$$\langle \ell \rangle = \frac{1}{2}\left(1 + \sqrt{\frac{\beta - 1}{\beta}}\right) :$$