^2 + ((2\pi T)(n + q_a - q_b))^2 + m_D^2(Q)}$$

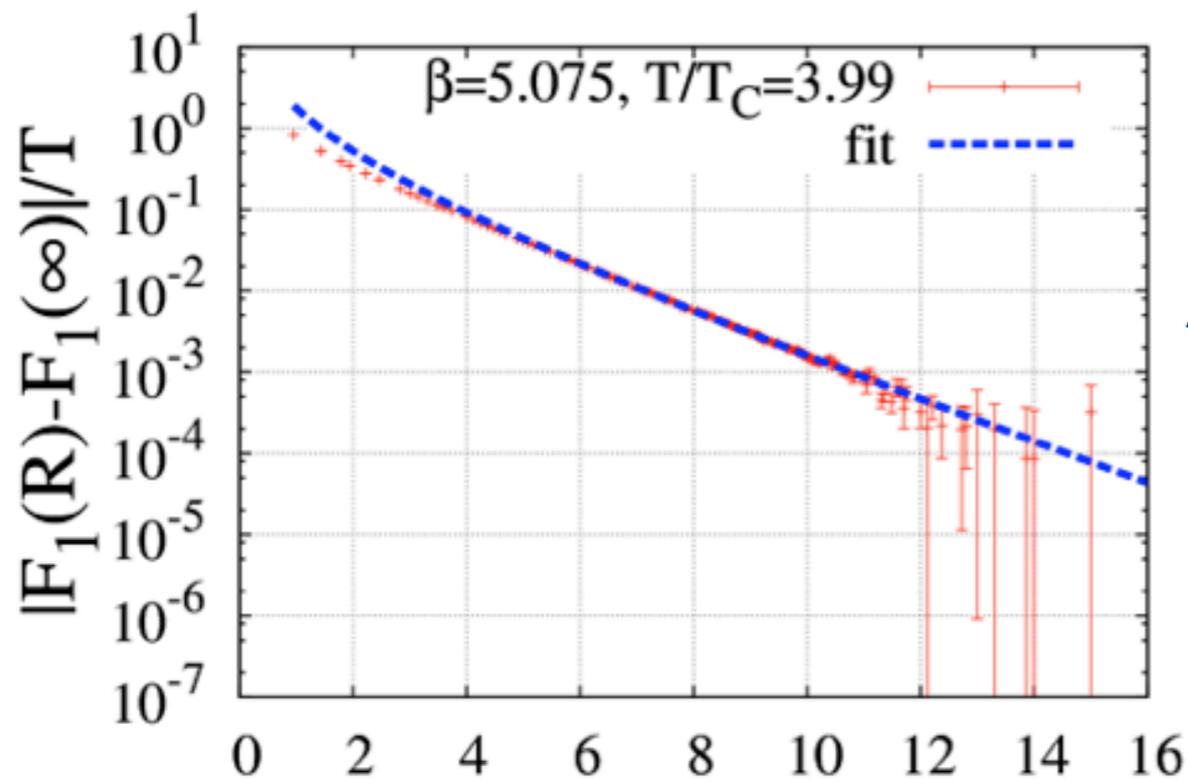
Off-diagonal color fields,  $q_a \neq q_b$  *heavy*: “mass”  $\sim (2 \pi T) (n + q_a - q_b) \sim 2 \pi T$

Diagonal color fields,  $q_a = q_b$  *light*: “mass”  $\sim$  Debye mass,  $m_D(Q) \sim g T$

