$$\ell_R \sim (\ell_N)^{p+} \, (\ell_{\overline{N}})^{p-} + O\left(\frac{1}{N}\right)$$