$$\langle \widetilde{\ell}_R \rangle \approx \exp\left(+ \frac{C_R}{N} \frac{(g^2 N)^{3/2}}{8\pi\sqrt{3}} \right)$$