$$\lambda(p) \sim \frac{1}{\log(p/\mu)}\,,\ p \to 0$$