*Unique prediction in semi-QGP: two types of gluon masses*

# Lattice data, pure SU(3): two masses near $T_c$ ?

O. Kaczmarek, arXiv: 0710.0498

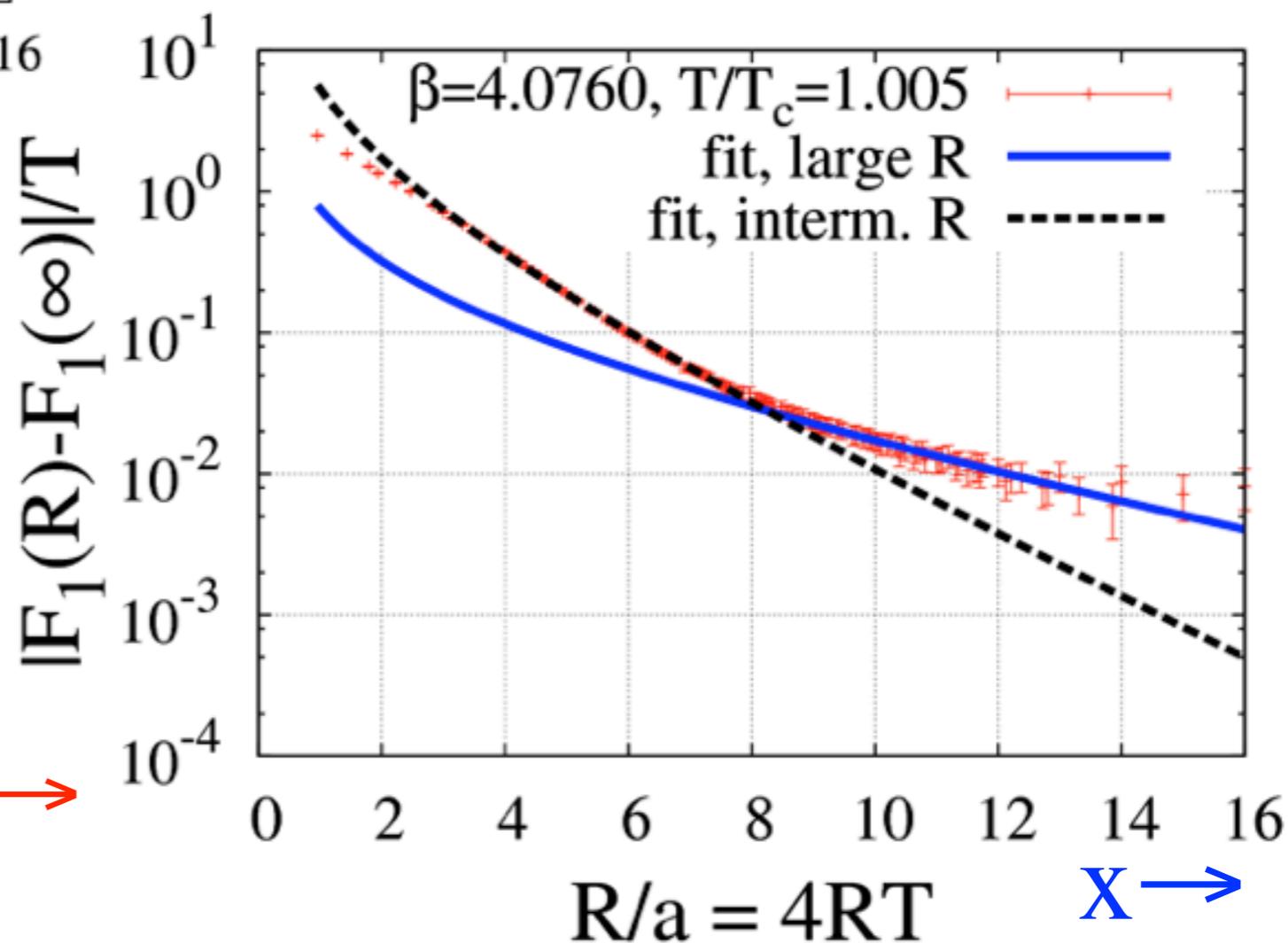


