$$\mathrm{tr}\mathbf{L}_{(N^2\pm N)/2} = \frac{1}{2}\left(\left(\mathrm{tr}\mathbf{L}_N\right)^2 \pm \mathrm{tr}\mathbf{L}_N^2\right)$$