$$\mathbf{L}_N = \mathbf{1}_N \longrightarrow \mathrm{tr}\,\mathbf{L}_{adj} = N^2 - 1$$