$\uparrow \log \langle A(x)A(0) \rangle$

$T = 4.0 T_c \uparrow$        $R/a$        $X \rightarrow$

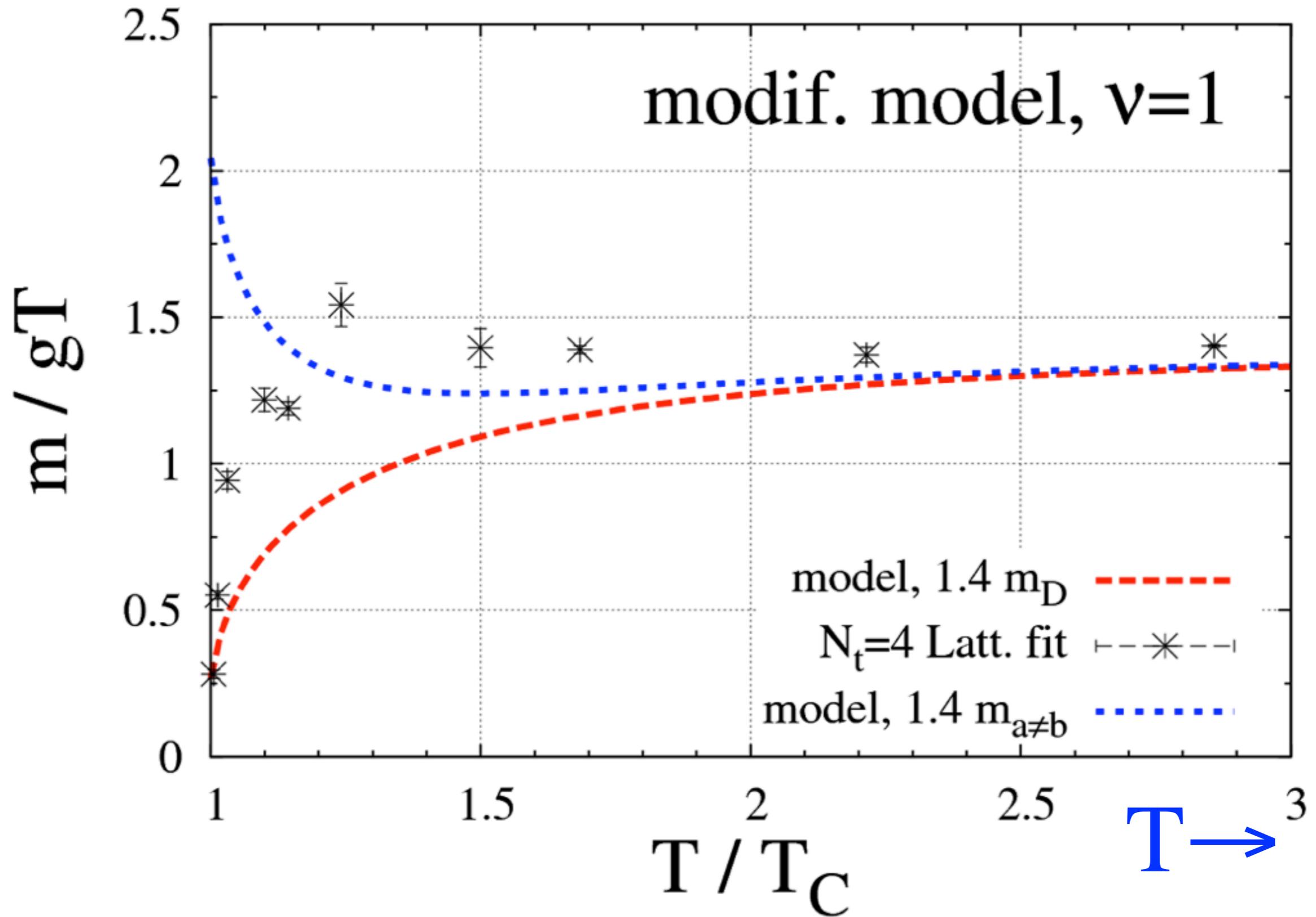
$\uparrow \log \langle A(x)A(0) \rangle$

