$$\mathcal{Z} = \int \Pi \; d\mathbf{L}_N(i) \; \exp\left(-\mathcal{S}(\ell_R(i))\right)$$