$T = 1.005 T_c \rightarrow$



$X \rightarrow$

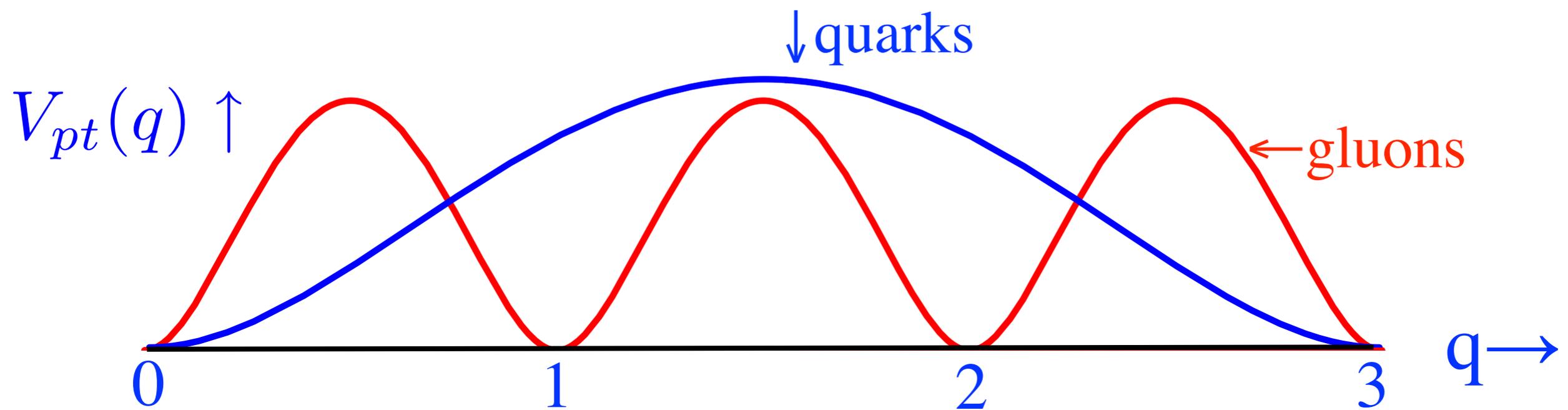
# Comparison: lattice vs model



# Adding quarks

Compute potential for constant  $A_0$  with quarks:

$$A_0^{cl} = \frac{2\pi T}{3g} q t_8$$



**Red:** potential for constant  $A_0$  from  $SU(3)$  gluons

$\langle L \rangle = \exp(2\pi i q/3) \mathbf{1}$ .  $q = 0, 1, 2$  are degenerate  $Z(3)$  vacua.

**Blue:** potential from quarks. Potential at  $q = 1, 2 \neq q = 0, 3$ .

True test: compute effects of dynamical quarks, see how  $T_c$  shifts, etc.

# Shear viscosity in the semi-QGP, 1

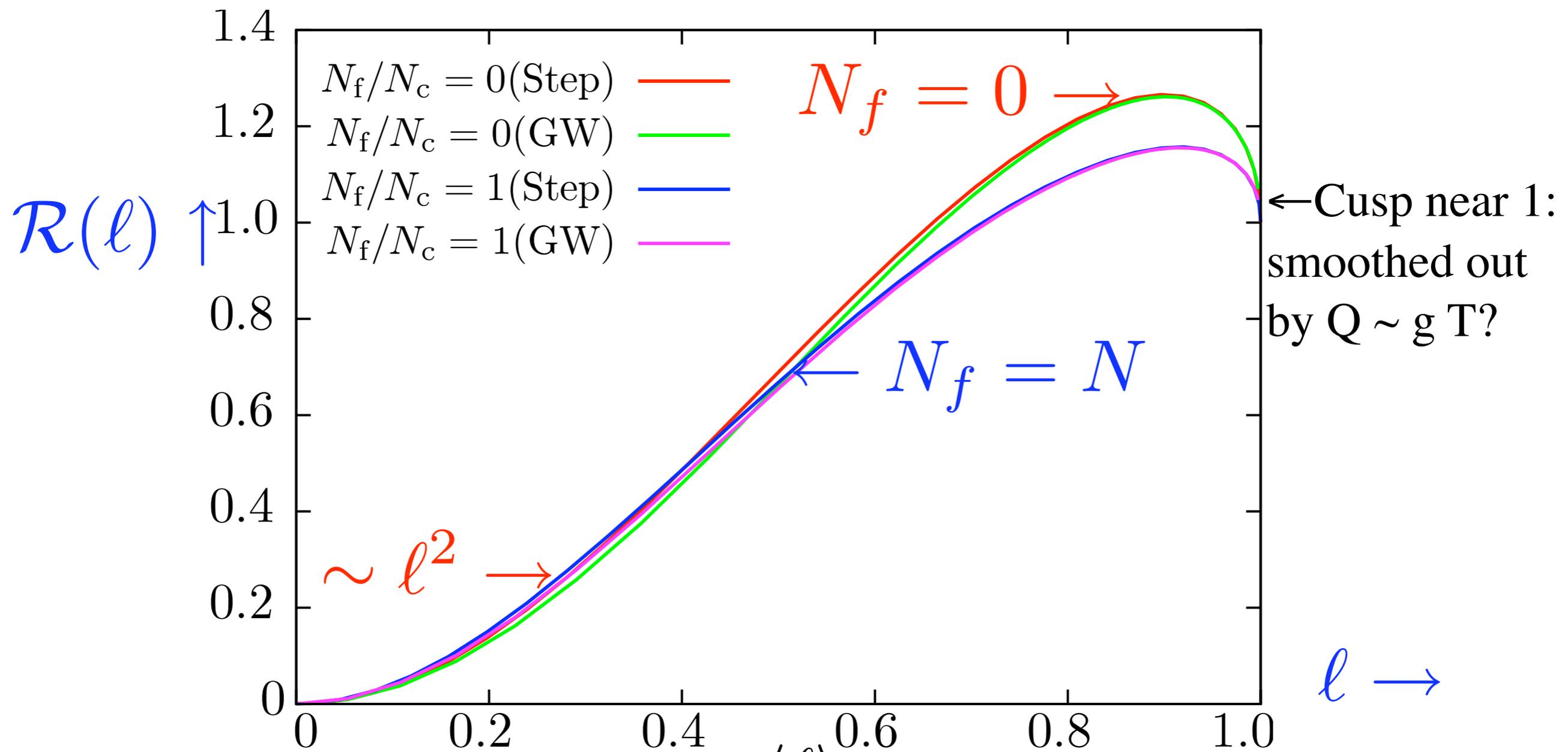
$R(l)$  = ratio of shear viscosity in semi-QGP/(complete QGP) for the *same* value of  $g$

$c_1, c_2$  #'s from

Arnold, Moore, & Yaffe, hep-ph/0302165

As  $l \rightarrow 0, R(l) \sim l^2$ . e.g.,  $R \sim 0.3$  for  $l \sim 0.3$

$$\eta = \frac{c_1 T^3}{g^4 \log(c_2/g)} \mathcal{R}(l)$$

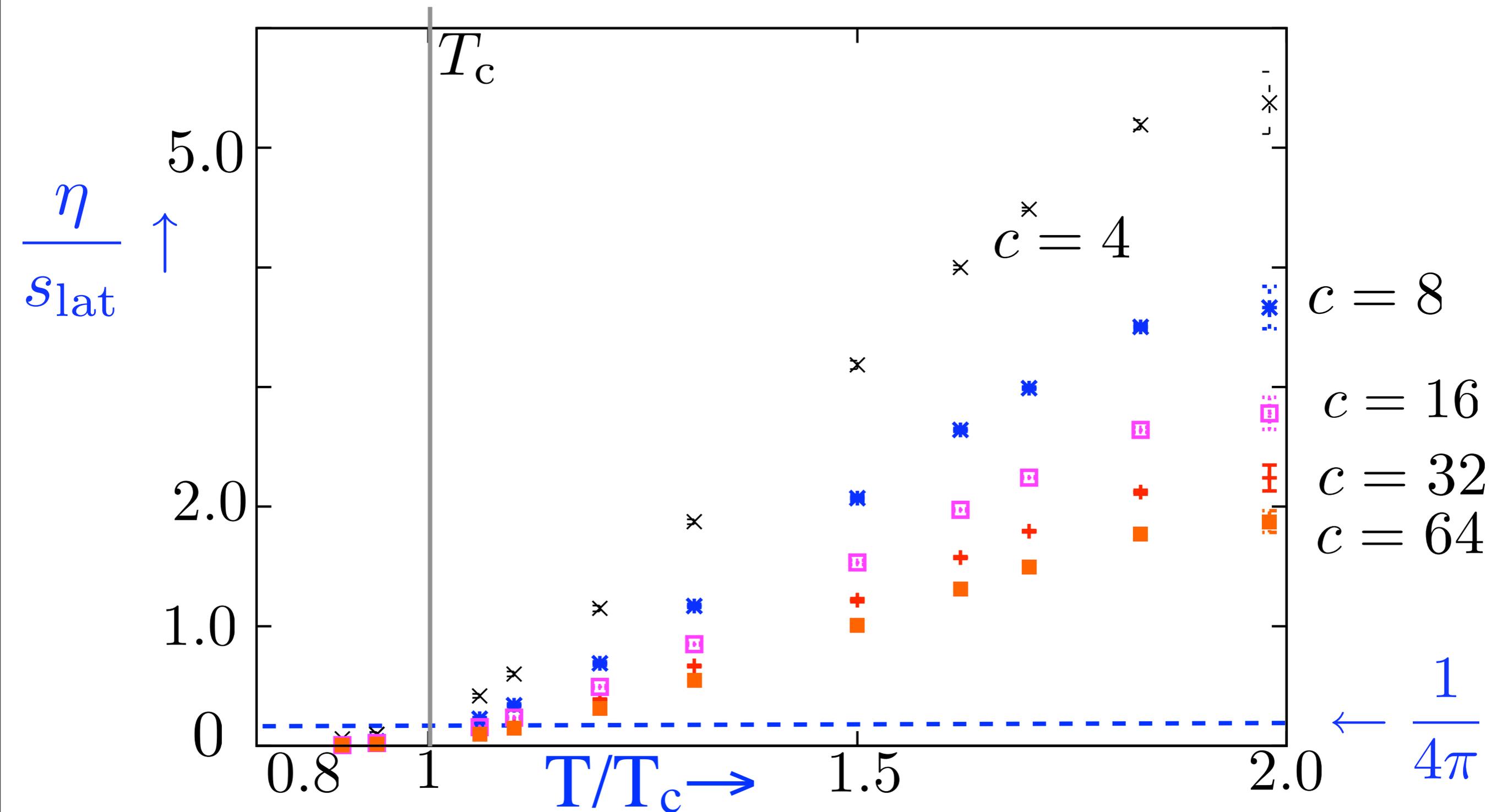


# Shear viscosity in the semi-QGP, 2

Leading log shear viscosity/lattice entropy.  $\alpha_s(T_c) \sim 0.3$ .

*Large increase from  $T_c$  to  $2 T_c$ . Clearly need results beyond leading log.*

*Also need to include: quarks and gluons *below*  $T_c$ , hadrons *above*  $T_c$ . Not easy.*



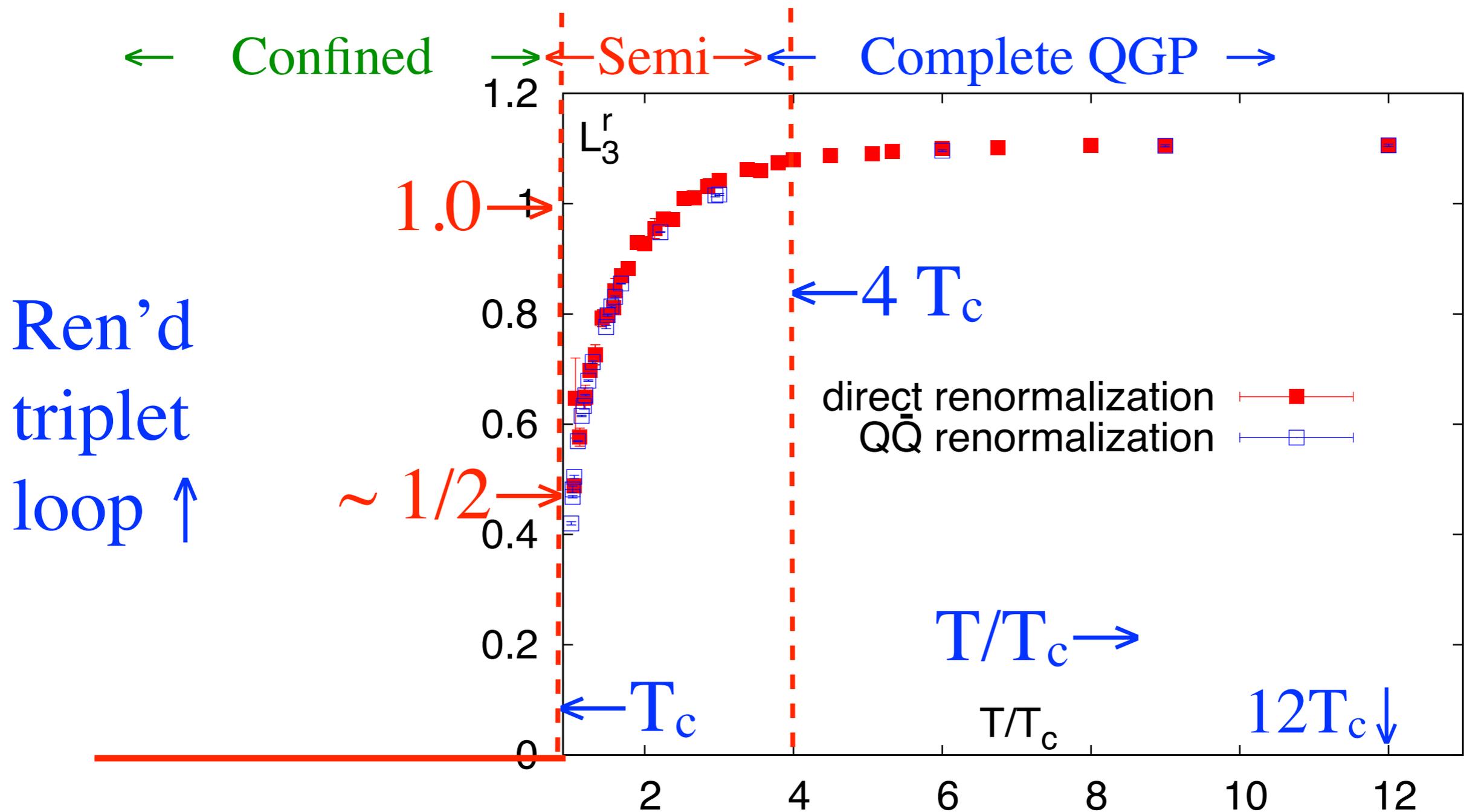
# Lattice: renormalized loop, c/o quarks

Gupta, Hubner & Kaczmarek 0711.2251: Lattice SU(3), no quarks.

Above: semi-QGP *narrow*,  $T_c^+$  to  $\sim 1.5 T_c$ . Lattice: *broad*,  $T_c^+$  to  $\sim 4 T_c$ .

Above agrees with Schwinger-Dyson: Marhauser & Pawłowski, 0812.1144

Our analysis does *not* agree with lattice ren.'d loop: reason for discrepancy?



# Conclusions

RHIC: (mainly) in the semi-QGP?

LHC: deep in the complete QGP?

Shear viscosity *increases* going from the semi- QGP,  
to the complete QGP.

Today: the width of the semi-QGP is *narrow*, from  $\sim T_c$  to  $\sim 1.5 T_c$ ,  
and *not* broad,  $\sim T_c$  to  $\sim 4 T_c$ .

# Conclusions

RHIC: (mainly) in the semi-QGP?

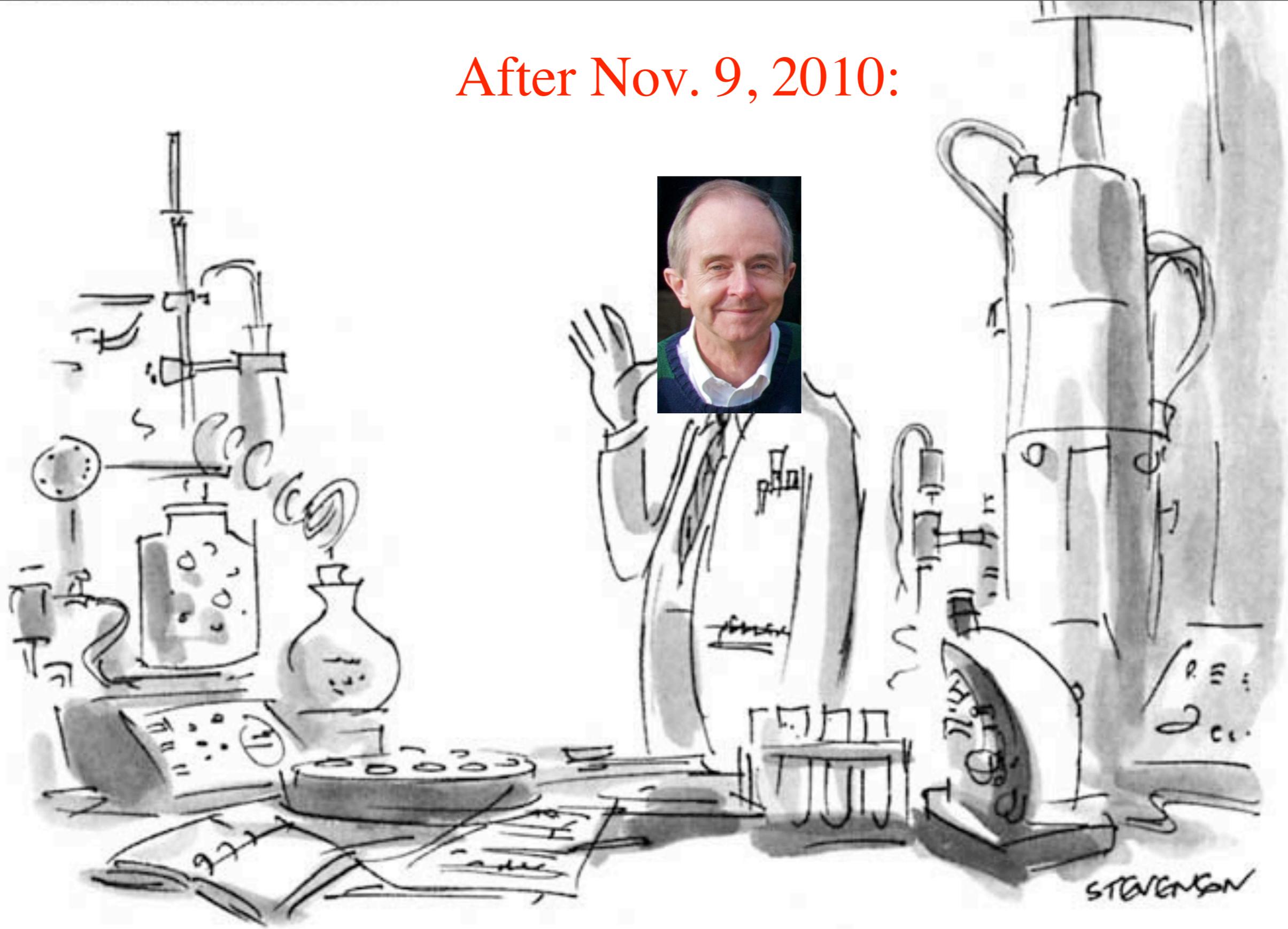
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and *not* broad,  $\sim T_c$  to  $\sim 4 T_c$ .

John Harris: “Expect the Unexpected”

After Nov. 9, 2010:



*"A possible eureka."*